

Dynamically induced Planck scale and inflation

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ABSTRACT: Theories where the Planck scale is dynamically generated from dimensionless interactions provide predictive inflationary potentials and super-Planckian field variations. We first study the minimal single field realisation in the low-energy effective field theory limit, finding the predictions $n_s \approx 0.96$ for the spectral index and $r \approx 0.13$ for the tensor-to-scalar ratio, which can be reduced down to ≈ 0.04 in presence of large couplings. Next we consider agravity as a dimensionless quantum gravity theory finding a multifield inflation that converges towards an attractor trajectory and predicts $n_s \approx 0.96$ and $0.003 < r < 0.13$, interpolating between the quadratic and Starobinsky inflation. These theories relate the smallness of the weak scale to the smallness of inflationary perturbations: both arise naturally because of small couplings, implying a reheating temperature of 10^{7-9} GeV. A measurement of r by KECK/BICEP3 would give us information on quantum gravity in the dimensionless scenario.

KEYWORDS: Cosmology of Theories beyond the SM, Renormalization Group

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Contents

1	Introduction	1
2	Effective field theory approach	3
2.1	Model-independent dimensionless single field inflation	4
2.2	The minimal model for dimensionless single field inflation	8
3	Inflation in agravity	12
3.1	Agravity in the Einstein frame	12
3.2	Computing multifield inflationary predictions	14
3.3	Inflationary predictions	15
4	Cosmology after inflation	17
4.1	Reheating	18
4.2	Dark matter	19
4.3	Inflation and the weak scale	20
5	Conclusions	21
A	RGE and the compatibility of frames	23

1 Introduction

The discovery of the Higgs boson [1, 2] and the lack (so far) of new physics challenged the standard view on naturalness of the electroweak scale (see presentations at the conferences [3, 4]). The latter led to the expectation that the Higgs boson should be accompanied by new physics at the weak scale that is able to provide a cut-off to quadratically divergent quantum corrections to the squared Higgs mass due to the standard model (SM) couplings.

Given that power divergent quantum corrections do not lead to any physical effect, some theorists are considering the possibility that the Higgs mass fine-tuning problem could be just an unphysical artifact of the standard renormalisation procedure, that introduces an artificial cut-off and unphysical bare parameters. On the contrary, heavy new particles coupled to the Higgs boson would lead to large physical corrections to the Higgs mass: the associated fine-tuning could be probed by experiments [5–7]. Thereby, one is led to redefine natural models as those where new physics heavier than the weak scale is weakly coupled to the Higgs.

Starting from these phenomenological considerations, various authors tried to develop a theoretical framework able of explaining the co-existence and the origin of the largely separated mass scales observed in nature. Most attempts involve, in some way or another,

classical scale invariance and dynamical generation of mass scales [8–39]. Implications for inflation have been explored in [39, 40].

The largest scale observed in Nature so far is the Planck scale. Inflationary [41–43] generation of primordial perturbations [44–46] can provide an observational window on Planck-scale physics. The recent BICEP2/KECK/PLANCK common analysis [47] of the B -mode polarisation data tries to control the astrophysical backgrounds [48] and hints at a value for the tensor-to-scalar ratio $r = 0.06 \pm 0.04$, in-between the previous BICEP2 [49] and Planck [50, 52, 53] results. If future experiments will find a statistically significant evidence for $r > 0$, this might be the first hint of the quantum nature of gravity, and a precise determination of r may help us to discriminate between different ultraviolet (UV) completions of gravity.¹ This result, therefore, invites for thorough common studies of gravity and inflation.

In this paper we explore the implications of the assumption that the Planck scale is generated dynamically, assuming that the same sector also provides inflation. The dynamics leading to dimensional transmutation can be due to strongly-coupled or to weakly-coupled physics. We here focus on weakly coupled dynamics, such that we can perform perturbative computations. The literature contains studies of models with a dynamical Planck scale (see e.g. [39, 56–61]) and of models with a dynamical inflaton potential (already the very first papers on inflation considered the possibility that the inflaton potential is generated dynamically by loop effects [62–64] via the Coleman-Weinberg mechanism [65]). Furthermore, dynamical generation of masses is compatible with the small observed cosmological constant provided that the scalar potential satisfies the ‘multiple point criticality principle’ [66], that was introduced for the SM Higgs boson and is extensively used in Higgs inflation [67, 68]. Originally, the non-minimal coupling for the usual inflaton was considered in [69–73].

In this paper we combine these concepts into a consistent framework and study implications for inflation, gravity and the electroweak scale. We follow two different approaches.

To obtain model independent results we first take an effective field theory approach and study the minimal single field inflation from dynamical generation of the Planck scale without knowing the theory of gravity. We assume that a complete theory of quantum gravity is not needed either because inflation is described by Einstein gravity at sub-Planckian energy or because some completion of Einstein gravity is weakly coupled enough. The inflaton is assumed to be the Higgs of gravity: the pseudo-Goldstone boson of scale invariance that acquires a vacuum expectation value (VEV) generating the Planck mass. The assumption of classical scale invariance allows us to deal with trans-Planckian inflaton field values [74, 75].

We find that in the limit when gravity effects can be ignored the inflationary observables converge towards the predictions of a quadratic inflationary potential [76], up to deviations due to higher order corrections, $n_s \approx 0.96$ and $r \approx 0.13^{+0.01}_{-0.03}$. We formulate conditions when this approximation is valid (details are collected in appendix A) and discuss the equivalence

¹However, an observable value of r can also be obtained for sub-Planckian field variations in certain cases [54, 55].

of Einstein and Jordan frames in this limit. For large values of the non-minimal coupling to gravity, we obtain much wider range for tensor-to-scalar ratio, $r > 0.04$, while the prediction for scalar spectral index remains the same. This is a new and much more constraining result compared to the corresponding result in the previous scale-invariant inflation study [40] due to extra constraints arising from the dynamically generated Planck scale and the dynamically realised multiple point criticality principle. We present the minimal model for this scenario and study its properties.

After the effective field theory study, we focus on a specific possibility for quantum gravity: agravity [39], which is the dimensionless renormalizable extension of Einstein gravity. New gravitational degrees of freedom, predicted by the theory, can be light enough to take part in inflationary dynamics. We thereby have multifield inflation, and we find the prediction $n_s \approx 0.96$ and a tensor-to-scalar ratio $0.003 < r < 0.13$ that interpolates between the values characteristic to quadratic [76] and to Starobinsky [77] inflation. In this context the smallness of the electroweak scale is connected to the smallness of the inflationary perturbations: both arise because the underlying theory is very weakly coupled.

In both cases, gravitational decays of the inflaton reheat the SM particles up to a temperature 10^7 – 10^9 GeV.

The organization of the paper is the following. In section 2 we present our results of the effective field theory approach to dynamically induced gravity and inflation. In section 3 we focus on agravity and compute inflationary parameters in this quantum gravity theory. In section 4 we collect our results on reheating and on dark matter (DM) abundance of the universe. We conclude in section 5 and present technical details in appendix A.

2 Effective field theory approach

In this section we present a general, model independent study of scale-invariant single field inflation in which the Planck scale is dynamically generated by the inflaton. The main aim of our effective field theory approach is to derive results that are valid for all possible UV completions of gravity. We, therefore, restrict our physical parameters such that inflation occurs within the low-energy (sub-Planckian) limit of gravity. More broadly, the hope of deriving general implications for inflation rests on the possibility that, if the scale symmetry is broken dynamically by a VEV induced by *weakly coupled* dynamics, it leaves a *light* scalar, which is the pseudo-Goldstone boson of scale invariance. Two experimental facts support this assumption, suggesting two possibilities where an effective field theory could be adequate:

- 1) First, the amplitude of primordial scalar perturbations is observed to be small, $P_R = (2.14 \pm 0.05) \times 10^{-9}$ [52, 53]. This suggests that inflation occurs at a sub-Planckian energy E , where the gravitational coupling $g(E) \sim E/\bar{M}_{\text{Pl}}$ ($\bar{M}_{\text{Pl}} = 2.4 \times 10^{18}$ GeV is the reduced Planck mass) is still small enough that no knowledge of the UV structure of quantum gravity is needed. We check that our effective field theory is valid in the parameter space we consider and that the results of our computations are trustable. We will explicitly demonstrate that the results obtained in the Jordan and Einstein frames are physically equivalent.

- 2) Second, the smallness of Higgs boson mass, $M_h/\bar{M}_{\text{Pl}} \sim 10^{-16}$ suggests that quantum gravity should be weakly coupled [39, 78], such that the quantum corrections to M_h are naturally small. *Soft-gravity* is the idea that the growth of the gravitational coupling $g(E)$ with energy could be stopped by new gravitational physics at an energy $E \sim M_g$ low enough that $g(E)$ saturates at a small enough value $g(E) \lesssim g(M_g)$. Then soft-gravity can be neglected during inflation even when Einstein gravity would become non-perturbative, extending the domain of validity of our computations.

In practice, both possibilities above amount to ignoring quantum gravity in a controllable way.

2.1 Model-independent dimensionless single field inflation

Assuming no explicit mass scale in the fundamental Lagrangian,² the inflaton field s , singlet under the SM gauge group, has a scalar potential consisting only of a quartic term

$$V = \frac{1}{4} \lambda_S(s) s^4, \quad (2.1)$$

where the self-coupling $\lambda_S(s)$ runs due to interactions (to be specified in the next subsection). The inflaton has a non-minimal coupling to gravity $-f(s)R/2$, where R is the Ricci scalar, parameterised by the dimensionless coupling ξ_S as

$$f(s) = \xi_S s^2. \quad (2.2)$$

We neglect the running of ξ_S in the limit of weak coupling of gravity in the Einstein frame (see appendix A for more details). We assume that the SM degrees of freedom are very weakly coupled to the inflaton and do not affect its dynamics. For example we assume that the allowed inflaton-Higgs mixing term $s^2|H|^2$ is negligibly small. We will show in section 4 that this assumption is compatible with an acceptable reheating of the universe after inflation.

