# ON THE RR LYRAE STARS IN GLOBULARS. IV. $\omega$ CENTAURI OPTICAL UBVRI PHOTOMETRY* 

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#### Abstract

New accurate and homogeneous optical UBVRI photometry has been obtained for variable stars in the Galactic globular cluster $\omega$ Cen (NGC 5139). We secured 8202 CCD images covering a time interval of 24 years and a sky area of $84 \times 48$ arcmin. The current data were complemented with data available in the literature and provided new, homogeneous pulsation parameters (mean magnitudes, luminosity amplitudes, periods) for 187 candidate $\omega$ Cen RR Lyrae (RRLs). Among them we have 101 RRc (first overtone) and 85 RRab (fundamental) variables, and a single candidate RRd (double-mode) variable. Candidate Blazhko RRLs show periods and colors that are intermediate between the RRc and RRab variables, suggesting that they are transitional objects. A comparison of the period distribution and the Bailey diagram indicates that RRLs in $\omega$ Cen show a long-period tail not present in typical Oosterhoff II (OoII) globulars. The RRLs in dwarf spheroidals and in ultra-faint dwarfs have properties between Oosterhoff intermediate and OoII clusters. Metallicity plays a key role in shaping the above evidence. These findings do not support the hypothesis that $\omega$ Cen is the core remnant of a spoiled dwarf galaxy. Using optical period-Wesenheit relations that are reddening-free and minimally dependent on metallicity we find a mean distance to $\omega$ Cen of $13.71 \pm 0.08 \pm 0.01 \mathrm{mag}$ (semi-empirical and theoretical calibrations). Finally, we invert the $I$-band period-luminosity-metallicity relation to estimate individual RRLs' metal abundances. The metallicity distribution agrees quite well with spectroscopic and photometric metallicity estimates available in the literature.


Key words: globular clusters: individual (omega Cen) - stars: distances - stars: horizontal-branch - stars: variables: RR Lyrae

## 1. INTRODUCTION

The Galactic stellar system $\omega$ Cen lies at the crossroads of several open astrophysical problems. It is the most massive Milky Way globular cluster (GC) $\left(4.05 \times 10^{6} M_{\odot}[d /\right.$ $(5.5 \pm 0.2 \mathrm{kpc})]^{3}$ where $d$ is the distance, D'Souza \&

[^0]Rix 2013) and was the first to show a clear and well defined spread in metal abundance (Norris \& Da Costa 1995; Johnson \& Pilachowski 2010) in $\alpha$ and in $s$ - and $r$-process elements (Johnson et al. 2009). On the basis of the above peculiarities it has also been suggested that $\omega$ Cen and a few other massive Galactic globular clusters (GGCs) might have been the cores of pristine dwarf galaxies (Da Costa \& Coleman 2008; Marconi et al. 2014).

The distance to $\omega$ Cen has been estimated using primary and geometrical distance indicators. The tip of the red giant branch (TRGB) was adopted by Bellazzini et al. (2004) and Bono et al. (2008b) with distances ranging from 13.65 to 13.70 mag . The $K$-band period-luminosity (PL) relations of RR Lyrae stars (RRLs) have been adopted by Longmore et al. (1990), Sollima
et al. (2006b), and Bono et al. (2008b). The distance moduli they estimated range from 13.61 to 13.75 mag . On the other hand, $\omega$ Cen distance moduli based on the relations between luminosity and iron abundance for RRLs range from 13.62 to 13.72 mag (Del Principe et al. 2006). The difference in distance between the different methods is mainly due to the intrinsic spread in the adopted diagnostics and in the reddening correction.

Optical PL relations for SX Phoenicis stars were adopted by McNamara (2011) who found a distance of $13.62 \pm 0.05 \mathrm{mag}$. One eclipsing variable has been studied by Kaluzny et al. (2007), and they found a distance modulus of $13.49 \pm 0.14 \mathrm{mag}$ and $13.51 \pm 0.12 \mathrm{mag}$ for the two components. The key advantage in dealing with eclipsing binaries is that they provide very accurate geometrical distances (Pietrzyński et al. 2013). Estimates based on cluster proper motions provide distance estimates that are systematically smaller than obtained from the other most popular distance indicators ( 13.27 mag , van Leeuwen et al. 2000; $13.31 \pm 0.04 \mathrm{mag}$, Watkins et al. 2013). The reasons for this difference are not yet clear.

The modest distance and the large mass of $\omega$ Cen make this stellar system a fundamental laboratory to constrain evolutionary and pulsation properties of old ( $t>10 \mathrm{Gyr}$ ) low-mass stars. The key advantage in dealing with stellar populations in this system is that they cover a broad range in metallicity $(-2.0 \lesssim[\mathrm{Fe} / \mathrm{H}] \lesssim-0.5$, Pancino et al. $2002 ;-2.5 \lesssim[\mathrm{Fe} /$ $\mathrm{H}] \lesssim+0.5$, Calamida et al. 2009; $-2.2 \lesssim[\mathrm{Fe} / \mathrm{H}] \lesssim-0.6$, Johnson \& Pilachowski 2010) and they are located at the same distance (Castellani et al. 2007). Moreover, the high total stellar mass provides an opportunity to trace fast evolutionary phases (Monelli et al. 2005; Calamida et al. 2008) together with exotic (Randall et al. 2011) and/or compact objects (Bono et al. 2003b).

For the same reasons mentioned above, $\omega$ Cen was a crucial crossroads for RRLs. The first detailed investigation of RRLs was provided more than a century ago in a seminal investigation by Bailey (1902). Using a large set of photographic plates he identified and characterized by eye 128 RRLs, providing periods, amplitudes and a detailed investigation of the shapes of the light curves. In particular, he suggested the presence of three different kinds of pulsating variables ( $\mathrm{RRa}, \mathrm{RRb}, \mathrm{RRc}$ ) in which the luminosity variation amplitude steadily decreases and the shape of the light curve changes from sawtooth to sinusoidal. This investigation was supplemented more than thirty years later by Martin (1938) on the basis of more than 400 photographic plates collected by H . van Gent on a time interval of almost four years and measured with a microdensitomer. He provided homogeneous photometry and very accurate periods for 136 RRL variables.

We needed to wait another half century to have a detailed and almost complete census of RRLs in $\omega$ Cen based on CCD photometry, by the OGLE project (Kaluzny et al. 1997, 2004). They collected a large number of CCD images in $V$ and $B$ covering a time interval of three years (Kaluzny et al. 1997) and one and half years (Kaluzny et al. 2004) and provided a detailed analysis of the occurrence of the Blazhko effect (a modulation of the light amplitude on timescales from tens of days to years; Blažko 1907). A similar analysis was performed by Weldrake et al. (2007) using the observing facility and photometric system of the MACHO project. They collected 875 optical images covering a period of 25 days.

A detailed near-infrared (NIR) analysis was performed by Del Principe et al. (2006) using time series data collected with SOFI at NTT. They provided homogeneous $J K_{s}$ photometry for 180 variables and provided a new estimate of the $\omega$ Cen distance modulus using the $K$-band PL relation ( $13.77 \pm 0.07 \mathrm{mag}$ ). A similar analysis was recently performed by Navarrete et al. (2015) based on a large set of images collected with the VISTA telescope. They provided homogeneous $J K_{s}$ photometry for 189 probable member RRLs (101 RRc, 88 RRab ) and discussed the pulsation properties of the entire sample in the NIR. In particular, they provided new NIR reference lines for Oosterhoff I (OoI) and Oosterhoff II (OoII) clusters. Moreover, they further supported the evidence that RRab in $\omega$ Cen display properties similar to OoII systems. These investigations have been complemented with a detailed optical investigation covering a sky area of more than 50 square degrees by Fernández-Trincado et al. (2015b). They detected 48 RRLs and the bulk of them (38) are located outside the tidal radius. However, detailed simulations of the different Galactic components and radial velocities for a sub-sample of RRLs indicate a lack of tidal debris around the cluster.

This is the fourth paper of a series focused on homogeneous optical, NIR, and mid-infrared (MIR) photometry of cluster RRLs. The structure of the paper is as follows. In Section 2 we present the optical multi-band $U B V R I$ photometry that we collected for this experiment together with the approach adopted to perform the photometry on individual images and on the entire data set. In Section 3.1 we discuss in detail the identification of RRLs and the photometry we collected from the literature to provide homogeneous estimates of the RRL pulsation parameters. Section 3.2 deals with the period distribution, while Section 3.3 discusses the light curves and the approach we adopted to estimate the mean magnitudes and the luminosity variation amplitudes. The Bailey diagram (luminosity variation amplitude versus period) is discussed in Section 3.4, while the amplitude ratios are considered in Section 3.5. Section 4 is focused on the distribution of RRLs in the color-magnitude diagram (CMD) and on the topology of the instability strip. In Section 5 we perform a detailed comparison of the period distribution and the Bailey diagram of $\omega$ Cen RRLs with the similar distributions in nearby gas-poor systems (globulars, dwarf galaxies). Section 6 deals with RRL diagnostics, namely the PL and the period-Wesenheit (PW) relation, while in Section 7 we discuss the new distance determinations to $\omega$ Cen based on optical PW relations. Section 8 deals with the metallicity distribution of the RRLs, based on the $I$-band PL relation, and the comparison with photometric and spectroscopic estimates available in the literature. Finally, Section 9 gives a summary of the current results together with a few remarks concerning the future of this project.

## 2. OPTICAL PHOTOMETRY

We provide new, accurate, and homogeneous calibrated multi-band UBVRI photometry for the candidate RRLs in $\omega$ Cen. The sky area covered by our calibrated photometry is roughly $57^{\prime} \times 56^{\prime}$ around the cluster center (see the end of this section). We acquired 8202 optical CCD images of $\omega$ Cen from proprietary data sets ( 6211 images, $76 \%$ ) and public archives and extracted astrometric and photometric measurements from them using well established techniques (see, e.g., Stetson 2000, 2005 and references therein). Among these we were able to