The coupling in eq. (2.2) has the same form as the usual gravitational coupling $-\bar{M}_{\text{Pl}}^2 R/2$ in the Einstein-Hilbert Lagrangian. With the assumptions made above we expect that the Planck scale and the cosmological constant must be generated by quantum corrections encoded in the dynamics of $\lambda_S(s)$. This is, indeed, possible since the running of λ_S allows the scalar potential of s to have a minimum at a non-zero field value. To generate the Planck scale, the VEV v_s of the inflaton field must be given by

$$v_s^2 = \frac{\bar{M}_{\text{Pl}}^2}{\xi_S}. \quad (2.3)$$

To compute inflationary observables we go from the Jordan frame possessing the non-minimal coupling (2.2) to the Einstein frame possessing the canonical Einstein-Hilbert

²In the full theory Lagrangian, the Higgs mass is generated via dimensional transmutation as well. We do not discuss this topic in detail here because it depends on the exact model realisation, which is outside the scope of this section. For further details in the agravity realisation, we refer the reader to the following sections and to [39], where the Higgs mass was generated in such a way.

action of gravity with the Weyl transformation

$$g_{\mu\nu}^E = \Omega(s)^2 g_{\mu\nu}, \quad \text{where} \quad \Omega(s)^2 = \frac{f(s)}{\bar{M}_{\text{Pl}}^2} = \frac{s^2}{v_s^2}. \quad (2.4)$$

The Einstein frame scalar potential is then given by

$$V_E(s) = \frac{V(s)}{\Omega(s)^4} = \frac{1}{4} \lambda_S(s) \frac{\bar{M}_{\text{Pl}}^4}{\xi_S^2}. \quad (2.5)$$

At the minimum the value of this potential must be (very close to) zero in order to yield the tiny positive vacuum energy density that gives the universe its current accelerated expansion.³ In our framework this requirement implies $\lambda_S(v_s) = 0$. The minimum condition on λ_S is

$$\frac{d\lambda_S}{dt}(v_s) = \beta_{\lambda_S}(v_s) = 0, \quad (2.6)$$

where $t = \ln \bar{\mu}$, $\bar{\mu}$ is the renormalisation scale and β_{λ_S} is the β function of λ_S . As usual, we resum log-enhanced quantum corrections by identifying the renormalisation scale $\bar{\mu}$ with the inflaton field value s . Moreover, in order to ensure that $\lambda_S(v_s) = 0$ is not just a stationary point but a minimum, we need to impose the requirement $\beta'_{\lambda_S}(v_s) \equiv d^2\lambda_S(v_s)/dt^2 > 0$. In explicit model realisations of this scenario these requirements imply conditions on the model parameters. We can Taylor expand λ_S around the minimum v_s obtaining

$$\lambda_S(s) = \frac{1}{2!} \beta'_{\lambda_S}(v_s) \ln^2 \frac{s}{v_s} + \frac{1}{3!} \beta''_{\lambda_S}(v_s) \ln^3 \frac{s}{v_s} + \dots, \quad (2.7)$$

where we have used $\lambda_S(v_s) = \beta_{\lambda_S}(v_s) = 0$. In any model, this is a perturbative expansion that holds for small enough couplings.⁴ Assuming weak couplings in order to get the correct small amplitude of primordial fluctuations, we will treat $\beta'_{\lambda_S}(v_s)$ and $\beta''_{\lambda_S}(v_s)$ as small constant parameters. We will show in the next subsection that this approximation can indeed hold in the explicit model realisation.

It is convenient to rewrite V_E in terms of the canonically normalised field s_E in the Einstein frame,

$$s_E = \sqrt{\frac{1+6\xi_S}{\xi_S}} \bar{M}_{\text{Pl}} \ln \frac{s}{v_s}, \quad (2.8)$$

or equivalently

$$s = v_s e^{\sqrt{\frac{\xi_S}{1+6\xi_S}} \frac{s_E}{\bar{M}_{\text{Pl}}}}. \quad (2.9)$$

Inserting (2.7) and (2.9) into (2.5) we get

$$V_E(s_E) \simeq \frac{\beta'_{\lambda_S}(v_s) \bar{M}_{\text{Pl}}^2}{8\xi_S(1+6\xi_S)} \left(1 + \sqrt{\frac{\xi_S}{1+6\xi_S}} \frac{\beta''_{\lambda_S}(v_s)}{3\bar{M}_{\text{Pl}}\beta'_{\lambda_S}(v_s)} s_E \right) s_E^2, \quad (2.10)$$

³Notice that the ‘multiple point criticality’ principle of [66] arises in the context of dynamical generation of scales because the dimensionless potential of eq. (2.1) necessarily has another, unphysical, minimum with zero cosmological constant at $s = 0$.

⁴Ref. [39] used a simpler approximation, neglecting also the $\ln^3 s$ term. Here we investigate its impact. Of course, an extra $\ln^4 s$ term is needed in order to stabilise the potential for $s \ll v_s$.

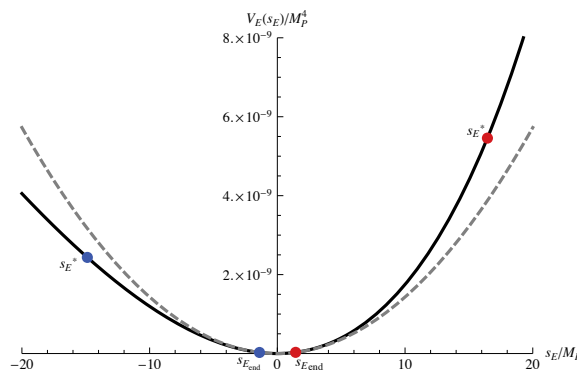


Figure 1. The Einstein-frame inflation potential $V_E(s_E)$ (solid) as computed in the minimal model of section 2.2, and its quadratic approximation (dashed). Blue dots show s_E^* and $s_{E\text{end}}$ for negative-field inflation and red dots for positive-field inflation. Other parameters are specified in the text.

which is nothing but a quadratic potential with a cubic correction. Such a potential is symmetric under the transformation $s_E \rightarrow -s_E$ and $\beta''_{\lambda_S}(v_s) \rightarrow -\beta''_{\lambda_S}(v_s)$, therefore by redefining the sign of s_E we can always assume that $\beta''_{\lambda_S}(v_s) \geq 0$. This potential allows for two different types of inflation:

- Negative-field inflation, when s_E rolls down from negative values to zero. This corresponds, in the Jordan frame, to small-field inflation (s rolls down from a value $s < v_s$ to v_s) for $\beta''_{\lambda_S}(v_s) > 0$ and to large-field inflation (s rolls down from a value $s > v_s$ to v_s) if $\beta''_{\lambda_S}(v_s) < 0$.
- + Positive-field inflation, when s_E rolls down from positive field values to zero. This corresponds, in the Jordan frame, to large-field inflation for $\beta''_{\lambda_S}(v_s) > 0$ and to small-field inflation if $\beta''_{\lambda_S}(v_s) < 0$.

We present in figure 1 an example plot of the Einstein frame potential $V_E(s_E)$, as computed in the minimal model presented later in section 2.2: the potential is well approximated by the cubic potential of eq. (2.10), with the following values of its parameters: $\xi_S(v_s) = 300$, $\beta'_{\lambda_S}(v_s) = 6 \times 10^{-5}$ and $\beta''_{\lambda_S}(v_s) = 9 \times 10^{-6}$. Figure 1 also shows the potential in quadratic approximation (dashed parabola), which is not quite perfect. We denote the field values corresponding to 60 e -folds (s_E^*) and to the end of inflation ($s_{E\text{end}}$) with blue dots for negative-field inflation and with red dots for positive-field inflation. We follow the same colour code throughout this section. Because of the loop-induced cubic term in s_E , the two inflation regimes are physically different and can be distinguished from each other experimentally. The potential in figure 1 yields $r = 0.11$ for negative-field and $r = 0.16$ for positive-field inflation. For large ξ_S , $\beta'_{\lambda_S}(v_s)$ and $\beta''_{\lambda_S}(v_s)$ (given by large couplings), higher order terms in the expansion (2.7) will become important. The cubic approximation breaks down and one has to consider numerically exact running of the couplings.

Under the soft-gravity assumption (described as point 2 at the beginning of section 2), this computation holds in all its parameter space. The model-independent approach (described as point 1) holds instead only as long as Einstein gravity can be neglected. It is

simple to check the validity range of the computations in the Einstein frame. The condition is

$$(V_E(s_E))^{1/4} \ll \bar{M}_{\text{Pl}}, \quad (2.11)$$

so that we can consistently ignore quantum gravity corrections. Such a condition should be realised at least for $s_E = s_E^*$, which corresponds to the maximum potential value for the inflation computations. Ignoring the cubic correction in eq. (2.10) we get

$$\frac{1}{8} \frac{\beta'_{\lambda_S}(v_s)}{\xi_S(6\xi_S + 1)} \ll \left(\frac{\bar{M}_{\text{Pl}}}{s_E^*} \right)^2. \quad (2.12)$$

We considered values of $\beta'_{\lambda_S}(v_s)$, $\beta''_{\lambda_S}(v_s)$ and ξ_S so that eq. (2.11) is satisfied, so that our computations are consistent and we can safely ignore quantum gravity corrections. The consistency condition (2.11) can also be expressed in the Jordan frame as

$$(V_J(s))^{1/4} \ll \sqrt{\xi_S} |s|, \quad (2.13)$$

leading to the same result expressed in (2.12) after taking into account the relation between s and s_E (see eq. (2.8)).

To better understand how the predictions of negative-field inflation differ from positive-field inflation due to the presence of the cubic term $\beta''_{\lambda_S}(v_s)/\beta'_{\lambda_S}(v_s)$, we expand the slow-roll parameters at first order in it. The scalar spectral index n_s and the tensor-to-scalar ratio r are given by

$$\begin{aligned} r &\simeq \frac{8}{N} \mp \frac{32\sqrt{2}}{9} \sqrt{\frac{\xi_S}{6\xi_S + 1}} \frac{\beta''_{\lambda_S}(v_s)}{\beta'_{\lambda_S}(v_s)} \left(\frac{1}{\sqrt{2N}} - \frac{1}{4N^2} \right), \\ n_s &\simeq 1 - \frac{r}{4} \pm \sqrt{\frac{\xi_S}{6\xi_S + 1}} \frac{\beta''_{\lambda_S}(v_s)}{\beta'_{\lambda_S}(v_s)} \frac{\sqrt{r}}{3\sqrt{2}}, \end{aligned} \quad (2.14)$$

where N denotes the number of e -folds, and the signs $+(-)$ should be used for the positive-field inflation and $-(+)$ for negative-field inflation. We see that (2.14) predicts somewhat different behaviour of n_s and r for the positive-field and negative-field inflation scenarios.