Table 1
Log of the Observations of $\omega$ Cen in Optical Bands

| Run | ID | $\mathrm{P} / \mathrm{A}^{\mathrm{a}}$ | Dates | Telescope | Camera | $U$ | $B$ | V | $R$ | I | Other | Multiplex |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | bond24 | A | 1988 Feb 22-Mar 02 | CTIO 0.9 m | RCA5 | $\ldots$ | 3 | 3 | 3 | 3 | $\ldots$ |  |
| 2 | bond 23 | A | 1989 Jan 16-25 | CTIO 0.9 m | RCA5 | $\ldots$ | 1 | 1 | 1 | 1 | ... |  |
| 3 | f32 | P | 1991 Jan 22 | CTIO 1.5 m | Tek 512 | $\ldots$ | 3 | 3 |  |  | $\ldots$ |  |
| 4 | emmi6 | A | 1993 Feb 17-21 | ESO NTT 3.6 m | EMMI susi3? | $\ldots$ | $\ldots$ | 47 | $\ldots$ | 47 | $\ldots$ |  |
| 5 | emmi 7 | A | 1993 Feb 18-21 | ESO NTT 3.6 m | EMMI susi3? | $\ldots$ | $\ldots$ | 2 | $\ldots$ | 2 | $\ldots$ |  |
| 6 | emmi5 | A | 1993 Jul 15-23 | ESO NTT 3.6 m | EMMI | $\ldots$ | $\ldots$ | 2 | $\ldots$ | 2 | $\ldots$ |  |
| 7 | susi1 | A | 1994 Dec 26-29 | ESO NTT 3.6 m | SUSI | $\ldots$ | 2 | 3 | $\ldots$ | 4 | ... |  |
| 8 | emmi2 | A | 1995 Mar 07-10 | ESO NTT 3.6 m | EMMI | $\ldots$ | $\ldots$ | 7 | $\ldots$ | 7 | $\ldots$ |  |
| 9 | danish95 | P | 1995 May 21-Jun 01 | ESO/Danish 1.5 m | Thompson CCD\#17 | $\ldots$ | 753 | 530 | $\ldots$ | 503 | ... |  |
| 10 | ct95jun | P | 1995 Jun 20-25 | CTIO 0.9 m | tek2 | $\ldots$ | 5 | 5 | $\ldots$ | 5 | $\ldots$ |  |
| 11 | omega | A | 1996 Apr 10 | CTIO 0.9 m | Tek2K_3 | $\ldots$ | 7 | 7 | $\ldots$ | $\ldots$ | $\ldots$ |  |
| 12 | danish96 | P | 1996 Mar 22-29 | $\begin{aligned} & \text { ESO/Dan- } \\ & \text { ish } 1.5 \mathrm{~m} \end{aligned}$ | LORAL2kx 2 k | $\ldots$ | 10 | 126 | $\ldots$ | 4 | $\ldots$ |  |
| 13 | apr97 | A | 1997 Apr 12-16 | ESO 0.9 m | ccd\$33 | $\ldots$ | $\cdots$ | 6 | $\ldots$ | 6 | $\ldots$ |  |
| 14 | bond5 | A | 1997 Jun 01-02 | CTIO 0.9 m | Tek2K_3 | 10 | 10 | 10 | $\ldots$ | 10 | $\ldots$ |  |
| 15 | danish98 | P | 1998 Mar 29-Jun 21 | ESO/Danish 1.5 m | LORAL2kx 2 k | $\ldots$ | 75 | 1833 | $\ldots$ | 73 | $\ldots$ |  |
| 16 | bond6 | A | 1998 Apr 16-22 | CTIO 0.9 m | Tek2K_3 | 10 | 10 | 12 | $\ldots$ | 12 | $\ldots$ |  |
| 17 | danish99 | P | 1999 Apr 01-08 | ESO/Danish 1.5 m | LORAL2kx 2 k | ... | ... | 354 | 275 | 3 | $\ldots$ |  |
| 18 | elena | A | 1999 May 01/Jul 10-11 | MPI/ESO 2.2 m | WFI | $\cdots$ | $\cdots$ | 8 | $\ldots$ | 8 | 24 |  |
| 19 | bond4 | A | 1999 Jun 11-16 | CTIO 0.9 m | Tek2K_3 | 1 | 1 | 1 | $\ldots$ | 1 | $\ldots$ |  |
| 20 | wfi12 | A | 1999 Jul 06-12 | MPI/ESO 2.2 m | WFI | 2 | 4 | 6 | $\ldots$ | 4 | 4 | $\times 8$ |
| 21 | wfi22 | A | 2000 Feb 25-Mar 01 | MPI/ESO 2.2 m | WFI | $\ldots$ | 4 | 6 | $\ldots$ | 3 | ... | $\times 8$ |
| 22 | bond7 | A | 2001 Mar 25-28 | CTIO 0.9 m | Tek2K_3 | 1 | 1 | 1 | $\ldots$ | 1 | ... |  |
| 23 | danish | P | 2001 Apr 14-Jul 01 | $\begin{aligned} & \text { ESO/Dan- } \\ & \text { ish } 1.5 \mathrm{~m} \end{aligned}$ | EEV 2kx 4 k | $\ldots$ | 26 | 37 | 23 | $\ldots$ | 560 |  |
| 24 | f31 | A | 2002 Mar 17 | CTIO 0.9 m | Tek2K_3 | $\ldots$ | $\ldots$ | 12 | $\ldots$ | $\cdots$ | $\ldots$ |  |
| 25 | fors0204 | A | 2002 Apr 06-13 | ESO VLT 8.0 m | FORS2 MIT/LL mosaic | $\ldots$ | 28 | 24 | $\ldots$ | 6 | $\ldots$ | $\times 2$ |
| 26 | wfi5 | A | 2002 Jun 17-21 | MPI/ESO 2.2 m | WFI | 11 | 13 | 15 | $\ldots$ | 12 | $\ldots$ | $\times 8$ |
| 27 | wfi8 | A | 2003 Apr 08-14 | MPI/ESO 2.2 m | WFI | $\ldots$ | 14 | 14 | $\ldots$ | $\ldots$ | $\ldots$ | $\times 8$ |
| 28 | vimos | A | $\begin{aligned} & 2003 \text { Jul 27-2006 } \\ & \text { Mar } 04 \end{aligned}$ | VLT 8 m | VIMOS | 13 | 8 | $\ldots$ | $\ldots$ | $\ldots$ | $\cdots$ | $\times 4$ |
| 29 | fors3 | A | 2005 Feb 15-17 | ESO VLT 8.0 m | FORS2 | $\ldots$ | $\ldots$ | 8 | $\cdots$ | $\ldots$ | $\ldots$ | $\times 2$ |
| 30 | saao | P | 2006 Mar 22-26 | SAAO 1.0 m | STE4 CCD | 56 | 56 | 68 | 1 | 70 | $\cdots$ |  |
| 31 | aug08 | P | 2008 Aug 26-28 | CTIO 4.0 m | Mosaic2 | 1 | 1 | 1 | $\ldots$ | 1 | 1 | $\times 8$ |
| 32 | efosc0904 | P | 2009 Apr 16-17 | ESO NTT 3.6 m | EFOSC/1.57 LORAL | $\ldots$ | 714 | $\ldots$ | $\cdots$ | $\ldots$ | ... |  |
| 33 | efosc09 | A | 2009 Apr 19-29 | ESO NTT 3.6 m | EFOSC/1.57 LORAL | 36 | 423 | 40 | 29 | $\ldots$ | $\ldots$ |  |
| 34 | wfi41 | A | 2012 Feb 22-29 | MPI/ESO 2.2 m | WFI | 5 | $\ldots$ | $\ldots$ | $\ldots$ | $\cdots$ | $\ldots$ | $\times 8$ |

Note. 1. Observer: H. E. Bond 2. Observer: H. E. Bond 3. Observer: A. R. Walker 4. Observer: G. P. Piotto 5. Observer: G. P. Piotto 6. Observer: "Sav/Zaggia" 7. Observer: Testa; ESO program identification 054.E-0404 8. Observer: Zaggia; ESO program identification 054.E-0337 9. Observer: L. M. Freyhammer 10. Observer: A. R. Walker 11. Observer: Soo-Chang Rey 12. Observer: L. M. Freyhammer 13. Observer: A. Rosenberg 14. Observer: H. E. Bond 15. Observer: L. M. Freyhammer 16. Observer: H. E. Bond 17. Observer: L. M. Freyhammer 18. Observer: E. Pancino; "other" $=\mathrm{H} \alpha$ 19. Observer: H. E. Bond 20. Observer: unknown; ESO program identification unknown; "other" $=856 / 14$ 21. Observer: M. Schirmer ; ESO program identification 164.O-0561(E) 22. Observer: H. E. Bond 23. Observer: L. M. Freyhammer; "other" = no filter 24. Observer: Pablo Candia 25. ESO program identification 60.A-9203(D) 26. ESO program identification 69.D-0582(A) 27. ESO program identification 69.D-0582(A) 28. ESO program identification 071.A-9004(A) 29. ESO program identification 074.D-0187(B) 30. Observer: L. M. Freyhammer 31. Observer: A. R. Walker; proposal identification 155; "other" = DDO51 32. ESO program identification 083.D-0833(A) 33. ESO program identification 083.D-0544(A) 34. ESO program identification 088.A-9012(A).
${ }^{\mathrm{a}} \mathrm{P}$ —proprietary data; A—archive data.
photometrically calibrate 7766 images (including $320 U-, 2632$ $B$-, 3588 V -, 339 R -, and 887 I -band images) covering a time interval of slightly over 24 years. Table 1 gives the $\log$ of observations and a detailed description of the different optical data sets adopted in this investigation. Note that the largest data sets are danish95 (1786 CCD images) ${ }^{21}$ and danish98 (1981 CCD images). The danish99 data set also includes a sizable

[^1]number of exposures ( 632 CCD images), but they were collected on two nights separated by seven days. For this reason, the danish99 data set is very useful to have an estimate of the shape of the light curve, but the period determinations based on this data set in isolation are not as accurate as those based on data sets covering a larger time interval. The $B$-band photometry based on danish 95 and on danish 98 images is less accurate when compared with the other data sets. The danish 98 data set showed large variations of the photometric zero-point with position on the chip. The large number of local standards

Table 2
Positions and Periods for $\omega$ Cen RRLs

| ID | $\begin{gathered} \alpha(\mathrm{J} 2000.0)^{\mathrm{a}} \\ \mathrm{~h} \mathrm{~m} \mathrm{~s} \end{gathered}$ | $\delta\left(\underset{0,1 / 1}{(\mathrm{~J} 2000.0)^{\mathrm{a}}}\right.$ | Period ${ }^{\text {b }}$ |  | $T_{0}(\mathrm{max})^{\text {c }}$ |  | $T_{0}\left(\right.$ rising ${ }^{\text {c }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Literature ${ }^{\text {d }}$ | LS | band | JD | band | JD |
| V3 | 132556.16 | -47 2554.2 | 0.8413 | 0.841262 | ... | ... | ... | $\ldots$ |
| V4 | 132612.94 | -47 2419.2 | 0.6273 | 0.627318 | $\ldots$ | ... | V | 49156.5732 |
| V5 | 132618.34 | -47 2312.8 | 0.5153 | 0.515280 | V | 50975.5712 | V | 49865.6237 |
| V7 | 132701.04 | -47 1400.1 | 0.7130 | 0.713034 | V | 49142.5355 | V | 49082.5766 |
| V8 | 132748.43 | -472820.6 | 0.5213 | 0.521326 | V | 51285.8083 | V | 49824.5018 |
| V9 | 132559.59 | -47 2624.4 | 0.5235 | 0.523464 | ... | ... | ... | ... |
| V10 | 132607.01 | -4724 37.0 | 0.3750 | 0.374882 | I | 49863.6418 | I | 52446.5061 |
| V11 | 132630.56 | -4723 01.9 | 0.5648 | 0.564806 | $\ldots$ | ... | ... | ... |
| V12 | 132627.19 | -4724 06.6 | 0.3868 | 0.386767 | V | 50983.6588 | V | 51276.7254 |
| V13 | 132558.19 | -4725 22.0 | 0.6690 | 0.669048 | ... | ... | V | 51316.5671 |
| V14 | 132559.67 | -47 3909.8 | 0.3771 | 0.377126 | $\ldots$ | $\ldots$ | ... | ... |
| V15 | 132627.10 | -47 2438.4 | 0.8106 | 0.810654 | $\ldots$ | $\ldots$ | $\ldots$ | ... |
| V16 | 132737.71 | -473735.0 | 0.3302 | 0.330196 | B | 51284.7529 | B | 51285.6659 |
| V18 | 132745.07 | -472456.9 | 0.6217 | 0.621686 | V | 51675.5857 | V | 51340.4589 |
| V19 | 132730.13 | -4728 05.7 | 0.2996 | 0.299552 | V | 51305.7769 | V | 49869.6627 |
| V20 | 132714.05 | -4728 06.8 | 0.6156 | 0.615564 | V | 50971.6926 | V | 50971.6481 |
| V21 | 132611.18 | -47 2559.3 | 0.3808 | 0.380809 | V | 51276.7515 | V | 50978.4818 |
| V22 | 132741.05 | -4734 07.9 | 0.3961 | 0.396084 | ... | ... | V | 51348.5895 |
| V23 | 132646.50 | -4724 39.6 | 0.5109 | 0.510870 | V | 50971.6918 | V | 49866.6429 |
| V24 | 132738.33 | -47 3414.8 | 0.4623 | 0.462222 | $\ldots$ | ... | ... | ... |
| V25 | 132625.52 | -4728 23.7 | 0.5884 | 0.588354 | I | 49861.6692 | I | 50921.8161 |
| V26 | 132623.63 | -4726 59.8 | 0.7847 | 0.784721 | V | 50975.6099 | V | 50978.6516 |
| V27 | 132626.04 | -4728 17.0 | 0.6157 | 0.615693 | V | 50978.6798 | V | 51276.5985 |
| V30 | 132615.94 | -47 2956.5 | 0.4044 | 0.404235 | V | 50971.6349 | V | 50975.5632 |
| V32 | 132703.36 | -472139.2 | 0.6204 | 0.620368 | V | 49866.7524 | V | 49863.6101 |
| V33 | 132551.59 | -47 2906.1 | 0.6023 | 0.602333 | V | 51313.5125 | V | 51285.7634 |
| V34 | 132607.20 | -47 3310.8 | 0.7340 | 0.733955 | V | 50984.4808 | V | 52443.5106 |
| V35 | 132653.26 | -47 2234.9 | 0.3868 | 0.386833 | V | 51276.6871 | V | 51276.5919 |
| V36 | 132710.21 | -47 1529.5 | 0.3798 | 0.379813 | V | 49113.5269 | V | 49114.5660 |
| V38 | 132703.24 | -4736 30.3 | 0.7791 | 0.779059 | V | 49862.8101 | V | 49869.7186 |
| V39 | 132759.82 | -4734 42.2 | 0.3934 | 0.393386 | ... | ... | ... | $\ldots$ |
| V40 | 132624.57 | -473046.7 | 0.6341 | 0.634098 | V | 50983.5875 | V | 49863.7202 |
| V41 | 132701.39 | -473102.0 | 0.6629 | 0.662934 | V | 50984.6043 | V | 50984.5522 |
| V44 | 132622.40 | -4734 35.7 | 0.5675 | 0.567536 | V | 50983.5733 | V | 50971.6089 |
| V45 | 132530.87 | -472720.8 | 0.5891 | 0.589135 | ... | ... | ... | . |
| V46 | 132530.25 | -4725 51.6 | 0.6870 | 0.686962 | V | 49819.6153 | V | 49821.6201 |
| V47 | 132556.49 | -472412.3 | 0.4853 | 0.485295 | ... | $\ldots$ | ... | $\ldots$ |
| V49 | 132607.74 | -47 3755.8 | 0.6046 | 0.604645 | V | 51675.4824 | V | 51335.6172 |
| V50 | 132553.94 | -47 2736.1 | 0.3862 | 0.386166 | ... | $\ldots$ |  | ... |
| V51 | 132642.60 | -472421.6 | 0.5742 | 0.574142 | V | 50984.6569 | V | 51276.8553 |
| V52 | 132635.17 | -4728 04.3 | 0.6604 | 0.660387 | $\ldots$ | ... | $\ldots$ | ... |
| V54 | 132623.52 | -471848.1 | 0.7729 | 0.772909 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V55 | 132545.10 | -47 4220.0 | 0.5817 | 0.581921 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V56 | 132555.46 | -47 3744.3 | 0.5680 | 0.568036 | ... | $\ldots$ | ... | $\ldots$ |
| V57 | 132749.43 | -473650.5 | 0.7944 | 0.794422 | $\ldots$ | ... | V | 51317.5478 |
| V58 | 132613.06 | -4724 03.4 | 0.3699 | 0.369922 | $\cdots$ | ... | V | 50971.6570 |
| V59 | 132618.43 | -47 2947.2 | 0.5185 | 0.518551 | V | 50977.4650 | V | 51276.6197 |
| V62 | 132626.59 | -47 2755.8 | 0.6198 | 0.619796 | V | 50984.5398 | V | 50984.4926 |
| V63 | 132507.89 | -473653.7 | 0.8259 | 0.825960 | ... | ... | ... | $\ldots$ |
| V64 | 132602.18 | -473619.5 | 0.3445 | 0.344474 | $\ldots$ | $\ldots$ | I | 49863.7704 |
| V66 | 132633.04 | -4722 25.6 | 0.4073 | 0.407273 | ... | ... | $\ldots$ | ... |
| V67 | 132628.58 | -47 1847.2 | 0.5645 | 0.564449 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V68 | 132612.82 | -47 1936.1 | 0.5346 | 0.534762 | ... | $\ldots$ | $\ldots$ | ... |
| V69 | 132510.95 | -473733.2 | 0.6532 | 0.653221 | ... | ... | $\ldots$ | $\cdots$ |
| V70 | 132727.76 | -4733 43.1 | 0.3907 | 0.390591 | $\cdots$ | $\ldots$ | I | 49862.8163 |
| V71 | 132708.07 | -47 2752.1 | 0.3575 | 0.357649 | V | 50971.5774 | V | 49865.6334 |
| V72 | 132733.04 | -47 1622.6 | 0.3845 | 0.384504 | $\ldots$ | ... | ... | ... |
| V73 | 132553.67 | -47 1610.6 | 0.5752 | 0.575204 | $\cdots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V74 | 132707.27 | -47 1734.3 | 0.5032 | 0.503214 | V | 51677.5088 | V | 55711.7447 |
| V75 | 132719.71 | -471846.9 | 0.4222 | 0.422142 | ... | ... | ... | ... |
| V76 | 132657.29 | -47 2007.9 | 0.3380 | 0.337960 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V77 | 132720.88 | -472206.0 | 0.4263 | 0.426041 | $\ldots$ | .. | V | 50977.4771 |
| V79 | 132825.06 | -4729 24.8 | 0.6083 | 0.608287 | V | 49832.5177 | V | 49922.5029 |