The approximation (2.14) breaks down if ξ_S and other couplings are large. In that case the deviation of r from quadratic inflation can be large too, as seen in the minimal model realisation presented in subsection 2.2.

In conclusion, the observed small value of P_R favours a small inflaton self-coupling. If other couplings are small as well, then the Einstein-frame inflaton potential is well approximated by a quadratic potential. If other couplings are large, the deviation of r from quadratic inflation can be strong, as shown in figure 3. In section 3 we will show that in agravity [39] — a concrete UV completion of gravity — dimensionless inflation can give a significantly smaller value of r if all couplings are small. Basically this will arise because agravity realises the soft-gravity scenario by adding to the Lagrangian dimensionless terms of R^2 form (as in Starobinsky inflation), leading to extra light scalars.

2.2 The minimal model for dimensionless single field inflation

In this subsection we present the minimal model that dynamically reproduces all features of dimensionless single field inflation considered in the previous subsection. Besides the inflaton s , the minimal model contains another real scalar σ and a Majorana fermion ψ . This is the minimal field content that is needed to achieve condition (2.6) dynamically. Indeed, the portal coupling of the inflaton with the extra scalar is needed to trigger dimensional transmutation while the extra fermion is needed to be able to tune the minimum of the potential according to the multiple point criticality principle. The latter is possible since the scalar and fermion couplings contribute to the running of the inflaton self-coupling with opposite signs, as is apparent from the RGEs presented in appendix A. This fact has also been used to achieve the multiple point criticality in Higgs inflation [79].

Thus the Jordan frame Lagrangian of the minimal model is

$$\sqrt{-g^J} \mathcal{L}^J = \sqrt{-g^J} \left[\mathcal{L}_{\text{SM}} - \frac{\xi_S}{2} s^2 R + \frac{(\partial s)^2}{2} + \frac{(\partial \sigma)^2}{2} + \frac{i}{2} \bar{\psi}^c \not{D} \psi + \mathcal{L}_Y - V \right], \quad (2.15)$$

$$\mathcal{L}_Y = \frac{1}{2} y_S s \bar{\psi}^c \psi + \frac{1}{2} y_\sigma \sigma \bar{\psi}^c \psi, \quad (2.16)$$

$$V = \frac{1}{4} \lambda_S s^4 + \frac{1}{4} \lambda_{S\sigma} s^2 \sigma^2 + \frac{1}{4} \lambda_\sigma \sigma^4, \quad (2.17)$$

where we neglected the couplings to the SM fields, as suggested by the hierarchy problem. In the Einstein frame, the Lagrangian reads

$$\begin{aligned} \sqrt{-g^E} \mathcal{L}^E = \sqrt{-g^E} \left[\frac{\mathcal{L}_{\text{SM}}}{\Omega(s)^4} - \frac{1}{2} M_{\text{Pl}}^2 R \right. \\ \left. + \frac{(\partial s_E)^2}{2} + \frac{(\partial \sigma_E)^2}{2} + \frac{i}{2} \bar{\psi}_E^c \not{D} \psi_E + \mathcal{L}_{Y_E} - V_E + \dots \right], \end{aligned} \quad (2.18)$$

$$\mathcal{L}_{Y_E} = \frac{1}{2} y_S v_s \bar{\psi}_E^c \psi_E + \frac{1}{2} y_\sigma \sigma_E \bar{\psi}_E^c \psi_E \equiv \frac{1}{2} m_\psi \bar{\psi}_E^c \psi_E + \frac{1}{2} y_\sigma \sigma_E \bar{\psi}_E^c \psi_E, \quad (2.19)$$

$$V_E = \frac{1}{4} \lambda_S v_s^4 + \frac{1}{4} \lambda_{S\sigma} v_s^2 \sigma_E^2 + \frac{1}{4} \lambda_\sigma \sigma_E^4 \equiv \Lambda + \frac{1}{2} m_\sigma^2 \sigma_E^2 + \frac{1}{4} \lambda_\sigma \sigma_E^4, \quad (2.20)$$

where, in order to have canonical kinetic terms, the Einstein-frame scalar and fermion fields are defined as

$$\sigma_E = \frac{\sigma}{\Omega(s)}, \quad \psi_E = \frac{\psi}{\Omega(s)^{\frac{3}{2}}}, \quad (2.21)$$

whereas gauge vectors are invariant under the transformation. It can be shown that the derivative of the denominator in (2.21) cancels out in the fermion kinetic term because of the spin connection contribution in \not{D} [80–82], whereas for scalars (with the exception of the canonically normalised inflaton field s_E) it induces a derivative interaction. For simplicity we omit these details in the above Lagrangian, which are essential for reheating the universe after inflation and will be discussed in section 4. Below, we work in the Einstein frame and omit indices (except for s_E).

Note that in the scalar potential and in the Yukawa terms of the high scale inflationary physics the scale transformation is equivalent to the substitution $s \rightarrow v_s$ and, therefore, in the Einstein frame the fermion ψ and the scalar σ do not have couplings to the inflaton at

tree-level. The Jordan frame self-coupling term of the inflaton becomes the cosmological constant Λ in the Einstein frame potential (2.20) (equivalent to (2.5)). The Yukawa and quartic portal terms of the inflaton become mass terms, giving the mass of the σ field in the Einstein frame by

$$m_\sigma^2 = \frac{1}{2} \lambda_{S\sigma}(v_s) \frac{\bar{M}_{\text{Pl}}^2}{\xi_S}, \quad (2.22)$$

and the mass of the fermion ψ in the Einstein frame by

$$m_\psi = y_S(v_s) \frac{\bar{M}_{\text{Pl}}}{\sqrt{\xi_S}}. \quad (2.23)$$

The scalar potential depends on the inflaton field only due to the running of the scalar couplings.

The renormalisation group equations (RGEs) of the model in the weakly coupled gravity limit are computed in appendix A. In the Jordan frame, gravity does not contribute to the running of the couplings at the one-loop level [119]. The transformation to the Einstein frame mixes the gravitational and scalar degrees of freedom such that in the Einstein frame the matter RGEs get contributions from gravity, that we neglect. We can explicitly verify the equivalence of the frames only up to these neglected effects, as discussed in appendix A around eq. (A.15).

We suppose that inflation takes place along the s field direction (that is, $\sigma = 0$). We will see later that such an assumption is self-consistent: since the scalar σ will turn out to be heavier than the inflaton, it does not take part in inflation. As discussed earlier, we need to realise $\lambda_S(v_s) = \beta_{\lambda_S}(v_s) = 0$. Imposing $\lambda_S(v_s) = 0$, the second condition becomes (see eq. (A.1)),

$$16\pi^2 \beta_{\lambda_S}(v_s) = \frac{1}{2} \lambda_{S\sigma}^2 - 4y_S^4 = 0, \quad (2.24)$$

Moreover, in order to ensure that v_s is not just a stationary point but a minimum, we need to impose that $\lambda_S''(v_s) = \beta_{\lambda_S}'(v_s) > 0$. At the minimum

$$\begin{aligned} \beta_{\lambda_S}'(v_s) &= \frac{1}{16\pi^2} [8y_S(\lambda_S - 2y_S^2)\beta_{y_S} + 4(9\lambda_S + y_S^2)\beta_{\lambda_S} + \lambda_{S\sigma}\beta_{\lambda_{S\sigma}}] \\ &= \frac{\lambda_{S\sigma}^2 [6\lambda_\sigma + (4 - \sqrt{2})\lambda_{S\sigma} - (4 + 6\sqrt{2})y_\sigma^2]}{256\pi^4}, \end{aligned} \quad (2.25)$$

where we have used $\lambda_S(v_s) = 0$ and the relations (2.3) and (2.24).

Physically, it means that the inflaton mass in the Einstein frame,

$$m_{s_E}^2 = \frac{\beta_{\lambda_S}'(v_s) \bar{M}_{\text{Pl}}^2}{4\xi_S(1 + 6\xi_S)}, \quad (2.26)$$

has to be positive. Since m_σ arises at tree-level, while m_{s_E} arises at loop level, the σ field is typically heavier than the inflaton field and remains frozen at its minimum $\sigma = 0$ during inflation. We thereby have realised the single field scenario discussed in the previous subsection. The presence of a non-vanishing Yukawa coupling y_S is needed in order to realise dynamical generation of the Planck scale with a vanishing cosmological constant;

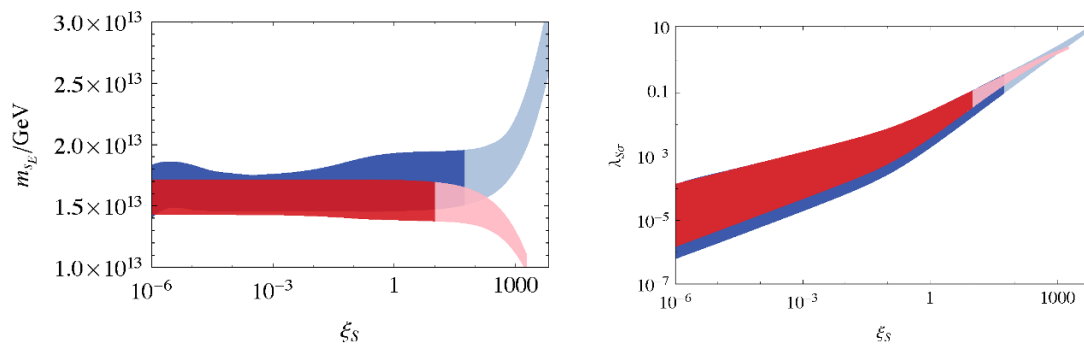


Figure 2. Acceptable range of parameters in the minimal dimensionless inflation model. *Left:* inflaton mass m_{s_E} as a function of ξ_S . *Right:* the inflaton- σ coupling $\lambda_{S\sigma}$ as a function of ξ_S . Blue means negative-field and red means positive-field inflation. Lighter colours mark the regions where gravity cannot be ignored in the Einstein frame.