Table 2
(Continued)

| ID | $\begin{gathered} \alpha(\mathrm{J} 2000.0)^{\mathrm{a}} \\ \mathrm{~h} \mathrm{~m} \mathrm{~s} \end{gathered}$ | $\delta\left(\underset{0,1 / 1}{(\mathrm{~J} 2000.0)^{\mathrm{a}}}\right.$ | Period ${ }^{\text {b }}$ |  | $T_{0}(\max )^{\text {c }}$ |  | $T_{0}\left(\right.$ rising ${ }^{\text {c }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Literature $^{\text {d }}$ | LS | band | JD | band | JD |
| V80 ${ }^{\text {e }}$ | 132855.06 | -47 3016.4 | 0.37718 | 0.377218 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V81 | 132736.65 | -47 2448.8 | 0.3894 | 0.389385 | ... | $\ldots$ | $\ldots$ | $\ldots$ |
| V82 | 132735.59 | -47 2630.8 | 0.3358 | 0.335765 | $\ldots$ | $\ldots$ | $\ldots$ |  |
| V83 | 132708.44 | -472134.4 | 0.3566 | 0.356610 | $\ldots$ | $\ldots$ | I | 49861.6428 |
| V84 | 132447.45 | -47 2956.5 | 0.5799 | 0.579918 | V | 49822.6629 | V | 49833.6112 |
| V85 | 132506.61 | -47 2333.5 | 0.7427 | 0.742749 | $\ldots$ | $\ldots$ | . | $\ldots$ |
| V86 | 132715.18 | -47 2611.6 | 0.6478 | 0.647841 | V | 50978.6454 | V | 50978.5945 |
| V87 | 132657.48 | -4725 35.6 | 0.3965 | 0.395941 | R | 51269.9734 | $\ldots$ | ... |
| V88 | 132655.92 | -47 2516.5 | 0.6902 | 0.690211 | V | 51675.5816 | V | 51336.6296 |
| V89 | 132645.97 | -47 2601.1 | 0.3751 | 0.374179 | R | 51269.9529 | ... | ... |
| V90 | 132645.74 | -47 2623.5 | 0.6034 | 0.603405 | V | 50985.6623 | V | 50973.5512 |
| V91 | 132650.60 | -47 2615.7 | 0.8952 | 0.895222 | V | 51335.4843 | V | 51675.5464 |
| V94 | 132557.10 | -4722 46.4 | 0.2539 | 0.253934 | ... | ... | $\ldots$ | ... |
| V95 | 132524.92 | -47 2852.9 | 0.4051 | 0.404966 | V | 51320.6449 | V | 51307.5743 |
| V96 | 132639.29 | -47 2703.2 | 0.6245 | 0.624528 | ... | ... | V | 51276.8216 |
| V97 | 132708.50 | -47 2531.3 | 0.6919 | 0.691890 | V | 49860.6212 | V | 51276.8570 |
| V98 | 132705.85 | -47 2657.0 | 0.2806 | 0.280566 | R | 51269.7700 | $\ldots$ | ... |
| V99 | 132702.15 | -47 2749.2 | 0.7662 | 0.766179 | V | 51339.6367 | V | 51346.4656 |
| V100 | 132704.03 | -47 2733.7 | 0.5527 | 0.552748 | V | 50975.6734 | V | 50975.6290 |
| V101 | 132730.23 | -47 2951.5 | 0.3409 | 0.340947 | ... | ... | V | 49869.7149 |
| V102 | 132722.10 | -4730 12.8 | 0.6914 | 0.691396 | V | 50975.5875 | V | 50975.5249 |
| V103 | 132714.28 | -47 2836.7 | 0.3289 | 0.328856 | V | 50977.4642 | V | 50978.7052 |
| V104 | 132807.80 | -4733 44.7 | 0.8665 | 0.866567 | V | 49824.5449 | V | 51316.6254 |
| V105 | 132746.04 | -47 3244.2 | 0.3353 | 0.335331 | V | 51677.6761 | ... | ... |
| V106 | 132659.18 | -4728 12.8 | 0.5699 | 0.569903 | $\ldots$ | ... | V | 51305.4665 |
| V107 | 132714.03 | -473058.3 | 0.5141 | 0.514104 | V | 50973.6737 | V | 49860.6035 |
| V108 | 132704.69 | -4729 26.0 | 0.5945 | 0.594457 | V | 50971.6508 | V | 50984.6830 |
| V109 | 132701.55 | -47 2936.9 | 0.7441 | 0.744099 | V | 50984.6119 | V | 50984.5494 |
| V110 | 132702.06 | -4730 07.0 | 0.3321 | 0.332102 | ... | ... | V | 51276.6422 |
| V111 | 132649.01 | -4728 40.5 | 0.7629 | 0.762901 | $\ldots$ | $\ldots$ | ... | ... |
| V112 | 132654.26 | $-473023.5$ | 0.4744 | 0.474356 | V | 49165.5101 | V | 50985.5829 |
| V113 | 132656.31 | -473147.8 | 0.5734 | 0.573376 | V | 50978.6264 | V | 50978.5866 |
| V114 | 132650.12 | -47 3021.3 | 0.6753 | 0.675308 | V | 50978.5500 | V | 50984.5544 |
| V115 | 132612.30 | -47 3417.9 | 0.6305 | 0.630480 | V | 50983.6326 | V | 50983.5881 |
| V116 | 132635.49 | -4728 07.2 | 0.7201 | 0.720134 | ... | .. | ... | ... |
| V117 | 132619.91 | -4729 21.5 | 0.4216 | 0.421643 | I | 49862.6933 | I | 49861.7506 |
| V118 | 132640.56 | -473019.4 | 0.6116 | 0.611620 | V | 50975.5726 | V | 50972.4694 |
| V119 | 132638.30 | -473118.3 | 0.3059 | 0.305875 | B | 50983.6283 | B | 49869.5645 |
| V120 | 132625.54 | -473249.0 | 0.5485 | 0.548547 | V | 51383.4995 | V | 51218.8794 |
| V121 | 132628.18 | -473151.0 | 0.3042 | 0.304182 | B | 49867.7385 | B | 49867.6664 |
| V122 | 132630.32 | -47 3302.5 | 0.6349 | 0.634921 | $\ldots$ | ... | $\ldots$ | ... |
| V123 | 132651.08 | -47 3713.2 | 0.4742 | 0.474857 | $\cdots$ | ... | $\cdots$ | $\ldots$ |
| V124 | 132654.39 | -47 3907.4 | 0.3319 | 0.331862 | V | 51336.5309 | V | 51695.5318 |
| V125 | 132648.97 | -474103.5 | 0.5929 | 0.592878 | V | 49163.5691 | V | 49116.6901 |
| V126 | 132808.12 | -474046.2 | 0.3420 | 0.341854 | ... | $\ldots$ | ... | ... |
| V127 | 132519.45 | -47 2837.5 | 0.3053 | 0.305273 | V | 49525.6515 | V | 49515.5167 |
| V128 | 132617.75 | -473013.5 | 0.8350 | 0.834992 | V | 50984.6784 | V | 51276.8207 |
| V130 | 132610.02 | -47 1339.9 | 0.4932 | 0.493251 | ... | ... | ... | ... |
| V131 | 132630.07 | -4729 41.1 | 0.3923 | 0.392116 | V | 49862.5642 | V | 50983.4807 |
| V132 | 132639.20 | -472910.0 | 0.6557 | 0.655644 | B | 49862.6154 | B | 49867.8041 |
| V134 | 132513.34 | -47 1228.5 | 0.6529 | 0.652918 | ... | $\ldots$ | ... | ... |
| V135 | 132628.09 | -472918.3 | 0.6326 | 0.632583 | V | 50977.4876 | V | 51276.6459 |
| V136 | 132631.08 | -472740.9 | 0.3919 | 0.391926 | ... | ... | R | 51269.8385 |
| V137 | 132631.54 | -47 2704.6 | 0.3342 | 0.334210 | R | 51269.7525 | R | 51270.0141 |
| V139 | 132637.75 | -472735.4 | 0.6769 | 0.676871 | V | 50978.6914 | V | 50972.5424 |
| V140 | 132642.17 | -4730 07.4 | 0.6198 | 0.619805 | R | 51269.8991 | ... | ... |
| V141 | 132640.90 | -4729 28.2 | 0.6974 | 0.697436 | V | 50973.6452 | V | 50975.6468 |
| V142 | 132642.65 | -4728 43.0 | 0.3758 | 0.375867 | ... | ... | ... | ... |
| V143 | 132642.61 | -47 2729.0 | 0.8207 | 0.820756 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V144 | 132643.05 | -472818.0 | 0.8353 | 0.835322 | $\ldots$ | ... | $\ldots$ | $\ldots$ |
| V145 | 132651.23 | -473108.8 | 0.3732 | 0.374104 | $\ldots$ | $\ldots$ | R | 451269.8875 |
| V146 | 132652.86 | -47 2928.2 | 0.6331 | 0.633097 | R | 51269.7827 | R | 451269.7359 |
| V147 | 132715.90 | -47 3110.1 | 0.4227 | 0.422344 | V | 50978.6557 | V | 50978.5404 |