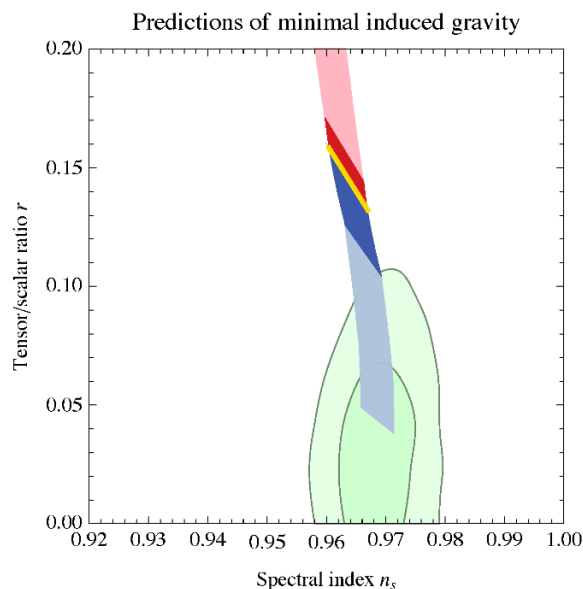


Figure 3. Predictions of dimensionless single field inflation in the (n_s, r) plane for $50 < N < 60$ e -folds assuming that gravity is described by the Einstein action, and that it gives small quantum corrections. The blue region shows the prediction of negative-field inflation and red shows positive-field inflation around the quadratic potential (the yellow line). Light blue and light red mark the regions where gravity cannot be ignored in the Einstein frame. The light green contours are the $1, 2\sigma$ best fit regions from PLANCK, BICEP2/KECK [47, 51–53].

this implies that m_ψ must be larger than the inflaton mass m_{s_E} . If the model has more than one fermion, some of them can be lighter than s_E .

Taking into account all constraints, we determine the allowed parameter region for the minimal model. In figure 2 we plot the inflaton mass as a function of ξ_S for both negative-field and positive-field inflation (the two regions are partially overlapping) for $50 < N < 60$ [83–85]. The non-minimal coupling cannot be arbitrarily small, because that would mean $v_s \gg \bar{M}_{\text{Pl}}$, implying trans-Planckian masses for σ and ψ . Trans-Planckian

masses are avoided for $\xi_S \gtrsim 10^{-6}$. An upper bound on the non-minimal coupling comes from the requirement that gravity corrections to couplings in the Einstein frame can be neglected (this is true if conditions (A.15) hold, see appendix A). The bound is $\xi_S \lesssim 10(50)$, for positive-field (negative-field) inflation. In the region where gravity corrections cannot be neglected in the Einstein frame, the range of ξ_S can be extended (shown with lighter colours) up to $\xi_S \simeq 1900$ for positive-field and $\xi_S \simeq 6900$ for negative-field inflation.⁵ In this case the upper bound on ξ_S arises from perturbativity of running couplings: $\lambda_\sigma \lesssim 2\pi/3$ and $\lambda_{S\sigma} \lesssim 4\pi$. The range of $\lambda_{S\sigma}(v_s)$ in the right panel of figure 2 is determined by the normalisation of the spectrum $P_R = V_E(s^*)/24\pi^2 \bar{M}_{\text{Pl}}^4 \epsilon(s^*)$. The running of $\lambda_{S\sigma}$ depends on the self-coupling λ_σ . If $\lambda_\sigma(v_s)$ is relatively small, then $\lambda_{S\sigma}(v_s)$ has to be larger at the potential minimum. If $\lambda_\sigma(v_s)$ is large, then $\lambda_{S\sigma}$ runs faster to the required value at s^* and can be smaller in the minimum. Variations of $\lambda_{S\sigma}$ and λ_σ determine the range of the inflaton mass in the left panel of figure 2 as well.

The inflaton potential in figure 1 corresponds to the model parameters $\xi_S(v_s) = 300$, $\lambda_{S\sigma}(v_s) = 0.725$, $\lambda_\sigma(v_s) = \pi/12$, $y_S(v_s) = 0.253$, $y_\sigma(v_s) = 0$ and $m_{s_E} = 1.28 \times 10^{13}$ GeV that are in the physical range, verifying our model independent results in the previous subsection.⁶ The large values of the couplings are needed to get a significant deviation from quadratic inflation.

The slow-roll parameters in this model are given by

$$\epsilon = \left[\frac{\lambda'_S(s)}{\lambda_S(s)} \right]^2 \frac{\xi_S s^2}{2(1 + 6\xi_S)}, \quad \eta = \frac{s\xi_S[\lambda'_S(s) + s\lambda''_S(s)]}{\lambda_S(s)(1 + 6\xi_S)}, \quad (2.27)$$

in terms of which the inflationary parameters are given by

$$n_s = 1 - 6\epsilon(s^*) + 2\eta(s^*), \quad r = 16\epsilon(s^*). \quad (2.28)$$

The predictions of dimensionless single field inflation for r as a function of n_s are presented in figure 3 for $50 < N < 60$ [83–85]. To compare our predictions with experimental results we plot in the same figure also the contours of the 1,2 σ best-fit regions from the official combination of the BICEP2/Keck Array/Planck [47, 51–53].

The yellow line represents the quadratic approximation obtained in the limit $\beta''_{\lambda_S}(v_s) = 0$ (see eq. (2.10)). The blue region shows the allowed parameter space for negative-field inflation and the red region for the positive-field inflation. In the region with darker colours around the yellow line, the conditions (A.15) hold and gravity corrections can be neglected in the Einstein frame. In this region, λ_σ and $\lambda_{S\sigma}$ are small and the inflaton potential is well approximated by (2.10). The predictions for the inflationary parameters n_s and r roughly coincide with the model-independent predictions. In the light red and light blue regions, the conditions (A.15) do not hold, but due to the equivalence of the frames the gravitational corrections in the Einstein frame must arise from scalar loops in the Jordan frame. The

⁵Notice that a large ξ -coupling does not necessarily spoil perturbative unitarity if the VEV of the corresponding scalar field is large [68, 86].

⁶We choose $y_\sigma(v_s) = 0$ for simplicity. If $y_\sigma \neq 0$, the predictions for inflation do not change, since its negative influence on the running of $\lambda_{S\sigma}$ must be countered by a larger value of λ_σ in order to get the correct value for P_R .

potential is not close to the cubic (2.10) any more. We see that for large couplings taking into account exact numerical solutions for RGE running can induce a large correction in r . For the number of e -folds $N = 60$, the lowest possible value of the tensor-to-scalar ratio is $r = 0.04$.

3 Inflation in agravity

In this section we reconsider inflation within agravity [39]: a renormalizable extension of Einstein gravity, obtained by adding all dimensionless couplings which are anyhow generated by quantum corrections, and removing any massive parameter such that power divergences must vanish. The action has the generic structure

$$\mathcal{S} = \int d^4x \sqrt{|\det g|} \left[\mathcal{L}_{\text{matter}} - \sum_i \xi_i \frac{\varphi_i^2}{2} R + \frac{R^2}{6f_0^2} + \frac{\frac{1}{3}R^2 - R_{\mu\nu}^2}{f_2^2} \right]. \quad (3.1)$$

The gravitational kinetic terms suppressed by the dimensionless constants f_0 and f_2 contain four derivatives: thereby the graviton contains a massive spin-2 ghost component [87], which is possibly problematic for energies above its mass $M_2 = |f_2| \bar{M}_{\text{Pl}} / \sqrt{2}$: we do not address the issue of finding a sensible interpretation for it (see [88–95] for some attempts). In this section, as mentioned in the introduction, we do not adopt the effective field theory approach of section 2 and eq. (3.1) is assumed to be the full action, like in ref. [39]. As a curiosity, we notice that the classical gravitational equations of motion, in a theory with neither matter nor cosmological constant, have inflationary solutions with arbitrary Hubble constant.

Of course, matter must be present in a realistic theory: a generic $\mathcal{L}_{\text{matter}}$ can be written in terms of real scalars φ , Weyl fermions ψ and vectors A_μ with gauge, Yukawa and quartic couplings g , y and λ . Furthermore, the scalars φ_i can have dimensionless ξ_i couplings to gravity. Once that scalars dynamically get a vacuum expectation value generating the Planck mass as $\sum_i \xi_i \varphi_i^2 = \bar{M}_{\text{Pl}}^2$, agravity realises the scenario of soft-gravity: the graviton splits into the usual graviton, a massive spin-2 ghost-like graviton and a scalar; their masses M_2 and M_0 represent the energy scale at which gravity softens, becoming described by the dimensionless couplings f_2 and f_0 .

The theory is renormalizable, and quantum corrections enhanced by large logarithms are taken into account, as usual, by substituting the couplings with running couplings (RGE equations have been computed in [39]), renormalised at an energy comparable to the energy or field value of the process under consideration.

3.1 Agravity in the Einstein frame

We want to employ the results in the literature that give the inflationary predictions of multifield Einstein gravity models. Then, we need to recast the agravity action of eq. (3.1) in Einstein form. We here use a compact notation, leaving implicit the sums over the scalars φ_i , which, in a realistic theory, include at least the Planckion s , the physical Higgs h and the other components of the Higgs doublet H .