Table 2
(Continued)

| ID | $\begin{gathered} \alpha(\mathrm{J} 2000.0)^{\mathrm{a}} \\ \mathrm{~h} \mathrm{~m} \mathrm{~s} \end{gathered}$ | $\delta\left(\begin{array}{c} (\mathrm{J} 2000.0)^{\mathrm{a}} \\ 0, \ldots \end{array}\right.$ | Period ${ }^{\text {b }}$ |  | $T_{0}(\max )^{\text {c }}$ |  | $T_{0}\left(\right.$ rising ${ }^{\text {c }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Literature ${ }^{\text {d }}$ | LS | band | JD | band | JD |
| V149 | 132732.86 | -47 1343.2 | 0.6827 | 0.682724 | ... | ... | ... | ... |
| V150 | 132740.24 | -47 3600.2 | 0.8993 | 0.899341 | V | 51286.8153 | V | 51672.5273 |
| V151 | 132825.40 | -47 1600.2 | 0.4078 | ... | $\ldots$ | ... | ... | ... |
| V153 | 132649.67 | -4726 23.8 | 0.3862 | 0.386249 | ... | ... | ... | $\ldots$ |
| V154 | 132703.13 | -473033.0 | 0.3223 | 0.322338 | $\cdots$ | ... |  | ... |
| V155 | 132653.65 | -4724 42.8 | 0.4139 | 0.413933 | V | 50984.6753 | V | 50971.7192 |
| V156 | 132647.90 | -473152.5 | 0.3591 | 0.359071 | V | 51677.5795 | V | 51217.8803 |
| V157 | 132646.48 | -47 2717.7 | 0.4064 | 0.405979 | V | 50971.6121 | V | 50975.5531 |
| V158 | 132645.33 | -47 3040.4 | 0.3673 | 0.367293 | ... | ... | ... | ... |
| V159 | 132324.44 | -47 4333.1 | 0.3431 | ... | $\ldots$ | ... | $\ldots$ | ... |
| V160 | 132536.09 | -47 1232.3 | 0.3973 | 0.397263 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V163 | 132549.49 | -47 2021.7 | 0.3132 | 0.313231 | $\ldots$ | $\ldots$ | $\ldots$ | ... |
| V165 | 132639.40 | -47 2655.8 | 0.5008 | 0.500745 | ... | ... | ... | $\ldots$ |
| V166 | 132645.99 | -47 2615.4 | 0.3402 | 0.340208 | $\ldots$ | ... | $\ldots$ | ... |
| V168 ${ }^{\text {f }}$ | 132552.75 | -473203.2 | 0.3213 | 0.321297 | ... | ... | $\ldots$ | ... |
| V169 | 132720.46 | -47 2359.5 | 0.3191 | 0.319113 | $\ldots$ | $\ldots$ | R | 51270.0415 |
| V171 ${ }^{\text {e }}$ | 132258.93 | -464724.8 | ... | ... | $\ldots$ | ... | $\ldots$ | ... |
| V172 | 132755.14 | -470438.7 | 0.73805 | 0.737928 | V | 54273.4654 | V | 53830.6679 |
| V173 | 132943.24 | -47 1654.1 | 0.35899 | ... | ... | ... | ... | ... |
| V175 ${ }^{\text {g }}$ | 132310.35 | -48 1904.4 | 0.31613 | $\ldots$ | ... | ... | $\ldots$ | ... |
| V177 ${ }^{\text {e }}$ | 132904.27 | -47 3621.5 | 0.3147 | 0.314737 | ... | ... | ... | ... |
| V178 ${ }^{\text {e }}$ | 133150.27 | -47 1822.4 | ... | ... | $\ldots$ | $\ldots$ | ... | $\ldots$ |
| V179 ${ }^{\text {e }}$ | 132345.51 | -48 1752.9 | ... | $\ldots$ | ... | ... | ... | ... |
| V181 ${ }^{\text {e,f }}$ | 133000.45 | -474845.6 | 0.5884 | $\ldots$ | ... | $\ldots$ | ... | $\ldots$ |
| V182 ${ }^{\text {e }}$ | 133213.42 | -470618.6 | 0.5454 | $\ldots$ | $\ldots$ | ... | ... | ... |
| V183 ${ }^{\text {f }}$ | 132939.55 | -473018.9 | 0.2961 | ... | ... | ... | ... | ... |
| V184 | 132728.50 | -473135.9 | 0.3034 | 0.303372 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V185 | 132604.09 | -472146.9 | 0.3330 | 0.333112 | ... | $\ldots$ | ... | ... |
| V261 | 132715.42 | -472129.9 | 0.4025 | 0.402524 | $\ldots$ | $\ldots$ | $\ldots$ | ... |
| V263 | 132613.14 | -47 2610.2 | 1.0122 | 1.012155 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V264 | 132639.66 | -473028.5 | 0.3214 | 0.321393 | R | 51270.0231 | R | 51269.9432 |
| V265 | 132630.22 | -4728 45.6 | 0.4226 | 0.421831 | ... | ... | $\ldots$ | ... |
| V266 | 132639.63 | -472802.0 | 0.3523 | 0.352314 | . | ... | $\ldots$ | $\ldots$ |
| V267 | 132640.20 | -4726 36.0 | 0.3158 | 0.315827 | R | 51269.7863 | R | 51270.0413 |
| V268 | 132635.13 | -47 2611.2 | 0.8129 | 0.812933 | V | 51319.4966 | V | 51305.5583 |
| V270 | 132656.55 | -4730 06.0 | 0.3127 | 0.313060 | V | 50983.5909 | V | 51276.8595 |
| V271 | 132647.12 | -4730 04.2 | 0.4432 | 0.443130 | $\ldots$ | $\ldots$ | ... | .. |
| V272 | 132642.92 | -4725 56.7 | 0.3115 | 0.311478 | B | 50984.5116 | B | 50985.6849 |
| V273 | 132654.35 | -47 2708.9 | 0.3671 | 0.367132 | $\ldots$ | ... | $\ldots$ | ... |
| V274 | 132643.74 | -4722 48.3 | 0.3111 | 0.311087 | R | 51269.9023 | R | 51269.8313 |
| V275 | 132649.74 | -47 2737.4 | 0.3776 | 0.377768 | ... | ... | ... | ... |
| V276 | 132716.49 | -473317.9 | 0.3078 | 0.307803 | $\ldots$ | $\ldots$ | $\ldots$ | ... |
| V277 | 132659.97 | -472729.5 | 0.3516 | 0.351518 | $\ldots$ | $\cdots$ | $\ldots$ | $\ldots$ |
| V280 | 132709.35 | -47 2306.1 | 0.2816 | 0.281663 | R | 51269.9402 | R | 51269.8730 |
| V281 | 132706.29 | -47 4723.1 | 0.2850 | 0.285029 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| V283 ${ }^{\text {f }}$ | 132736.43 | -474640.0 | 0.5173 | 0.517349 | V | 49160.6603 | V | 49871.4634 |
| V285 | 132540.12 | -47 3448.5 | 0.3290 | 0.329015 | ... | ... | ... | ... |
| V288 | 132810.40 | -4723 47.4 | 0.2954 | 0.295567 | $\cdots$ | ... | $\ldots$ | ... |
| V289 | 132803.56 | -472127.8 | 0.3081 | 0.308092 | V | 51335.6008 | V | 49886.5767 |
| V291 | 132638.53 | -4733 28.3 | 0.3340 | 0.333987 | ... | ... | $\ldots$ | ... |
| NV339 | 132629.68 | -472952.3 | 0.3013 | 0.301324 | ... | $\ldots$ | R | 51269.8675 |
| NV340 | 132638.93 | -47 2732.8 | 0.3018 | 0.301821 | $\ldots$ | $\ldots$ | . | ... |
| NV341 | 132654.65 | -4728 48.3 | 0.3061 | 0.306145 | $\ldots$ | $\ldots$ | R | 51269.7419 |
| NV342 | 132718.68 | -4728 23.4 | 0.3084 | 0.308386 | $\ldots$ | $\ldots$ | $\ldots$ | ... |
| NV343 | 132647.81 | -47 2937.5 | 0.3102 | 0.310214 | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| NV344 | 132638.05 | -4724 44.9 | 0.3138 | 0.313767 | $\ldots$ | $\ldots$ | $\ldots$ | ... |
| NV346 | 132646.93 | -47 2814.3 | 0.3276 | 0.327626 | $\ldots$ | $\ldots$ | R | 51269.7469 |
| NV347 | 132650.84 | -472746.1 | 0.3288 | 0.328912 | $\ldots$ | ... | R | 51269.6745 |
| NV349 | 132651.81 | -47 2744.2 | 0.3642 | 0.364193 | $\ldots$ | ... | $\cdots$ | ... |
| NV350 | 132656.39 | -473050.5 | 0.3791 | 0.379109 | V | 51276.7921 | V | 51276.6883 |
| NV351 | 132642.64 | -47 2735.7 | 0.3856 | 0.385149 | $\ldots$ | . | ... | ... |
| NV352 | 132654.39 | -4729 12.0 | 0.3975 | 0.397561 | $\ldots$ | $\ldots$ | $\cdots$ | $\ldots$ |
| NV353 | 132643.80 | -47 2756.7 | 0.4010 | 0.401849 | I | 49868.6942 | I | 49863.7793 |

Table 2
(Continued)

| ID | $\begin{gathered} \alpha(\mathrm{J} 2000.0)^{\mathrm{a}} \\ \mathrm{~h} \mathrm{~m} \mathrm{~s} \end{gathered}$ | $\delta\left(\underset{0, \prime \prime \prime}{(\mathrm{~J} 2000.0)^{\mathrm{a}}}\right.$ | Period ${ }^{\text {b }}$ |  | $T_{0}(\max )^{\text {c }}$ |  | $T_{0}\left(\right.$ rising ${ }^{\text {c }}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Literature ${ }^{\text {d }}$ | LS | band | JD | band | JD |
| NV354 | 132638.60 | -47 2510.2 | 0.4199 | 0.419413 | $\ldots$ | $\ldots$ | R | 51269.7085 |
| NV357 | 132617.78 | -4730 24.0 | 0.2978 | 0.297778 | $\ldots$ | $\ldots$ | V | 51306.6406 |
| NV366 | 132641.57 | -473142.3 | 0.9999 | 0.999924 | ... | ... | ... | ... |
| NV399 | 132629.54 | -4730 03.0 | 0.3098 | 0.309808 | V | 52743.6880 | V | 51276.6715 |
| NV411 | 132640.77 | -4728 17.0 | 0.8449 | 0.844273 | ... | ... | ... | ... |
| NV433 ${ }^{\text {e,f }}$ | 132903.53 | -47 4858.3 | 0.6671 | 0.667130 | ... | ... | ... | $\ldots$ |
| NV455 ${ }^{\text {e }}$ | 132753.94 | -465543.9 | 0.9325 | ... | $\ldots$ | ... | $\ldots$ | $\ldots$ |
| NV456 ${ }^{\text {e }}$ | 132214.49 | -4724 21.6 | 0.3835 | ... | $\ldots$ | $\ldots$ | $\ldots$ | $\ldots$ |
| NV457 ${ }^{\text {f,h }}$ | 132954.56 | -475046.0 | 0.50859 | 0.508615 | $\ldots$ | ... | ... | $\ldots$ |
| NV458 ${ }^{\text {f,h }}$ | 133000.09 | -47 135.6 | 0.62031 | 0.620309 | $\ldots$ | $\ldots$ | V | 53877.5014 |

Notes.
${ }^{\mathrm{a}}$ The mean epoch associated to these coordinates is 2004 May.
${ }^{\mathrm{b}}$ Pulsation periods (days) based either on a compilation of literature values (Clement et al. 2001) or on the current estimate using the LS method.
${ }^{c}$ Epoch of light maximum and of mean magnitude on the rising branch (HJD-2,400,000) estimated using the spline fit to optical light curves.
${ }^{\text {d }}$ V80, V172 and V173 from Navarrete et al. (2015), V175 from Fernández-Trincado et al. (2015b), others from Clement et al. (2001).
${ }^{\mathrm{e}}$ Coordinates from Clement's catalog.
${ }^{\mathrm{f}}$ Candidate field RRL.
${ }^{\mathrm{g}}$ Coordinates from Fernández-Trincado et al. (2015b).
${ }^{\mathrm{h}}$ Coordinates from Navarrete et al. (2015).
allowed us to take account of this positional effect. The photometry based on all the other data sets was labeled other and provides most of the time interval covered by our photometric catalog. Note that these data were collected with several ground-based telescopes available at CTIO ( 0.9 m , 1.5 m , Blanco 4 m ), ESO ( $0.9 \mathrm{~m}, \mathrm{MPI} / \mathrm{ESO} 2.2 \mathrm{~m}$, NTT, VLT), and SAAO ( 1 m ). In passing we also note that the current data set was also built up to detect fast evolving objects, i.e., objects experiencing evolutionary changes on relatively short timescales.

The defining of local standards in the field of $\omega$ Cen was performed following the same criteria discussed in our previous work on M4 (free from blending, a minimum of three observations, standard error lower than 0.04 mag , and intrinsic variability smaller than 0.05 mag ; Stetson et al. 2014a). As a whole, 4180 stars satisfy these requirements and 4112 of these have high-quality photometry (at least five observations, standard error $<0.02 \mathrm{mag}$ and intrinsic variability smaller than 0.05 mag ) in at least two bands: 3462 in $U, 4112$ in $B, 4106$ in $V, 875$ in $R$, and 3445 in $I$.

These stars have been used as a local reference for the photometric calibration of 847,138 stars in the field of $\omega$ Cen from the final ALLFRAME reduction (Stetson 1994). The median seeing of the different data sets is $1!2$, but our 25 th percentile is $0!!86$, and the 10 th percentile is $0!65$. We measured stars in up to 2000 images covering the innermost cluster regions ( $13.4 \times 13!5$ ); this means that the stars located there were observed in $\sim 200$ images with seeing better than $0!65$. The cluster regions in which we measured stars in up to 100 images is $36!6 \times 31!6$; this means that roughly ten images were collected with a seeing better than $0!$ ! 65 . The use of ALLFRAME means that detections visible in these images and their positions were also used to fit those same stars in the poorer-seeing images. This analysis resulted in 583,669 stars with calibrated photometry in all three of $B, V$, and $I ; 202,239$ of them had calibrated photometry in all five of $U, B, V, R$, and $I$. A more detailed analysis of the current multiband
photometric data set will be provided in a forthcoming paper (V. F. Braga et al. 2016, in preparation).

The astrometry of our photometric catalog is on the system of the USNO A2.0 catalog (Monet 1998). The astrometric accuracy is $0!!1$ and allows us to provide a very accurate estimate of $\omega$ Cen's centroid. Following the approach applied to Fornax by Stetson et al. (1998b) we found $\alpha_{\text {center }}=13^{\mathrm{h}} 26^{\mathrm{m}}$ $46^{\text {s }} 71, \delta_{\text {center }}=-47^{\circ} 28^{\prime \prime} 59!.9$. The stars adopted to estimate the position of the cluster center have $V$-band magnitude between 16 and 20 and are located (with varying weights) up to $\sim 14^{\prime}$ from the adopted center. The mean epoch associated to these coordinates is 2004 May. New and accurate structural parameters will be provided in a forthcoming paper.

## 3. RRLS STARS

### 3.1. Identification

We adopted the online reference catalog for cluster variables "Catalogue of Variable Stars in Globular Clusters" by Clement et al. (2001, updated 2015). This catalog lists 456 variables (197 candidate RRLs) within the truncation radius ( $r_{t}=$ 57.03 arcmin, Harris 1996) of $\omega$ Cen and it is mostly based on the detailed investigations of Kaluzny et al. (2004). This catalog was supplemented with more recent discoveries by Weldrake et al. (2007) and Navarrete et al. (2015). Two candidate field RRLs NV457 and NV458 discovered by Navarrete et al. (2015) were not included in the online catalog. To provide accurate and homogeneous photometry for the entire sample of RRLs along the line of sight of $\omega$ Cen, they were included in the current sample. We have also removed the field star V180 from the sample, following Navarrete et al. (2015) who classify it as a W UMa binary star on the basis of its color and pulsation amplitude. Finally, we have included V175, recently recognized as a field RRL by FernándezTrincado et al. (2015b), who updated the uncertain classification of this object by Wilkens (1965). We ended up with 199 candidate RRLs. Eight out of the 199 objects are, according to their mean magnitudes and proper motions, candidate field
stars (van Leeuwen et al. 2000; Navarrete et al. 2015). Note that we also included two variables with periods similar to RRLs but for which the classification is not well established, namely NV366 (Kaluzny et al. 2004) and the candidate field variable NV433 (Weldrake et al. 2007).

To overcome possible observational biases in the current RRL sample, the identification of variable stars was performed ab initio using the Welch-Stetson (WS, Welch \& Stetson 1993; Stetson 1996) index. We adopted our own photometric catalog and we identified 176 candidate RRLs that had a WS index larger than 1.1. This list was cross-matched with Clement's catalog and we found that all of them were already known. We then compared the individual coordinates based on our astrometric solution with those given in the literature and found that the median difference of the coordinates is $0!41$, with a standard deviation from the median of $0!26$. The difference for the entire sample is smaller than $2^{\prime \prime}$; only for six out of the 176 stars is the difference between $1^{\prime \prime}$ and $2^{\prime \prime}$.

The above data were supplemented with unpublished Walraven WULBV photometry for two RRLs-V55 and V84 -collected by J. Lub in 1980-1981 at the Dutch telescope in La Silla. The Walraven photometry was transformed into the standard Johnson-Kron-Cousins photometric system (UBV) using the transformations provided by Brand \& Wouterloot (1988). Moreover, we supplemented the photometry of the two variables observed by J. Lub with $U B V$ photoelectric photometry from Sturch (1978). The number of RRLs for which we provide new astrometry is 186 , while those for which we provide new photometry is 178 .

For nine out of the remaining 21 stars, we were able to recover optical photometry in the literature: (a)-V281 and V283 from OGLE ( $V$ band, Kaluzny et al. 1997); (b)—V80, V177, NV411 and NV433 ( $V+R$ band, Weldrake et al. 2007); (c)—V172, NV457 and NV458 from CATALINA ( $V$ band, Drake et al. 2009, 2013a, 2013b, 2014; Torrealba et al. 2015).
We performed detailed tests concerning the photometric zero-point using the objects in common and we found that there is no difference, within the photometric errors, between the current photometry and the photometry provided by OGLE, CATALINA, Sturch (1978), and by J. Lub. On the other hand, we have not been able to transform into the standard photometric system the photometry collected by Weldrake et al. (2007) for the four variables V80, V177, NV411, and NV433. For these four objects we only provided a homogeneous period determination, while the other five were fully characterized (period, mean magnitude, amplitude).

The positions of the $\omega$ Cen RRLs based on our astrometric solution are listed in columns 2 and 3 of Table 2, together with their literature and current pulsation period (columns 4 and 5). The epoch of the mean magnitude along the rising branch (Inno et al. 2015) and of the maximum light are listed in columns 6-9 together with the photometric band adopted for the measurements. Note that the above epochs have been estimated using the spline fits of the light curves discussed in Section 3.3.
The sky distribution of the 187 candidate RRLs for which we have estimated pulsation parameters is shown in Figure 1, where red squares and light blue circles mark the position of fundamental (RRab) and first-overtone (RRc) RRLs (see Section 3.2). The candidate RRd variable V142 (see notes on individual variables in the Appendix) is marked with a green triangle.


Figure 1. Spatial distribution of the entire sample of $\omega$ Cen RRLs (199). The current optical photometry covers a sky area of $\approx 25^{\prime}$ across the cluster center. The upward red and black arrows plotted on the right ascension axis display the core and the half-mass radius (Harris 1996). The black arrows plotted in the bottom right corner display the orientation. The squares and open circles display the position of RRab (90) and RRc (104) variables, respectively. The candidate RRd variable (V142) is marked with a green triangle. Magenta squares (RRab) and circles (RRc) mark the position of the eight variables for which we have retrieved periods and either optical or NIR mean magnitudes in the literature and for which a mode classification is possible. Black stars mark the position of the four variables for which we do not have solid pulsation paramter estimates and mode classification. The plus symbols mark the position of the eight candidate field RRLs.

We retrieved mean optical magnitude and periods from the literature for three variables: V151 (Martin 1938), V159 (van Gent 1948) and for V175 (Fernández-Trincado et al. 2015b). Mean NIR magnitudes and periods for five variables (V173, V181, V183, V455, V456) were retrieved from Navarrete et al. (2015). Magenta squares (RRab) and circles (RRc) mark the position of these eight variables. The four candidate variables identified by Wilkens (1965, V171, V178, V179) and by Sawyer Hogg (1973, V182) for which we do not have solid estimates of the pulsation parameters and mode classification are marked with black stars. Among the 195 RRLs for which the pulsation characterization has been performed we have 104 RRc, 90 RRab, and a single RRd variable.

We performed a number of statistical tests concerning the radial distribution of RRab and RRc, but no clear difference was found.

### 3.2. Period Distribution

To take full advantage of the observing strategy adopted to collect the time series we used two independent methods to determine the periods: the string method (Stetson 1996; Stetson et al. 1998a) and our variant of the Lomb-Scargle (LS) method (Scargle 1982). The key advantages of these methods are: (a) they use multi-band photometry simultaneously; (b) they take account of intrinsic photometric errors. We have checked that, within 0.002 days, period estimates based on the two methods agree quite well with each other. The periods based on the LS method also agree with those given in the Clement catalog. The difference between the LS and the Clement periods is typically smaller than 0.0001 days. Only 28 variables show a difference
larger than 0.0001 days, but none has a difference larger than 0.001 days. Table 2 only gives the periods based on the LS method, because this method was also used for the variables with photometry only available in the literature. A preliminary analysis on the uncertainties of the periods suggests that they cannot be larger than $1 \times 10^{-6}$ days.
The period derivatives of RRLs in $\omega$ Cen have been investigated by Jurcsik et al. (2001). They collected photometric data available in the literature covering more than a century. They found that a sizable sample of RRab display a steady increase in their period, thus supporting the redward evolution predicted by horizontal branch (HB) models (Bono et al. 2016). On the other hand, the RRc showed irregular trends in period changes. This indicates that period changes are affected by evolutionary effects and by other physical mechanisms that have not been fully constrained (Renzini \& Sweigart 1980, p. 271). We plan to provide more quantitative constraints of the period changes after the analysis of NIR images we have already collected, since they will allow us to further increase the time interval covered by our homogeneous photometry.

It is well known that $\omega$ Cen hosts a sizable sample of RRc with periods longer than 0.4 days (Kaluzny et al. 2004). To constrain the pulsation mode of the candidate RRLs, we need to take account of their distribution in the Bailey diagram (period versus luminosity variation amplitude, see Section 3.4).

The current data allowed us to confirm the pulsation mode of the current candidate RRLs; they are listed in the last column of Table 3. Using either optical or NIR mean magnitudes (see Section 3.1) as a selection criterion to discriminate between candidate field and cluster RRLs, we found that the candidate cluster RRLs number 187, and among them are 101 RRc, 85 RRab, and a single candidate RRd variable.
To make the separation between field and cluster stars clearer, the former in Figure 1 are marked with a plus sign. As expected, field candidates tend to be located between the halfmass radius ( $r_{h}=5$ arcmin, Harris 1996) and the tidal radius ( $r_{t}$ $=1.2$, Marconi et al. 2014) of the cluster.
Note that, according to Weldrake et al. (2007) and Navarrete et al. (2015), the classification of the variable NV433, which has a peculiar light curve, is unclear. However, its apparent magnitude ( $K \sim 14.151 \mathrm{mag}$, Navarrete et al. 2015) seems to suggest that it is a candidate field variable.
The period distribution plotted in Figure 2 shows, as expected, a prominent peak for RRc (light blue shaded area) with roughly $20 \%$ of the variables ( 18 out of 101 ) with periods longer than 0.4 days.
The RRab show a broad period distribution ranging from 0.47 days to roughly one day (red shaded area). Long-period ( $P \geqslant 0.82-0.85$ days) RRLs are quite rare in Galactic globulars. Several of them have also been identified in two peculiar bulge metal-rich globulars-NGC 6388, NGC 6441 (Pritzl et al. 2001, 2002)—and in the Galactic field (Wallerstein et al. 2009). Whether they are truly long-period RRLs or shortperiod Type II Cepheids (TIICs) is still a matter of lively debate (Marconi et al. 2011; Soszyński et al. 2011). In the current investigation we are assuming, following the OGLE team, that the transition between RRLs and TIICs takes place across one day. More quantitative constraints on this relevant issue will be addressed in a future paper.
The ratio between the number of RRc and the total number of RRL $\left(N_{\text {tot }}=N_{a b}+N_{d}+N_{c}\right)$ is quite large $\left(N_{c} / N_{\text {tot }}=0.54\right)$,
roughly $\sim 0.1$ larger than the typical ratio of OoII clusters: $N_{c} /$ $N_{\text {tot }} \sim 0.44$, while the same ratio in OoI clusters is $N_{c} /$ $N_{\text {tot }} \sim 0.29$ (Oosterhoff 1939; Castellani \& Quarta 1987; Caputo 1990). The mean fundamental (F) period is $\left\langle P_{a b}\right\rangle=0.668$ days, i.e., quite similar to OoII clusters, since they have $\left\langle P_{a b}\right\rangle \sim 0.651$ days, while OoI clusters have $\left\langle P_{a b}\right\rangle \sim 0.557$ days. The mean first overtone (FO) period is $\left\langle P_{c}\right\rangle=0.359$ days, once again similar to OoII clusters, since they have $\left\langle P_{c}\right\rangle=0.356$ days, while OoI clusters have $\left\langle P_{c}\right\rangle=0.312$ days. However, these mean parameters should be treated with caution, since they have been estimated using the same selection criteria adopted by Fiorentino et al. (2015), i.e., we only took into account GCs hosting at least 35 RRLs. A more detailed comparison with different Oosterhoff groups and with RRLs in nearby stellar systems is given in Section 5.