We start adding to the generic agravity Lagrangian the vanishing term $-(R + 3f_0^2\chi/2)^2/6f_0^2$, where χ is an auxiliary field with no kinetic term. Such new term is designed to cancel $R^2/6f_0^2$, leaving

$$\mathcal{L} = \sqrt{|\det g|} \left[\mathcal{L}_{\text{matter}} + \frac{\frac{1}{3}R^2 - R_{\mu\nu}^2}{f_2^2} - \frac{f}{2}R - \frac{3f_0^2}{8}\chi^2 \right], \quad (3.2)$$

where $f = \chi + \xi\varphi^2$ and⁷

$$\mathcal{L}_{\text{matter}} = \frac{(D_\mu\varphi)^2}{2} - \frac{1}{4}F_{\mu\nu}^2 + \bar{\psi}i\not{D}\psi + (y\varphi\psi\psi + \text{h.c.}) - V(\varphi). \quad (3.3)$$

Here y denotes a set of Yukawa couplings and V is a general quartic potential. Next, we transform the $-fR/2$ term into the canonical Einstein term $-\bar{M}_{\text{Pl}}^2 R_E/2$ by performing a rescaling of the metric,

$$g_{\mu\nu}^E = g_{\mu\nu} \times f/\bar{M}_{\text{Pl}}^2. \quad (3.4)$$

In the limit of constant f (global scale transformation) our dimensionless action is invariant provided that the scalars φ , the fermions ψ and the vectors A_μ are also rescaled as:

$$\varphi_E = \varphi \times (\bar{M}_{\text{Pl}}^2/f)^{1/2}, \quad \psi_E = \psi \times (\bar{M}_{\text{Pl}}^2/f)^{3/4}, \quad A_{\mu E} = A_\mu. \quad (3.5)$$

However, we need to consider a non-constant f and perform a local scale transformation, under which all dimensionless terms without derivatives remain (trivially) invariant. Furthermore, various kinetic terms happen to be also (non-trivially) invariant: this is the case for the fermion kinetic terms [80–82], the vector kinetic terms and the graviton kinetic term proportional to $1/f_2^2$. The scalar kinetic terms are not invariant (away from the special conformal value $\xi = -1/6$); thereby we keep using φ in addition to φ_E for the scalars. Then the Einstein-frame Lagrangian is:

$$\begin{aligned} \mathcal{L} = \sqrt{\det g_E} \left[\frac{\frac{1}{3}R_E^2 - R_{E\mu\nu}^2}{f_2^2} - \frac{1}{4}F_{E\mu\nu}^2 + \bar{\psi}_E i\not{D}\psi_E \right. \\ \left. + (y\varphi_E\psi_E\psi_E + \text{h.c.}) - \frac{\bar{M}_{\text{Pl}}^2}{2}R_E + \mathcal{L}_\varphi - V_E \right], \end{aligned} \quad (3.6)$$

where

$$\mathcal{L}_\varphi = \bar{M}_{\text{Pl}}^2 \left[\frac{(D_\mu\varphi)^2}{2f} + \frac{3(\partial_\mu f)^2}{4f^2} \right], \quad V_E = \frac{\bar{M}_{\text{Pl}}^4}{f^2} \left[V(\varphi) + \frac{3f_0^2}{8}\chi^2 \right]. \quad (3.7)$$

A kinetic term for f has been generated [96], such that f becomes an extra scalar, with no gauge charge.⁸ The kinetic metric in scalar field space has constant *negative* curvature $-N_\varphi(N_\varphi + 1)\bar{M}_{\text{Pl}}^2/6$, where N_φ is the total number of scalars φ , and can be conveniently put in conformal form by redefining $z = \sqrt{6}f$, such that our final Lagrangian is

$$\mathcal{L}_\varphi = \frac{6\bar{M}_{\text{Pl}}^2}{z^2} \frac{(D_\mu\varphi)^2 + (\partial_\mu z)^2}{2} \quad (3.8)$$

⁷If one makes the sum over the scalars φ_i explicit, one should read $\xi\varphi^2$ as $\sum_i \xi_i \varphi_i^2$, the kinetic term $(D_\mu\varphi)^2$ as $\sum_i D_\mu\varphi_i D_\mu\varphi_i$ and so on.

⁸The scalar kinetic term is conformally invariant for $\xi_\varphi = -1/6$; this manifests as cancellations in the scalar kinetic terms.

and

$$V_E(z, \varphi) = \frac{36\bar{M}_{\text{Pl}}^4}{z^4} \left[V(\varphi) + \frac{3f_0^2}{8} \left(\frac{z^2}{6} - \xi_\varphi \varphi^2 \right)^2 \right]. \quad (3.9)$$

We anticipate here a non-trivial peculiarity of the Einstein-frame Lagrangian, best seen by considering the case of a single ‘Planckion’ scalar field s , such that $f = \xi_S s^2$: by using the first equation in (3.5) we obtain that $s_E = \bar{M}_{\text{Pl}}/\sqrt{\xi_S}$ is a constant i.e. its quartic becomes a cosmological constant and its Yukawa couplings become fermion mass terms. How can this be equivalent to the Jordan frame Lagrangian where s has quartic and Yukawa interactions? The point is that s , being the pseudo-Goldstone boson of spontaneously broken approximate scale invariance (the explicit breaking of scale invariance coming from the quantum running of the coupling constants is small because we are assuming perturbative couplings), couples to the divergence of the dilatation current \mathcal{D}_μ , $\partial_\mu \mathcal{D}_\mu$, that vanishes at tree-level because we consider special dimensionless theories.⁹

Mass eigenstates. We compute here the mass eigenstates formed by the scalars $\phi = \{h, s, z\}$ at the minimum of the potential, where the scalars kinetic terms of eq. (3.8) become canonical. Indeed, minimisation with respect to z leads to $z^2 = 6\bar{M}_{\text{Pl}}^2 + 16V/f_0^2\bar{M}_{\text{Pl}}^2$. Minimisation with respect to s gives $\partial V/\partial s - 4\xi_S s V/\bar{M}_{\text{Pl}}^2 = 0$, that should be solved by $\bar{M}_{\text{Pl}}^2 = \sum \xi_i \varphi_i^2 \simeq \xi_S s^2$. The measured value of the cosmological constant implies a negligible value of V at the minimum, simplifying the above equations. Minimisation with respect to h then leads to a negligible vacuum expectation value. On the other hand gauge invariance implies that h should appear at least quadratically in V ; therefore expanding h around its VEV necessarily produces at least one power of this negligible VEV, which implies that the Higgs negligibly mixes with s and z . The mass matrix for the fields s and z around the minimum is given by the second derivatives of V_E :

$$M_s^2 \begin{pmatrix} 1 & 0 \\ 0 & 0 \end{pmatrix} + \frac{f_0^2 \bar{M}_{\text{Pl}}^2}{2} \begin{pmatrix} 6\xi_S & \sqrt{6\xi_S} \\ \sqrt{6\xi_S} & 1 \end{pmatrix}. \quad (3.10)$$

The first term alone would give a Planckion with mass $M_s^2 = \partial^2 V/\partial s^2$. The second term alone would give a spin-0 graviton with mass $M_0^2 = \frac{1}{2}f_0^2 \bar{M}_{\text{Pl}}^2(1 + 6\xi_S)$. Taking into account both terms, the mass eigenvalues are

$$M_\pm^2 = \frac{M_s^2 + M_0^2}{2} \pm \frac{1}{2} \sqrt{(M_s^2 + M_0^2)^2 - 4 \frac{M_s^2 M_0^2}{1 + 6\xi_S}}. \quad (3.11)$$

3.2 Computing multifield inflationary predictions

The classical equations of motion for the Einstein-frame scalar fields $\phi = \{z, s, h\}$ during inflation in slow-roll approximation are

$$\frac{d\phi}{dN} = -\frac{z^2}{6V_E} \frac{\partial V_E}{\partial \phi}, \quad (3.12)$$

⁹The explicit verification that the Jordan frame couplings of s vanish on-shell needs manipulations similar to the ones used to verify the analogous property of the couplings of a Goldstone boson of a U(1) global symmetry, when a Dirac fermion mass term $\bar{\Psi}\Psi$ is re-expressed as derivatives acting within a chiral current $\bar{\Psi}\gamma_\mu\gamma_5\Psi$.

having defined the number of e -folds N as $dN = H dt$. The spin-2 massive graviton does not affect such classical equations of motion, and we assume that it can be neglected even at the quantum level. The quantum predictions for inflation can now be computed by using the previous literature on multifield inflation [97–102]; they can be expressed in terms of the number of e -folds starting from a generic initial point, $N(h, s, z)$:

- The power-spectrum of scalar fluctuations is given by

$$P_R(k) = \left(\frac{H}{2\pi}\right)^2 \frac{z^2}{6\bar{M}_{\text{Pl}}^2} (\nabla N)^2 \quad (3.13)$$

with H computed at horizon exit $k = aH$ and

$$(\nabla F)^2 \equiv \left(\frac{\partial F}{\partial z}\right)^2 + \left(\frac{\partial F}{\partial s}\right)^2 + \left(\frac{\partial F}{\partial h}\right)^2. \quad (3.14)$$

- The spectral index n_s of scalar perturbations is given by

$$\begin{aligned} n_s \equiv 1 + \frac{d \ln P_R}{d \ln k} = \frac{1}{6z^2 V_E^2 (\nabla N)^2} & \left\{ 6V_E^2 \left(z^2 (\nabla N)^2 - 12 \right) - z^4 (\nabla N)^2 (\nabla V_E)^2 \right. \\ & + 2z^3 V_E \left[\left(\frac{\partial N}{\partial h}\right)^2 \left(z \frac{\partial^2 V_E}{\partial h^2} - \frac{\partial V_E}{\partial z} \right) + \left(\frac{\partial N}{\partial z}\right)^2 \left(z \frac{\partial^2 V_E}{\partial z^2} + \frac{\partial V_E}{\partial z} \right) \right. \\ & + 2 \frac{\partial N}{\partial h} \left(\frac{\partial N}{\partial z} \left(z \frac{\partial^2 V_E}{\partial z \partial h} + \frac{\partial V_E}{\partial h} \right) + z \frac{\partial N}{\partial s} \frac{\partial^2 V_E}{\partial s \partial h} \right) + 2 \frac{\partial N}{\partial z} \frac{\partial N}{\partial s} \left(z \frac{\partial^2 V_E}{\partial s \partial z} + \frac{\partial V_E}{\partial s} \right) \\ & \left. \left. + \left(\frac{\partial N}{\partial s}\right)^2 \left(z \frac{\partial^2 V_E}{\partial s^2} - \frac{\partial V_E}{\partial z} \right) \right] \right\}. \end{aligned} \quad (3.15)$$

- The tensor power spectrum is given by $P_t(k) = (2/\bar{M}_{\text{Pl}}^2)(H/2\pi)^2$. Equivalently, the tensor-to-scalar ratio is given by

$$r \equiv \frac{4P_t}{P_R} = \frac{48}{z^2 (\nabla N)^2}. \quad (3.16)$$

The measured values at $k = 0.002 \text{ Mpc}^{-1}$ are $P_R(k) = (2.14 \pm 0.05) \times 10^{-9}$ [52, 53], $n_s = 0.965 \pm 0.006$ [50, 52, 53] and $r = 0.06 \pm 0.04$ (according to [47]) or $r = 0 \pm 0.04$ (according to [52, 53]).