### 3.3. Light Curves

The observing strategy of the large optical data sets adopted in this investigation was focused on RRLs. The main aim was an extensive and homogeneous characterization of their pulsation properties (period, mean magnitudes, amplitudes, and epochs of minimum and maximum light). The time coverage ( 24 years) and the approach adopted to perform simultaneous multiband photometry allow us to provide very accurate period determinations (see Section 3.2).
This experiment was also designed to provide accurate estimates of period variations, but this topic will be addressed in a forthcoming paper. This is the reason why we collected a few hundred phase points in a single band on individual nights. More importantly, we collected more than one thousand phase points on a time interval of one to two weeks. As a whole, this extremely dense sampling provides us with very good phase coverage for both short- and long-period RRLs. However, the phase coverage is marginally affected by aliasing in the transition between RRL and short-period TIIC (BL Herculis), i.e., in the period range across $\sim 1.0$ day.

The results of this observing strategy are visible in Figures 35 that show, from left to right, a selection of optical light curves in the UBVRI bands for an RRL star pulsating in the F mode (V100), in the FO mode (V103), and a RRab variable affected by Blazhko (V120). The number of phase points per band and the period are also labeled. The vertical bars display individual photometric errors. They are of the order of $\sigma_{U} \sim 0.026$, $\sigma_{B} \sim 0.025, \sigma_{V} \sim 0.014, \sigma_{R} \sim 0.012$ and $\sigma_{I} \sim 0.035$.
Solid red lines in Figures $3-5$ show the spline fits that we adopted to derive mean magnitudes, amplitudes and epochs of mean and maximum light of the RRLs. The UBVRI mean magnitudes of the candidate RRLs were derived by intensityaveraging the spline fits over a full pulsation cycle. They are listed in columns 2-6 of Table 3. Column 12 of the same table gives the photometric quality index of the individual light curves in the different bands. It is 0 for no phase coverage, 1 for poor phase coverage, 2 for decent coverage, and 3 for good coverage. The errors of the mean magnitudes have been determined as the weighted standard deviation between the spline fit and the individual phase points. We found that the errors on average, for good quality light curves, are: $\sigma_{B}=0.02 \mathrm{mag}, \sigma_{V}=0.01 \mathrm{mag}$, $\sigma_{R}=0.01 \mathrm{mag}$ and $\sigma_{I}=0.03 \mathrm{mag}$. The same errors for decent quality light curves are: $\sigma_{U}=0.02 \mathrm{mag}, \sigma_{B}=0.02 \mathrm{mag}$, $\sigma_{V}=0.01 \mathrm{mag}, \quad \sigma_{R}=0.02 \mathrm{mag}$ and $\sigma_{I}=0.04 \mathrm{mag}$. The mean magnitudes of the objects for which the light curve coverage is poor, typically in the Uband, was estimated as the

Table 3
Optical—UBVRI—Mean Magnitudes and Amplitudes for $\omega$ Cen RRLs

| ID | $\begin{gathered} \hline U^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \hline B^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \hline V^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} R^{R^{\mathrm{a}}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \hline I^{a} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A U^{\mathrm{b}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \hline A B^{\mathrm{b}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A V^{b} \\ (\text { mag } \end{gathered}$ | $\begin{gathered} \hline A R^{b} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \hline A D^{b} \\ (\mathrm{mag}) \end{gathered}$ | $q_{U B V R I}{ }^{\text {c }}$ | Mode ${ }^{\text {d }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V3 | $15.017 \pm 0.015$ | $14.888 \pm 0.005$ | $14.391 \pm 0.004$ |  | $13.685 \pm 0.010$ | 1.054 | 0.934 | 0.761 | $\ldots$ | 0.401 | 12301 | RRab |
| V4 | $15.207 \pm 0.185$ | $14.882 \pm 0.005$ | $14.467 \pm 0.009$ | $14.462 \pm 0.180$ | $13.787 \pm 0.018$ | ... | 1.525 | 1.119 | ... | 0.904 | 23322 | RRab |
| V5 | $15.303 \pm 0.028$ | $15.197 \pm 0.013$ | $14.702 \pm 0.011$ | $14.359 \pm 0.012$ | $14.174 \pm 0.031$ | 0.972 | 1.021 | 0.852-1.271 | 1.118 | 0.437 | 13332 | RRab* |
| V7 | $15.068 \pm 0.017$ | $14.896 \pm 0.010$ | $14.594 \pm 0.010$ | ... | $13.768 \pm 0.012$ | 0.739 | 0.885 | 0.950 | ... | 0.293 | 11301 | RRab |
| V8 | $15.126 \pm 0.022$ | $15.016 \pm 0.008$ | $14.671 \pm 0.005$ | $\ldots$ | $14.046 \pm 0.014$ | 1.368 | 1.467 | 1.263 | ... | 0.695 | 11302 | RRab |
| V9 | $15.592 \pm 0.403$ | $15.204 \pm 0.010$ | $14.779 \pm 0.006$ | $14.498 \pm 0.179$ | $14.175 \pm 0.023$ | ... | 1.348 | 0.700-1.170 | ... | 0.516 | 22322 | RRab* |
| V10 | $14.869 \pm 0.031$ | $14.826 \pm 0.017$ | $14.505 \pm 0.013$ | $14.027 \pm 0.018$ | $13.919 \pm 0.024$ | 0.694 | 0.565 | 0.421 | 0.539 | 0.280 | 12323 | RRc |
| V11 | $15.045 \pm 0.020$ | $14.866 \pm 0.026$ | $14.476 \pm 0.035$ | $14.406 \pm 0.221$ | $13.886 \pm 0.032$ | 0.675 | 0.784-1.261 | 0.453-1.017 |  | 0.576 | 22323 | RRab* |
| V12 | $14.950 \pm 0.024$ | $14.891 \pm 0.016$ | $14.498 \pm 0.008$ | $14.207 \pm 0.009$ | $13.915 \pm 0.030$ | 0.606 | 0.562 | 0.438 | 0.338 | 0.303 | 13333 | RRc |
| V13 | $15.025 \pm 0.022$ | $14.873 \pm 0.007$ | $14.471 \pm 0.004$ | ... | $13.828 \pm 0.009$ | 0.934 | 1.215 | 0.959 | ... | 0.440 | 12301 | RRab |
| V14 | $15.080 \pm 0.029$ | $14.860 \pm 0.067$ | $14.520 \pm 0.024$ | ... | $13.994 \pm 0.050$ | 0.737 | 0.598 | 0.477 | $\ldots$ | 0.295 | 12302 | RRc |
| V15 | $15.011 \pm 0.025$ | $14.904 \pm 0.024$ | $14.368 \pm 0.010$ | $14.163 \pm 0.091$ | $13.686 \pm 0.034$ | 0.926 | 0.884 | 0.724 | ... | 0.481 | 13323 | RRab |
| V16 | $15.154 \pm 0.103$ | $14.912 \pm 0.003$ | $14.558 \pm 0.004$ | ... | $14.042 \pm 0.013$ | ... | 0.685 | 0.487 | ... | 0.305 | 23301 | RRc |
| V18 | $15.216 \pm 0.011$ | $14.841 \pm 0.005$ | $14.551 \pm 0.005$ | ... | $13.849 \pm 0.010$ | 1.333 | 1.307 | 1.152 | ... | 0.574 | 22301 | RRab |
| V19 | $15.455 \pm 0.020$ | $15.133 \pm 0.015$ | $14.829 \pm 0.005$ | ... | $14.319 \pm 0.040$ | 0.391 | 0.571 | 0.442 | ... | 0.277 | 12302 | RRc |
| V20 | $15.158 \pm 0.036$ | $14.990 \pm 0.018$ | $14.540 \pm 0.008$ | $14.209 \pm 0.008$ | $13.898 \pm 0.035$ | 0.888 | 1.376 | 1.098 | 0.948 | 0.686 | 12313 | RRab |
| V21 | $15.046 \pm 0.018$ | $14.698 \pm 0.013$ | $14.431 \pm 0.009$ | $14.135 \pm 0.009$ | $13.908 \pm 0.024$ | 0.555 | 0.624 | 0.476 | 0.376 | 0.248 | 12333 | RRc |
| V22 | $15.131 \pm 0.023$ | $14.857 \pm 0.009$ | $14.545 \pm 0.004$ |  | $13.922 \pm 0.011$ | 0.533 | 0.528 | 0.441 | ... | 0.323 | 12301 | RRc* |
| V23 | $15.304 \pm 0.017$ | $15.211 \pm 0.021$ | $14.821 \pm 0.011$ | $14.680 \pm 0.264$ | $14.192 \pm 0.029$ | 1.493 | 1.348 | 1.079 | ... | 0.705 | 23323 | RRab |
| V24 | $15.141 \pm 0.084$ | $14.810 \pm 0.008$ | $14.448 \pm 0.008$ | ... | $13.828 \pm 0.009$ | ... | 0.469 | 0.408 | ... | 0.229 | 22202 | RRc |
| V25 | $15.209 \pm 0.252$ | $14.889 \pm 0.017$ | $14.470 \pm 0.010$ | $14.065 \pm 0.010$ | $13.894 \pm 0.030$ | ... | 1.160 | 0.912 | 0.820 | 0.639 | 22313 | RRab |
| V26 | $15.109 \pm 0.021$ | $14.996 \pm 0.010$ | $14.470 \pm 0.008$ | $14.003 \pm 0.013$ | $13.773 \pm 0.015$ | 0.474 | 0.786 | 0.618 | 0.446 | 0.393 | 12312 | RRab |
| V27 | $15.448 \pm 0.019$ | $15.248 \pm 0.024$ | $14.665 \pm 0.012$ | $14.229 \pm 0.011$ | $13.968 \pm 0.032$ | 0.685 | 0.707 | 0.562 | 0.406 | 0.341 | 12323 | RRab |
| V30 | $15.089 \pm 0.147$ | $14.813 \pm 0.021$ | $14.451 \pm 0.010$ | $13.962 \pm 0.009$ | $13.882 \pm 0.031$ | ... | 0.443 | 0.393 | 0.276 | 0.216 | 22333 | RRc* |
| V32 | $14.990 \pm 0.019$ | $14.860 \pm 0.014$ | $14.485 \pm 0.013$ | ... | $13.874 \pm 0.024$ | 1.001 | 1.437 | 1.133-1.242 | ... | 0.801 | 13303 | RRab* |
| V33 | $14.935 \pm 0.012$ | $14.904 \pm 0.005$ | $14.538 \pm 0.005$ | ... | $13.912 \pm 0.013$ | 1.470 | 1.500 | 1.177 | ... | 0.727 | 13301 | RRab |
| V34 | $15.045 \pm 0.022$ | $14.926 \pm 0.013$ | $14.428 \pm 0.011$ | ... | $13.761 \pm 0.019$ | 1.082 | 0.982 | 0.790 | ... | 0.497 | 13303 | RRab |
| V35 | $15.015 \pm 0.024$ | $14.880 \pm 0.012$ | $14.502 \pm 0.008$ | $14.290 \pm 0.008$ | $13.957 \pm 0.021$ | 0.459 | 0.599 | 0.488 | 0.356 | 0.291 | 13333 | RRc |
| V36 | $15.088 \pm 0.009$ | $14.791 \pm 0.009$ | $14.537 \pm 0.041$ | $14.241 \pm 0.008$ | $13.912 \pm 0.011$ | 0.427 | 0.574 | 0.487 | 0.334 | 0.321 | 11311 | RRc |
| V38 | $15.061 \pm 0.018$ | $14.941 \pm 0.011$ | $14.465 \pm 0.011$ | ... | $13.754 \pm 0.021$ | 0.635 | 0.770 | 0.606 | ... | 0.377 | 13303 | RRab |
| V39 | $15.233 \pm 0.013$ | $14.833 \pm 0.006$ | $14.534 \pm 0.009$ | $\ldots$ | $13.948 \pm 0.011$ | 0.480 | 0.571 | 0.500 | ... | 0.303 | 12202 | RRc |
| V40 | $15.109 \pm 0.022$ | $14.941 \pm 0.017$ | $14.511 \pm 0.009$ | $13.965 \pm 0.010$ | $13.866 \pm 0.036$ | 1.116 | 1.394 | 1.121 | 0.851 | 0.714 | 13313 | RRab |
| V41 | $15.209 \pm 0.030$ | $14.936 \pm 0.030$ | $14.505 \pm 0.013$ | $\ldots$ | $13.791 \pm 0.042$ | 1.338 | 1.212 | 0.983 | ... | 0.656 | 12302 | RRab |
| V44 | $15.315 \pm 0.027$ | $15.197 \pm 0.011$ | $14.709 \pm 0.009$ | $13.902 \pm 0.009$ | $14.083 \pm 0.014$ | 1.023 | 1.252 | 0.975 | 0.763 | 0.599 | 13322 | RRab |
| V45 | $15.199 \pm 0.028$ | $14.886 \pm 0.006$ | $14.560 \pm 0.009$ | ... | $13.877 \pm 0.007$ | 0.975 | 1.089 | 1.110 | ... | 0.502 | 11101 | RRab* |
| V46 | $15.152 \pm 0.016$ | $14.957 \pm 0.005$ | $14.501 \pm 0.005$ | ... | $13.951 \pm 0.102$ | 1.071 | 1.238 | 0.952 | ... | ... | 12302 | RRab |
| V47 | $15.102 \pm 0.113$ | $14.692 \pm 0.009$ | $14.347 \pm 0.004$ | ... | $13.778 \pm 0.011$ | ... | 0.518 | 0.403 | ... | 0.253 | 22201 | RRc |
| V49 | $15.245 \pm 0.018$ | $15.088 \pm 0.006$ | $14.597 \pm 0.004$ |  | $13.963 \pm 0.025$ | 1.204 | 1.294 | 0.944 | ... | 0.621 | 13302 | RRab |
| V50 | $15.228 \pm 0.012$ | $14.995 \pm 0.004$ | $14.638 \pm 0.005$ | $14.360 \pm 0.012$ | $13.956 \pm 0.013$ | 0.523 | 0.668 | 0.461 | 0.359 | 0.235 | 13312 | RRc |
| V51 | $15.025 \pm 0.025$ | $14.905 \pm 0.020$ | $14.511 \pm 0.009$ | $14.504 \pm 0.176$ | $13.932 \pm 0.051$ | 1.432 | 1.478 | 1.178 | ... | 0.781 | 13323 | RRab |
| V52 | $14.870 \pm 0.206$ | $14.648 \pm 0.023$ | $14.245 \pm 0.019$ | $\ldots$ | $13.723 \pm 0.019$ | .. | 1.313 | 1.372 | ... | 0.706 | 11101 | RRab |
| V54 | $14.951 \pm 0.025$ | $14.910 \pm 0.004$ | $14.410 \pm 0.006$ | $14.162 \pm 0.163$ | $13.718 \pm 0.012$ | 0.685 | 0.647 | 0.636 | $\ldots$ | 0.409 | 13211 | RRab |
| V55 | $15.735 \pm 0.083$ | $15.181 \pm 0.021$ | $14.693 \pm 0.021$ | ... | ... | $\ldots$ | 1.079 | 0.845 | ... | ... | 23311 | RRab |
| V56 | $15.386 \pm 0.020$ | $15.203 \pm 0.010$ | $14.757 \pm 0.005$ | $\ldots$ | $14.148 \pm 0.015$ | 0.791 | 0.657-1.618 | 0.451-1.117 | $\ldots$ | 0.507 | 12202 | RRab* |
| V57 | $15.156 \pm 0.011$ | $14.974 \pm 0.004$ | $14.469 \pm 0.004$ | ... | $13.650 \pm 0.013$ | 0.711 | 0.755 | 0.597 | ... | 0.207 | 13302 | RRab |
| V58 | $15.158 \pm 0.127$ | $14.791 \pm 0.016$ | $14.454 \pm 0.012$ | $14.130 \pm 0.012$ | $13.948 \pm 0.025$ | ... | 0.275 | 0.213 | 0.237 | 0.130 | 22232 | RRc |
| V59 | $15.306 \pm 0.423$ | $15.120 \pm 0.059$ | $14.674 \pm 0.028$ | $14.222 \pm 0.015$ | $14.041 \pm 0.026$ | ... | 1.136 | 0.790-1.140 | ... | 0.573 | 12313 | RRab* |
| V62 | $15.164 \pm 0.038$ | $14.828 \pm 0.019$ | $14.423 \pm 0.014$ | $14.037 \pm 0.014$ | $13.814 \pm 0.038$ | 0.771 | 1.439 | 1.123 | 0.852 | 0.727 | 13333 | RRab |
| V63 | $15.742 \pm 0.192$ | $14.961 \pm 0.011$ | $14.461 \pm 0.012$ | ... | $13.743 \pm 0.012$ | ... | 0.606 | 0.483 | ... | 0.280 | 22202 | RRab |
| V64 | $15.013 \pm 0.024$ | $14.886 \pm 0.014$ | $14.541 \pm 0.015$ | $\ldots$ | $14.034 \pm 0.022$ | 0.810 | 0.585 | 0.485 | ... | 0.326 | 23303 | RRc |
| V66 | $14.963 \pm 0.103$ | $14.865 \pm 0.024$ | $14.479 \pm 0.010$ | $14.215 \pm 0.009$ | $13.881 \pm 0.044$ | $\ldots$ | 0.504 | 0.392 | 0.317 | 0.303 | 22232 | RRc |
| V67 | $15.304 \pm 0.013$ | $15.085 \pm 0.006$ | $14.688 \pm 0.005$ | $14.609 \pm 0.097$ | $14.081 \pm 0.018$ | 1.596 | 1.295 | 0.919-1.074 | ... | 0.700 | 13312 | RRab* |
| V68 | $14.857 \pm 0.172$ | $14.645 \pm 0.006$ | $14.243 \pm 0.004$ | $\ldots$ | $13.627 \pm 0.017$ | ... | 0.512 | 0.378 | $\ldots$ | 0.171 | 21301 | RRc |