3.3 Inflationary predictions

In general, predictions of multifield inflation depend on the inflationary trajectory reducing the predictive power. However, our potential $V_E(h, s, z)$ has a peculiar structure, such that all classical trajectories converge towards a unique attractor solution even when scalar masses are comparable at the minimum (examples are shown in figure 4). This presumably happens because we are considering dimensionless dynamics, such that the derivatives of the potential are hierarchical almost everywhere in field space. We find that slow-roll inflation starts only when such attractor is reached. In order to understand our results, it is useful to first consider three relevant extreme limits:

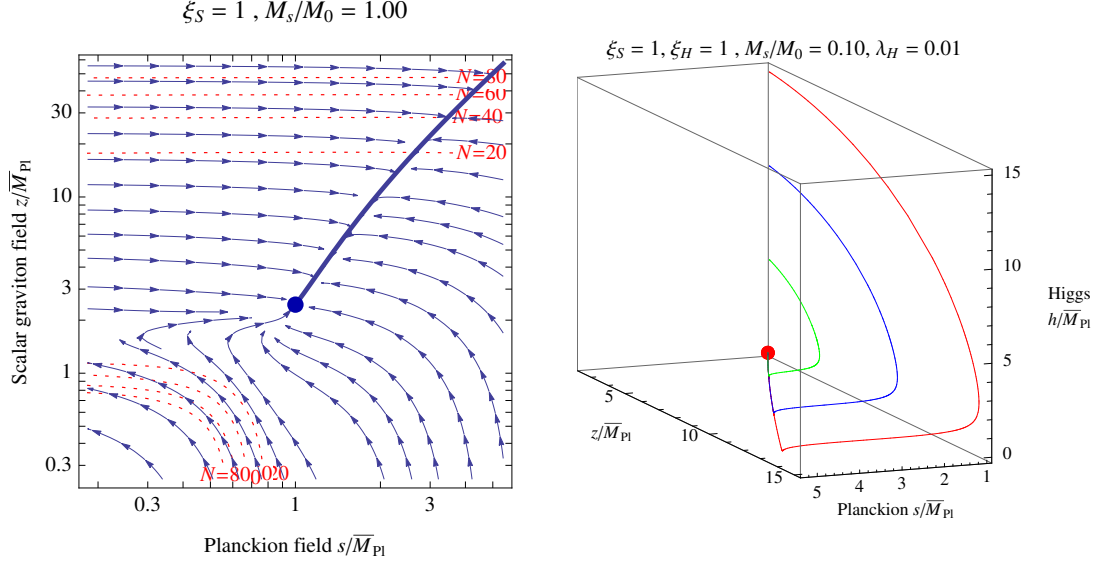


Figure 4. *Left:* sample of classical field evolution in the (s, z) plane with $h = 0$ for $\xi_S = 1$ and $M_s = M_0$. All trajectories starting from different initial values converge towards a unique inflationary attractor (thick curve) that ends at the minimum (thick dot). The red dashed contour-lines show the number N of e -foldings. *Right:* sample of classical field evolution in the (h, s, z) space, showing that an attractor solution with negligible h is reached even starting from $h \gg s, z$.

1. *Planckion inflation.* If $M_0 \gg M_s$ (obtained when the agravity coupling f_0 is larger than the matter couplings in the inflaton sector), the attractor corresponds to $z^2 \approx 6\xi_S s^2$, which is the valley along which the squared term proportional to f_0^2 in V_E , eq. (3.9), nearly vanishes. Then the potential simplifies to $V_E \simeq (\bar{M}_{\text{Pl}}^2/\xi_S s^2)^2 V$, reproducing the situation considered in [39] and in section 2. The inflationary predictions are

$$n_s \approx 1 - \frac{2}{N} \stackrel{N \approx 60}{\approx} 0.967, \quad r \approx \frac{8}{N} \stackrel{N \approx 60}{\approx} 0.13. \quad (3.17)$$

The scalar amplitude $P_R = M_s^2 N^2 / 6\pi^2 \bar{M}_{\text{Pl}}^2$ is reproduced for $M_s \approx 1.4 \times 10^{13}$ GeV.

2. *Scalar graviton inflation.* In the opposite limit, $M_s \gg M_0$ (obtained when the agravity coupling f_0 is smaller than the matter couplings), the attractor solution approximately corresponds to a Planckion s frozen at its VEV. Thereby the Planck constant remains fixed, and the inflaton is z , the scalar component of the graviton. In this limit we obtain Starobinsky inflation [77] that predicts the same n_s as in the previous case and a smaller value of r :

$$n_s \approx 1 - \frac{2}{N} \stackrel{N \approx 60}{\approx} 0.967, \quad r \approx \frac{12}{N^2} \stackrel{N \approx 60}{\approx} 0.003. \quad (3.18)$$

The scalar amplitude $P_R = f_0^2 N^2 / 48\pi^2$ is reproduced for $f_0 \approx 1.8 \times 10^{-5}$.

3. *Higgs inflation.* We find that, for any value of M_0/M_s , inflation is never dominated by the Higgs, because its quartic self-coupling λ_H (assumed to be positive) is unavoidably larger than the other scalar couplings, taking into account its RG running. Even

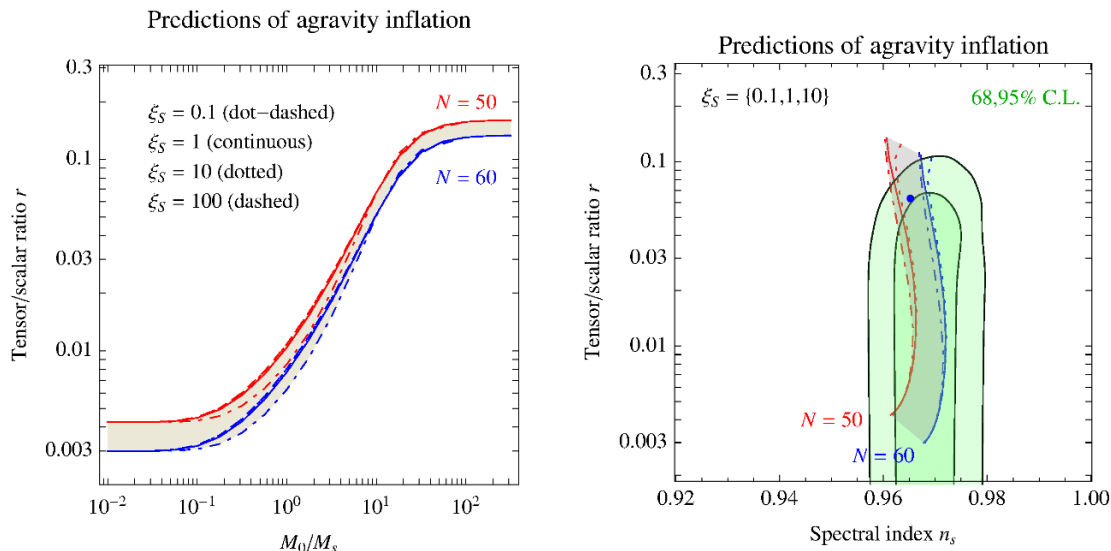


Figure 5. *Left:* predictions for the tensor/scalar ratio r after $N = 50$ or 60 e -folds of inflation for various values of ξ_S as function of M_0/M_s . In the limit where this ratio is large (small), inflation is dominated by the Planckion (the scalar component of the graviton). *Right:* predictions for the scalar spectral index n_s and for the tensor/scalar ratio r with the same coding. The green area is favoured by a global fit of PLANCK, BICEP2/KECK [47, 51–53]

assuming that the Higgs has a dominant initial vacuum expectation value [67], in our multifield context inflation starts only after that the field evolution has reached the attractor solution along which h is subdominant, as exemplified in figure 4b.

Notice that in both limits 1. and 2. the predictions do not depend on ξ_S nor on ξ_H .

We next proceed to numerically compute the inflationary predictions corresponding to the intermediate cases by using the general formulae presented in section 3.2.

Figure 5 (left) shows the prediction for r at $N = 50$ and 60 e -folds while M_s/M_0 is varied from small to large values: we find that r smoothly interpolates between the two limiting cases, $0.003 < r < 0.13$. The intermediate region remains negligibly dependent on the value of ξ_S . Furthermore, the value of $n_s - 1$ approximately scales as $1/N$ and remains close to its common value achieved in the two limiting cases. Figure 5 (right) shows the prediction in the (n_s, r) plane.¹⁰ The prediction is compatible with the region (in green) preferred by data at 68, 95% confidence level according to the latest combination from PLANCK, BICEP2/KECK [47, 51–53]. Next generation experiments could probe r down to $\text{few} \times 10^{-3}$.

4 Cosmology after inflation

We here outline the main possibilities for cosmology after inflation in the present context, and the possible connections with leptogenesis and Dark Matter. In section 4.3 we return to the Higgs mass hierarchy problem.

¹⁰When both fields are relevant, our prediction for (n_s, r) lies in the ‘forbidden region’ according to the claim in [103–105] that assumes single field inflation. Unlike in the previous section, all couplings are here small. Other potentials that lead to similar intermediate values of r are considered in [106–109].