Table 3
(Continued)

| ID | $\begin{gathered} U^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} B^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} V^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} R^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} I^{a} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{aligned} & A U^{b} \\ & (\mathrm{mag}) \end{aligned}$ | $\begin{gathered} A B^{b} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A V^{b} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A R^{b} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A I^{b} \\ (\mathrm{mag}) \end{gathered}$ | $q_{U B V R I}{ }^{\text {c }}$ | Mode ${ }^{\text {d }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V69 | $15.163 \pm 0.028$ | $14.943 \pm 0.167$ | $14.504 \pm 0.100$ | ... | $13.839 \pm 0.020$ | 1.261 | 1.400 | 1.018 | ... | 0.638 | 11101 | RRab* |
| V70 | $14.980 \pm 0.156$ | $14.810 \pm 0.014$ | $14.466 \pm 0.017$ | ... | $13.926 \pm 0.043$ | ... | 0.531 | 0.433 | ... | 0.240 | 23303 | RRc |
| V71 | $15.055 \pm 0.188$ | $14.877 \pm 0.022$ | $14.509 \pm 0.013$ | $14.227 \pm 0.013$ | $13.948 \pm 0.041$ |  | 0.558 | 0.414 | 0.317 | 0.306 | 23333 | RRc |
| V72 | $15.191 \pm 0.012$ | $14.809 \pm 0.007$ | $14.501 \pm 0.010$ | ... | $13.946 \pm 0.017$ | 0.520 | 0.553 | 0.431 | ... | 0.323 | 12202 | RRc |
| V73 | $15.294 \pm 0.018$ | $15.190 \pm 0.203$ | $14.752 \pm 0.131$ | $\ldots$ | $14.066 \pm 0.078$ | 0.427 | ... |  | ... |  | 12202 | RRab* |
| V74 | $15.199 \pm 0.021$ | $14.944 \pm 0.005$ | $14.620 \pm 0.004$ | ... | $13.955 \pm 0.017$ | 1.121 | 1.532 | 1.123-1.253 | ... | 0.644 | 12302 | RRab* |
| V75 | $15.100 \pm 0.025$ | $14.851 \pm 0.004$ | $14.483 \pm 0.004$ | $14.160 \pm 0.010$ | $13.803 \pm 0.025$ | 0.448 | 0.529 | 0.381 | 0.255 | 0.347 | 12211 | RRc |
| V76 | $14.975 \pm 0.023$ | $14.804 \pm 0.005$ | $14.507 \pm 0.006$ | ... | $14.014 \pm 0.013$ | 0.346 | 0.485 | 0.380 | ... | 0.270 | 12201 | RRc |
| V77 | $15.094 \pm 0.023$ | $14.899 \pm 0.034$ | $14.485 \pm 0.019$ | $14.162 \pm 0.020$ | $13.856 \pm 0.063$ | 0.498 | 0.514 | 0.392 | 0.321 | 0.300 | 23222 | RRc |
| V79 | ... | $14.989 \pm 0.097$ | $14.585 \pm 0.015$ |  | $13.787 \pm 0.016$ | ... | 1.405 | 1.163 | ... | 0.527 | 02301 | RRab |
| V81 | $15.286 \pm 0.160$ | $14.889 \pm 0.005$ | $14.524 \pm 0.010$ | $\ldots$ | $13.989 \pm 0.020$ | $\ldots$ | 0.532 | 0.474 | $\ldots$ | 0.245 | 23302 | RRc |
| V82 | $15.115 \pm 0.121$ | $14.825 \pm 0.007$ | $14.520 \pm 0.014$ | $\ldots$ | $14.022 \pm 0.052$ | $\ldots$ | 0.518 | 0.413 | $\ldots$ | 0.257 | 22202 | RRc* |
| V83 | $15.069 \pm 0.177$ | $14.864 \pm 0.012$ | $14.532 \pm 0.013$ | $\ldots$ | $13.990 \pm 0.024$ | $\ldots$ | 0.616 | 0.520 | ... | 0.302 | 23203 | RRc |
| V84 | $14.786 \pm 0.070$ | $14.735 \pm 0.020$ | $14.265 \pm 0.016$ | $\ldots$ | $\ldots$ | 0.880 | 0.832 | 0.655 | $\ldots$ | ... | 12300 | RRab |
| V85 | $15.427 \pm 0.022$ | $14.946 \pm 0.006$ | $14.513 \pm 0.011$ | ... | $13.779 \pm 0.011$ | 0.546 | 0.536 | 0.437 | $\ldots$ | 0.267 | 12202 | RRab |
| V86 | $15.097 \pm 0.029$ | $14.976 \pm 0.016$ | $14.509 \pm 0.011$ | $14.279 \pm 0.219$ | $13.810 \pm 0.038$ | 0.959 | 1.262 | 1.001 | ... | 0.693 | 13322 | RRab |
| V87 | $15.168 \pm 0.019$ | $14.926 \pm 0.017$ | $14.516 \pm 0.009$ | $14.279 \pm 0.009$ | $13.919 \pm 0.024$ | 0.486 | 0.552 | 0.460 | 0.352 | 0.273 | 13133 | RRc |
| V88 | $15.080 \pm 0.023$ | $14.941 \pm 0.005$ | $14.503 \pm 0.004$ | ... | $13.849 \pm 0.012$ | 1.083 | 1.024 | 0.855 | ... | 0.506 | 23302 | RRab |
| V89 | $15.453 \pm 0.266$ | $15.021 \pm 0.018$ | $14.613 \pm 0.014$ | $14.359 \pm 0.012$ | $14.065 \pm 0.037$ | ... | 0.574 | 0.460 | 0.387 | 0.301 | 22232 | RRc |
| V90 | $15.123 \pm 0.030$ | $14.886 \pm 0.017$ | $14.454 \pm 0.017$ | $14.262 \pm 0.018$ | $13.997 \pm 0.055$ | 1.277 | 1.395 | 1.130 | 0.921 | 0.816 | 12333 | RRab |
| V91 | $15.028 \pm 0.012$ | $14.871 \pm 0.018$ | $14.334 \pm 0.004$ | $14.034 \pm 0.081$ | $13.574 \pm 0.030$ | 0.643 | 0.772 | 0.588 | ... | 0.387 | 13323 | RRab |
| V94 | $15.333 \pm 0.134$ | $15.049 \pm 0.006$ | $14.763 \pm 0.004$ | ... | $14.315 \pm 0.010$ | ... | 0.265-0.448 | 0.172-0.326 | ... | 0.106 | 21101 | RRc* |
| V95 | $15.265 \pm 0.011$ | $14.930 \pm 0.004$ | $14.562 \pm 0.004$ | $14.278 \pm 0.083$ | $13.884 \pm 0.101$ | 0.561 | 0.582 | 0.422 | ... | ... | 13322 | RRc |
| V96 | $15.156 \pm 0.027$ | $14.883 \pm 0.048$ | $14.457 \pm 0.018$ | $14.352 \pm 0.121$ | $13.809 \pm 0.062$ | 0.925 | 1.320 | 1.029 | ... | 0.700 | 12222 | RRab |
| V97 | $15.074 \pm 0.326$ | $14.862 \pm 0.017$ | $14.489 \pm 0.008$ | $14.361 \pm 0.102$ | $13.781 \pm 0.033$ | ... | 1.110 | 0.941 | ... | 0.629 | 23323 | RRab* |
| V98 | $15.500 \pm 0.015$ | $15.146 \pm 0.004$ | $14.773 \pm 0.005$ | $14.481 \pm 0.036$ | $14.309 \pm 0.017$ | 0.500 | 0.665 | 0.461 | 0.380 | 0.250 | 12232 | RRc |
| V99 | $14.847 \pm 0.039$ | $14.691 \pm 0.008$ | $14.255 \pm 0.004$ | $13.892 \pm 0.271$ | $13.649 \pm 0.017$ | 1.079 | 1.406 | 1.145 | ... | 0.503 | 12221 | RRab |
| V100 | $15.803 \pm 0.090$ | $15.088 \pm 0.029$ | $14.638 \pm 0.012$ | $14.307 \pm 0.012$ | $13.951 \pm 0.051$ | ... | 1.300 | 1.028 | 0.810 | 0.614 | 13332 | RRab |
| V101 | $15.095 \pm 0.046$ | $14.891 \pm 0.018$ | $14.563 \pm 0.016$ | ... | $14.047 \pm 0.038$ | 1.003 | 0.534 | 0.394 | ... | 0.256 | 12202 | RRc |
| V102 | $15.164 \pm 0.024$ | $14.979 \pm 0.015$ | $14.519 \pm 0.009$ | $14.114 \pm 0.132$ | $13.827 \pm 0.053$ | 0.648 | 1.209 | 0.933 | ... | 0.606 | 13323 | RRab |
| V103 | $15.207 \pm 0.013$ | $14.818 \pm 0.023$ | $14.474 \pm 0.012$ | $14.166 \pm 0.011$ | $13.959 \pm 0.038$ | 0.395 | 0.362 | 0.297 | 0.226 | 0.166 | 13332 | RRc |
| V104 | $15.294 \pm 0.102$ | $15.046 \pm 0.004$ | $14.507 \pm 0.004$ | ... | $13.701 \pm 0.011$ | ... | 0.525 | 0.378 | ... | 0.205 | 23302 | RRab |
| V105 | $15.331 \pm 0.016$ | $15.076 \pm 0.007$ | $14.734 \pm 0.005$ | $\ldots$ | $14.161 \pm 0.011$ | 0.399 | 0.648 | 0.461 | $\ldots$ | 0.260 | 11302 | RRc |
| V106 | $15.110 \pm 0.024$ | $14.861 \pm 0.022$ | $14.532 \pm 0.006$ | $14.269 \pm 0.013$ | $13.924 \pm 0.045$ | 1.230 | 1.089-1.652 | 1.083-1.282 | 0.854 | 0.804 | 12312 | RRab* |
| V107 | $15.354 \pm 0.028$ | $15.152 \pm 0.022$ | $14.753 \pm 0.009$ | $14.314 \pm 0.010$ | $14.117 \pm 0.034$ | 1.426 | 1.457 | 1.169 | 0.895 | 0.793 | 13333 | RRab |
| V108 | $15.126 \pm 0.023$ | $14.909 \pm 0.024$ | $14.518 \pm 0.014$ | $14.297 \pm 0.233$ | $13.912 \pm 0.030$ | 1.226 | 1.340 | 1.117 | ... | 0.685 | 13223 | RRab |
| V109 | $15.127 \pm 0.027$ | $14.852 \pm 0.018$ | $14.426 \pm 0.013$ | $14.064 \pm 0.016$ | $13.764 \pm 0.027$ | 0.759 | 1.247 | 0.995 | 0.857 | 0.599 | 13313 | RRab |
| V110 | $15.126 \pm 0.032$ | $14.917 \pm 0.023$ | $14.609 \pm 0.009$ | $14.235 \pm 0.011$ | $14.089 \pm 0.029$ | 0.749 | 0.616 | 0.487 | 0.454 | 0.253 | 11132 | RRc |
| V111 | $15.123 \pm 0.025$ | $15.037 \pm 0.052$ | $14.461 \pm 0.015$ | $14.135 \pm 0.095$ | $13.739 \pm 0.094$ | 0.651 | 0.775 | 0.649 | ... | 0.389 | 12222 | RRab |
| V112 | $15.494 \pm 0.022$ | $14.819 \pm 0.021$ | $14.505 \pm 0.019$ | $14.186 \pm 0.018$ | $14.001 \pm 0.034$ | 0.946 | 1.160-1.358 | 1.030-1.160 | 0.818 | 0.674 | 13333 | RRab* |
| V113 | $15.535 \pm 0.286$ | $15.006 \pm 0.024$ | $14.596 \pm 0.013$ | $14.045 \pm 0.013$ | $13.977 \pm 0.032$ | ... | 1.532 | 1.250 | 0.971 | 0.865 | 23313 | RRab |
| V114 | $15.375 \pm 0.176$ | $14.937 \pm 0.044$ | $14.506 \pm 0.014$ | $14.083 \pm 0.013$ | $13.810 \pm 0.051$ | ... | 1.141 | 0.920 | 0.721 | 0.602 | 23313 | RRab |
| V115 | $15.085 \pm 0.021$ | $14.959 \pm 0.015$ | $14.504 \pm 0.012$ | $13.645 \pm 0.015$ | $13.860 \pm 0.024$ | 1.353 | 1.265 | 0.990-1.160 | 0.959 | 0.638 | 12223 | RRab* |
| V116 | $15.164 \pm 0.027$ | $14.931 \pm 0.017$ | $14.463 \pm 0.019$ | $\ldots$ | $13.658 \pm 0.024$ | 0.969 | 1.013 | 0.653 | ... | 0.726 | 11101 | RRab |
| V117 | $15.085 \pm 0.108$ | $14.890 \pm 0.016$ | $14.444 \pm 0.012$ | $13.994 \pm 0.010$ | $13.908 \pm 0.029$ | ... | 0.550 | 0.435 | 0.346 | 0.268 | 22323 | RRc |
| V118 | $15.044 \pm 0.030$ | $14.963 \pm 0.023$ | $14.428 \pm 0.011$ | $13.979 \pm 0.010$ | $13.734 \pm 0.031$ | 1.041 | 1.182 | 1.057 | 0.840 | 0.654 | 12333 | RRab |
| V119 | $15.238 \pm 0.084$ | $14.902 \pm 0.027$ | $14.614 \pm 0.009$ | $14.191 \pm 0.009$ | $14.094 \pm 0.059$ | ... | 0.370 | 0.299 | 0.232 | 0.175 | 23232 | RRc |
| V120 | $15.159 \pm 0.027$ | $15.180 \pm 0.018$ | $14.755 \pm 0.008$ | $14.343 \pm 0.034$ | $14.051 \pm 0.038$ | 1.461 | 0.960-1.661 | 0.724-1.241 | 0.668 | 0.569 | 13313 | RRab* |
| V121 | $15.187 \pm 0.164$ | $14.845 \pm 0.023$ | $14.545 \pm 0.010$ | $14.051 \pm 0.009$ | $14.046 \pm 0.049$ | ... | 0.364 | 0.286 | 0.220 | 0.193 | 23232 | RRc |
| V122 | $15.022 \pm 0.032$ | $14.985 \pm 0.027$ | $14.520 \pm 0.008$ | $14.113 \pm 0.114$ | $13.866 \pm 0.051$ | 1.507 | 1.359 | 1.091 | ... | 0.718 | 13323 | RRab |
| V123 | $15.056 \pm 0.100$ | $14.835 \pm 0.025$ | $14.457 \pm 0.021$ |  | $13.889 \pm 0.055$ | ... | 0.477 | 0.422 | ... | 0.242 | 21101 | RRc |
| V124 | $15.001 \pm 0.039$ | $14.914 \pm 0.004$ | $14.561 \pm 0.004$ | $\cdots$ | $14.167 \pm 0.039$ | 0.761 | 0.730 | 0.504 | ... | ... | 13303 | RRc |