4.1 Reheating

We assumed that the inflaton sector that generates the Planck scale is very weakly coupled to the SM sector, such that the weak scale is naturally much lighter than the Planck scale. Because of this, we need to study with special attention how the SM sector can be reheated by the inflaton decays. The decay of the inflaton I with mass M_I and width Γ_I reheats the universe up to a temperature

$$T_{\text{RH}} = \left[\frac{90}{\pi^2 g_*} \Gamma_I^2 \bar{M}_{\text{Pl}}^2 \right]^{1/4}, \quad (4.1)$$

where $g_* \sim 100$ is the number of relativistic degrees of freedom at T_{RH} . We need to compute the total inflaton decay width Γ_I and its decay channels, in order to check if the SM sector is reheated up to a large enough temperature.

Section 2 identified the inflaton as the Planckion s and section 3 added the scalar graviton as a possible extra candidate, finding that the inflaton I is a combination of the two. We can treat these possibilities jointly given that they have similar couplings, as we now discuss. The Planckion and the scalar component of the graviton respectively couple to

$$\frac{\partial_\mu \mathcal{D}_\mu}{\bar{M}_{\text{Pl}}/\sqrt{\xi_S}} \quad \text{and} \quad \frac{T_{\mu\mu}}{\bar{M}_{\text{Pl}}}, \quad (4.2)$$

where $T_{\mu\mu}$ is the trace of the energy-momentum tensor and $\partial_\mu \mathcal{D}_\mu$ is the divergence of the dilatation current $\mathcal{D}_\mu = T_{\mu\nu} x_\nu + \mathcal{D}'_\mu$. According to the Noether procedure, the first term comes from the transformation of the coordinates $\delta x_\nu \propto x_\nu$; the second term comes from the variations of the fields and produces a difference between $\partial_\mu \mathcal{D}_\mu$ and $T_{\mu\mu}$. The theory is explicitly dimensionless in the Jordan frame such that a non-zero divergence arises only at loop level, and is given by

$$\partial_\mu \mathcal{D}_\mu = \frac{\beta_{g_1}}{2g_1} Y_{\mu\nu}^2 + \frac{\beta_{g_2}}{2g_2} W_{\mu\nu}^2 + \frac{\beta_{g_3}}{2g_3} G_{\mu\nu}^2 + \beta_{y_t} H Q_3 U_3 + \beta_{\lambda_H} |H|^4 + \dots, \quad (4.3)$$

where \dots denotes terms beyond the SM and $\beta_g = dg/d \ln \bar{\mu}$ is the β function of the coupling g . The dominant gluon term gives

$$\Gamma(I \rightarrow gg) \approx \frac{|\xi_S| g_3^4 M_s^3}{(4\pi)^5 \bar{M}_{\text{Pl}}^2}. \quad (4.4)$$

This unavoidable decay channel alone is able of reheating the universe up to

$$T_{\text{RH}} \approx 10^7 \text{ GeV} \left(\frac{M_s}{10^{13} \text{ GeV}} \right)^{3/2} \quad (4.5)$$

for $\xi_S \sim 1$.

The trace of the energy-momentum tensor $T_{\mu\mu}$ receives the same loop contribution. However, it also receives a new, possibly dominant, tree-level contribution. Indeed, $T_{\mu\mu}$ would vanish in a conformal theory; we are instead considering a non-conformal theory where the ξ couplings of scalars are generically different from the conformal value $\xi = -1/6$,

as already discussed around eq. (3.6). Focusing on the Higgs boson h , the resulting tree-level decay is best computed by transforming the $[(\partial_\mu h)^2 - \xi_H h^2 R]/2$ part of the Lagrangian to the Einstein frame and to canonically normalised fields $h_E = h \times \bar{M}_{\text{Pl}}/\sqrt{f}$ and s_E . We find the effective operator¹¹

$$-(1 + 6\xi_H) \sqrt{\frac{\xi_S}{1 + 6\xi_S}} \frac{h_E^2}{2} \frac{\partial^2 s_E}{\bar{M}_{\text{Pl}}} \quad (4.6)$$

that produces a tree-level contribution to the decay width

$$\Gamma(I \rightarrow h_E h_E) = \Gamma(I \rightarrow ZZ) = \frac{1}{2} \Gamma(I \rightarrow WW) \approx \frac{(1 + 6\xi_H)^2 |\xi_S|}{|1 + 6\xi_S|} \frac{M_I^3}{64\pi \bar{M}_{\text{Pl}}^2}. \quad (4.7)$$

The decays to electroweak vectors arise because their longitudinal components are the Goldstone components of the Higgs doublet H . For $\xi_{S,H} \sim 1$ this channel gives a $T_{\text{RH}} \approx 10^9 \text{ GeV}$, two orders of magnitude larger than in eq. (4.5). However, in section 4.3 we will find that naturalness of the Higgs mass favours a ξ_H so close to $-1/6$ that $\Gamma(I \rightarrow h_E h_E)$ becomes subdominant with respect to $\Gamma(I \rightarrow gg)$.

4.2 Dark matter

So far we neglected possible inflaton decays into the inflaton sector. For example the minimal model introduced in section 2.2 contains an extra scalar and an extra fermion. Such decays are not kinematically allowed if the inflaton is the lightest component of its sector. This is the case in the minimal model, and likely holds more in general, given that the Planckion is the light pseudo-Goldstone boson of scale invariance.

However, the inflaton sector must contain fermions in order to provide a negative Yukawa contribution to the β function of the Planckion quartic. Fermions ψ have an associated $\psi \rightarrow -\psi$ symmetry that keeps the lightest fermion stable.

If the lightest fermion within the inflaton sector has no gauge interactions, then it can also couple to the SM sector behaving as a right handed neutrino N . It can generate the observed light neutrino masses via $N LH$ Yukawa couplings [111] (in such a case $M_N \lesssim 10^7 \text{ GeV}$ in order to avoid an unnaturally large quantum correction to the Higgs mass [5–7, 112]) and it can provide baryogenesis via leptogenesis [113, 114].

The lightest fermion in the inflaton sector is instead a stable Dark Matter candidate if it cannot couple to the SM sector (for example because it has gauge interactions under the inflaton sector). Assuming that it is light enough to be produced by inflaton decays, it inherits the observed primordial adiabatic density perturbations.¹²

The decay width of the inflaton into Dark Matter could be computed along the lines of eq. (4.3). A less model-dependent possibility is that such DM fermions get their mass from another source, independent from the Planckion, that also breaks scale invariance but

¹¹A contribution to it was computed in [110].

¹²An alternative production mechanism can operate even if the fermions are so heavy that decays into them are not kinematically allowed; however, this alternative would lead to Dark Matter with isocurvature perturbations [115], which are no longer compatible with observations.

at a lower energy scale. Then such fermion masses would contribute to $\partial_\mu \mathcal{D}_\mu$ and to $T_{\mu\mu}$ as $M\bar{\Psi}\Psi$ (we are considering, for example, a Dirac mass term) giving the contribution¹³

$$\Gamma(I \rightarrow \bar{\Psi}\Psi) \approx \frac{|\xi_S| M^2 M_I}{8\pi(1 + 6\xi_S)\bar{M}_{\text{Pl}}^2}. \quad (4.8)$$

By identifying the fermion Ψ with Dark Matter, its abundance is

$$\Omega_{\text{DM}} \equiv \frac{\rho_{\text{DM}}}{\rho_{\text{cr}}} = \frac{s_0 M}{3H_0^2/8\pi G_N} \frac{\Gamma(I \rightarrow \text{DM})}{\Gamma(I \rightarrow \text{SM})} \approx \frac{0.110}{h^2} \times \frac{M}{0.40 \text{ eV}} \frac{\Gamma(I \rightarrow \text{DM})}{\Gamma(I \rightarrow \text{SM})}, \quad (4.9)$$

having inserted the present entropy density ($s_0 = g_{s0} T_0^3 2\pi^2/45$ with $g_{s0} = 43/11$), the present Hubble constant $H_0 = h \times 100 \text{ km/sec Mpc}$, and the present temperature $T_0 = 2.725 \text{ K}$. The observed DM abundance is reproduced for

$$M \approx (10 - 200) \text{ TeV} \left(\frac{M_I}{10^{13} \text{ GeV}} \right)^{2/3}. \quad (4.10)$$

where the lower (higher) estimate applies if $\Gamma(I \rightarrow gg)$ ($\Gamma(I \rightarrow h_E h_E)$) dominates. The proximity of this mass with the range favoured by the hypothesis that DM is a thermal relic is an accident: this DM candidate leads to negligible non-gravitational signals in agreement with present observations.

Finally, we recall that the Higgs potential might be unstable at energies above 10^{10} GeV (for a precise computation see [116]). The compatibility of this possible instability with cosmology is discussed in [117].

4.3 Inflation and the weak scale

In models that allow for super-Planckian field variations, inflation becomes a generic natural phenomenon [41–43]; however, small parameters are needed to get the observed amplitude of scalar perturbation $P_R \approx 10^{-9}$ rather than $P_R \sim 1$ from chaotic inflation. We obtain a naturally small P_R because we are considering a dimensionless theory with small couplings. Small couplings are also needed in order to keep the Higgs mass M_h naturally much smaller than \bar{M}_{Pl} . These models predict a non-trivial connection of the form

$$M_h \sim P_R \bar{M}_{\text{Pl}} \quad (4.11)$$

between the weak scale, the Planck scale and the amplitude of inflationary perturbations. Eq. (4.11) ignores loop factors $(4\pi)^2$, e -fold factors $N \approx 60$ and the possibility that different couplings have different size. In the rest of the section we add such factors showing that the observed M_h/\bar{M}_{Pl} and P_R are compatible.

As discussed above, inflation wants $f_0 \gtrsim 10^{-5}$. Thereby, we need to compute the maximal value of f_0 naturally allowed by the Higgs mass.

¹³The analogous contribution from SM fermion masses is negligible, and the Higgs mass terms M_h would give a contribution suppressed by two extra powers of M_h/M_I .

Whatever sector dynamically breaks scale invariance, it must provide an effective Einstein term $-\bar{M}_{\text{Pl}}^2 R/2$. Then, inserting such a term in gravitational loop corrections to the Higgs propagator, one estimates a correction to the Higgs mass of order

$$\delta M_h^2 \sim \xi_H \frac{g^2(M_g) M_g^2}{(4\pi)^2}, \quad (4.12)$$

where, as anticipated in section 2, we assume a soft-gravity scenario where new physics at M_g stops the growth of the gravitational coupling $g(E) = E/\bar{M}_{\text{Pl}}$. Here we are neglecting the contributions to δM_h^2 proportional to powers of M_h^2 because they are not dangerous from the point of view of naturalness. The one-loop effect in (4.12) is proportional to ξ_H , the ξ -coupling that provides interactions between the Higgs and gravity, which do not involve the Higgs mass or derivatives on the external Higgs field. If ξ_H vanishes, the correction to M_h^2 arises at two loops.

Within agravity $M_g \sim M_0, M_2$ and the estimate in eq. (4.12) gets replaced by a precise result [39]: the log-enhanced correction to the Higgs mass is described by the following RG equation, valid at energies between \bar{M}_{Pl} and M_g :

$$(4\pi)^2 \frac{d}{d \ln \bar{\mu}} \frac{M_h^2}{\bar{M}_{\text{Pl}}^2} = -\xi_H [5f_2^4 + f_0^4(1 + 6\xi_H)] + \dots, \quad (4.13)$$

where $\bar{\mu}$ is the $\overline{\text{MS}}$ renormalization scale and \dots denotes negligible terms. If $\xi_{S,H} \sim 1$, naturalness implies $f_0 \lesssim 10^{-8}$. This bound can be relaxed by performing a more complete discussion at the light of the RGE for ξ_H [39]:

$$(4\pi)^2 \frac{d\xi_H}{d \ln \bar{\mu}} = (1 + 6\xi_H) \left(y_t^2 - \frac{3}{4}g_2^2 - \frac{3}{20}g_1^2 + 2\lambda_H \right) + \frac{f_0^2}{3}\xi_H(1 + 6\xi_H)(2 + 3\xi_H) - \frac{5}{3}\frac{f_2^4}{f_0^2}\xi_H + \dots, \quad (4.14)$$

where \dots denote beyond-the-SM terms. We see that the ξ couplings can naturally acquire two special values:

- close to zero, $\xi \sim y^2/(4\pi)^2$, where y is a generic coupling of the theory, e.g. $y \sim y_t$ in the SM;
- close to the conformal value, $\xi + 1/6 \sim f_2^4/(4\pi f_0)^2$.

In the latter case, the larger $f_0 \sim 10^{-5}$ called by inflation becomes naturally allowed. We thereby conclude that the smallness of M_h/\bar{M}_{Pl} and the smallness of P_R are mutually compatible, although the ξ terms need to lie in special natural ranges.

5 Conclusions

We computed the inflationary predictions of models where mass scales (in particular the Planck scale) are absent at tree-level and generated only by quantum corrections from dimensionless dynamics. The same sector that generates the Planck mass does also provide

cosmological inflation with super-Planckian field variations: the slow-roll parameters are related to the β -functions of the theory. We consider two scenarios: single field inflation in an effective field theory approach, and inflation in agravity, which is a UV completion of general relativity coupled to the SM fields.

In the first case, in the limit where couplings are small enough that gravity effects can be ignored in the Einstein frame, we showed the consistency between computations in the Jordan and in the Einstein frames, obtaining an inflaton potential which is approximatively quadratic with a cubic correction, leading to

$$n_s \approx 0.967, \quad r \approx 0.13. \quad (5.1)$$

If, instead, ξ_S and other couplings are large one can obtain smaller values of r , down to about 0.04, as shown in figure 3.

In the second case, we considered agravity, the dimensionless extension of Einstein gravity that allows, for small enough couplings, the natural co-existence of the small weak scale with the much larger Planck scale \bar{M}_{Pl} even in absence of new physics at the weak scale. Agravity implies an extra scalar component of the graviton and an extra spin-2 ghost-like graviton that make quantum gravity renormalizable and controlled by two dimensionless couplings f_0, f_2 . A small amplitude of scalar perturbations is also predicted because this sector must contain small couplings such that the weak scale M_h/\bar{M}_{Pl} is naturally small, resulting in a relation that scales as $P_R \sim M_h/\bar{M}_{\text{Pl}}$, more precisely discussed in section 4.3. We computed the inflationary predictions finding the result in figure 5 (right):

$$n_s \approx 0.967, \quad 0.003 < r < 0.13, \quad (5.2)$$

which agrees with present observations. Figure 5 (left) shows that the upper range of r is realised if the ‘Higgs of gravity’ is the lighter scalar that dominates inflation (this limit gives the effective field theory scenario discussed above); the lower range is realised if instead the lighter inflationary field is the scalar component of the graviton.

Both in the effective field theory and in agravity, the inflaton decays via Planck-suppressed interactions (it couples to a combination of the trace of the energy momentum tensor and of the divergence of the dilatation current) producing a reheating temperature $T_{\text{RH}} \sim 10^{7-9}$ GeV.

Furthermore the inflation sector must contain fermions that either behave as right-handed neutrinos (if they have no gauge interactions) or are stable. In the latter case, they might be light enough that the inflaton can decay in them, providing the observed Dark Matter abundance with adiabatic primordial inhomogeneities if their mass is around 10 – 200 TeV.

A determination of the tensor-to-scalar ratio r in the future can help us to discriminate between different paradigms behind inflation and to test quantum theories of gravity such as agravity.

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A RGE and the compatibility of frames

In this appendix we give more details about the compatibility between computations performed in the Jordan and Einstein frame in the effective field theory approach described in section 2. This is particularly relevant since we have to make sure that the RG running in the Jordan frame and in the Einstein frame is consistent.

It has been shown that the results computed in the Jordan and Einstein frames are compatible with each other [120, 121]. However, according to the problem at hand, computations can be easier in one frame or another. Usually it is easier to compute the RGEs in the Jordan frame, while inflationary calculations are more simply performed using standard formulæ valid in the Einstein frame. The RGEs of the Jordan frame can be applied to Einstein frame once we keep in mind that also the renormalisation scale has to rescale under a Weyl transformation [120, 121]. In order to fully recover the equivalence one would need to include gravitational loops, that we neglect.

Let us consider the minimal model described by the Lagrangian (2.17) in the Jordan frame. Assuming the possibility to neglect quantum gravity corrections eq. (2.11), the one-loop level β -functions for the couplings in the Jordan frame are given by

$$16\pi^2\beta_{\lambda_S} = 18\lambda_S^2 + \frac{1}{2}\lambda_{S\sigma}^2 + 4\lambda_S y_S^2 - 4y_S^4, \quad (\text{A.1})$$

$$16\pi^2\beta_{\lambda_\sigma} = 18\lambda_\sigma^2 + \frac{1}{2}\lambda_{S\sigma}^2 + 4\lambda_\sigma y_\sigma^2 - 4y_\sigma^4, \quad (\text{A.2})$$

$$16\pi^2\beta_{\lambda_{S\sigma}} = 4\lambda_{S\sigma}^2 + 6\lambda_{S\sigma}(\lambda_S + \lambda_\sigma) + 4\lambda_{S\sigma}(y_S^2 + y_\sigma^2) - 24y_S^2 y_\sigma^2, \quad (\text{A.3})$$

$$16\pi^2\beta_{y_S} = 4y_S(y_S^2 + y_\sigma^2), \quad (\text{A.4})$$

$$16\pi^2\beta_{y_\sigma} = 4y_\sigma(y_S^2 + y_\sigma^2), \quad (\text{A.5})$$

$$16\pi^2\beta_{\xi_S} = \left(\xi_S + \frac{1}{6}\right) \left(6\lambda_S + \frac{1}{6}y_S^2\right). \quad (\text{A.6})$$

We used the PyR@TE package [118] to derive the RGEs for the scalar and Yukawa couplings and ref. [119] for the non-minimal coupling ξ_S . On the other hand, in the approximation of weakly coupled gravity, the RGEs for the parameters of the Einstein frame Lagrangian (2.18) are

$$16\pi^2\beta_\Lambda = \frac{1}{2}m_\sigma^4 - m_\psi^4, \quad (\text{A.7})$$

$$16\pi^2\beta_{\lambda_\sigma} = 18\lambda_\sigma^2 + 4\lambda_\sigma y_\sigma^2 - 4y_\sigma^4, \quad (\text{A.8})$$

$$16\pi^2\beta_{m_\sigma^2} = (6\lambda_\sigma + 4y_\sigma^2)m_\sigma^2 - 24y_\sigma^2 m_\psi^2, \quad (\text{A.9})$$

$$16\pi^2\beta_{m_\psi} = 4y_\sigma^2 m_\psi, \quad (\text{A.10})$$

$$16\pi^2\beta_{y_\sigma} = 4y_\sigma^3, \quad (\text{A.11})$$

where the connection between the Jordan and Einstein frame parameters is given by

$$\Lambda = \frac{1}{4} \frac{\lambda_S}{\xi_S^2} \bar{M}_{\text{Pl}}^4, \quad (\text{A.12})$$

$$m_\sigma^2 = \frac{1}{2} \frac{\lambda_{S\sigma}}{\xi_S} \bar{M}_{\text{Pl}}^2, \quad (\text{A.13})$$

$$m_\psi = \frac{y_S}{\sqrt{\xi_S}} \bar{M}_{\text{Pl}}. \quad (\text{A.14})$$

We see that the RGEs are not perfectly matching with each other. This is because we neglect gravitational corrections due to the mixing of gravitational and scalar degrees of freedom in the transformation between the frames. To match the RGEs of the Jordan frame and the RGEs of Einstein frame in the weak gravity limit, we need to impose

$$\lambda_S \ll \lambda_{S\sigma} \ll \lambda_\sigma, \quad \beta_{y_S} \ll y_S, \quad \beta_{\xi_S} \ll \xi_S, \quad (\text{A.15})$$

on the Jordan frame parameters. However, since physical observables are frame independent [120, 121], the quantum gravity corrections in the Einstein frame must be reproduced by scalar loops in the Jordan frame.

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