Table 3
(Continued)

| ID | $\begin{gathered} U^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} B^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} V^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} R^{\mathrm{a}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} I^{a} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{aligned} & A U^{\mathrm{b}} \\ & (\mathrm{mag}) \end{aligned}$ | $\begin{gathered} A B^{b} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A V^{\mathrm{b}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A R^{b} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} A l^{b} \\ (\mathrm{mag}) \end{gathered}$ | $q_{U B V R I}{ }^{\text {c }}$ | Mode ${ }^{\text {d }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| V125 | $14.883 \pm 0.012$ | $15.048 \pm 0.009$ | $14.587 \pm 0.010$ | ... | $13.991 \pm 0.178$ | 1.229 | 1.024 | 1.202 | ... |  | 12303 | RRab |
| V126 | $15.294 \pm 0.107$ | $14.866 \pm 0.008$ | $14.566 \pm 0.008$ | ... | $14.017 \pm 0.012$ | ... | 0.570 | 0.508 | ... | 0.204 | 12201 | RRc |
| V127 | $15.373 \pm 0.009$ | $14.883 \pm 0.008$ | $14.632 \pm 0.013$ | $14.288 \pm 0.037$ | $14.117 \pm 0.008$ | 0.299 | 0.397 | 0.325 | $\ldots$ | 0.144 | 23332 | RRc |
| V128 | $14.819 \pm 0.273$ | $14.828 \pm 0.018$ | $14.341 \pm 0.008$ | $13.815 \pm 0.088$ | $13.650 \pm 0.029$ | ... | 0.753 | 0.591 | ... | 0.374 | 23323 | RRab |
| V130 | $15.599 \pm 0.323$ | $15.165 \pm 0.011$ | $14.731 \pm 0.011$ | $14.576 \pm 0.076$ | $14.145 \pm 0.016$ | ... | 1.223 | 0.585-1.234 |  | 0.293 | 22211 | RRab* |
| V131 | $15.228 \pm 0.245$ | $14.828 \pm 0.020$ | $14.456 \pm 0.010$ | $14.054 \pm 0.009$ | $13.878 \pm 0.035$ | $\ldots$ | 0.551 | 0.429 | 0.338 | 0.273 | 22232 | RRc |
| V132 | $15.208 \pm 0.038$ | $14.836 \pm 0.038$ | $14.427 \pm 0.016$ | $14.031 \pm 0.016$ | $13.736 \pm 0.051$ | 0.864 | 1.188 | 0.985 | 0.764 | 0.556 | 13322 | RRab |
| V134 | $15.402 \pm 0.014$ | $15.030 \pm 0.010$ | $14.501 \pm 0.010$ | ... | $13.711 \pm 0.015$ | 0.908 | 1.049 | 0.989 |  | 0.402 | 22201 | RRab |
| V135 | $15.135 \pm 0.023$ | $14.904 \pm 0.027$ | $14.301 \pm 0.025$ | $13.672 \pm 0.037$ | $13.764 \pm 0.047$ | 0.947 | 1.269 | 0.937 | 0.645 | 0.588 | 12332 | RRab |
| V136 | $15.018 \pm 0.016$ | $14.712 \pm 0.025$ | $14.321 \pm 0.016$ | $14.015 \pm 0.020$ | $13.823 \pm 0.047$ | 0.319 | 0.493 | 0.385 | 0.285 | 0.253 | 12232 | RRc |
| V137 | $15.064 \pm 0.023$ | $14.890 \pm 0.020$ | $14.540 \pm 0.011$ | $14.248 \pm 0.010$ | $14.034 \pm 0.046$ | 0.503 | 0.617 | 0.498 | 0.364 | 0.282 | 12232 | RRc |
| V139 | $15.175 \pm 0.029$ | $14.845 \pm 0.024$ | $14.324 \pm 0.012$ | $13.964 \pm 0.011$ | $13.606 \pm 0.036$ | 0.892 | 1.050 | 0.843 | 0.676 | 0.530 | 12333 | RRab |
| V140 | $15.293 \pm 0.199$ | $14.671 \pm 0.019$ | $14.368 \pm 0.022$ | $13.712 \pm 0.020$ | $13.794 \pm 0.018$ | ... | 1.051 | 0.493-1.162 | 0.473 | 0.396 | 21122 | RRab* |
| V141 | $15.175 \pm 0.019$ | $14.916 \pm 0.026$ | $14.459 \pm 0.014$ | $14.101 \pm 0.079$ | $13.776 \pm 0.034$ | 0.693 | 0.794-1.239 | 0.568-1.050 | . | 0.434 | 13323 | RRab* |
| V142 | $15.453 \pm 0.222$ | $14.984 \pm 0.013$ | $14.466 \pm 0.017$ | $14.319 \pm 0.017$ | $13.833 \pm 0.038$ | ... | 0.590 | 0.280-0.640 | 0.350 | 0.517 | 21122 | RRd |
| V143 | $15.008 \pm 0.040$ | $14.874 \pm 0.163$ | $14.284 \pm 0.036$ | $13.752 \pm 0.031$ | $13.563 \pm 0.040$ | 0.957 | 0.801 | 0.563 | 0.411 | 0.396 | 13213 | RRab |
| V144 | $14.973 \pm 0.149$ | $14.967 \pm 0.022$ | $14.429 \pm 0.012$ | $14.064 \pm 0.014$ | $13.684 \pm 0.025$ | ... | 0.616 | 0.487 | 0.418 | 0.341 | 22232 | RRab |
| V145 | $15.422 \pm 0.177$ | $14.972 \pm 0.029$ | $14.540 \pm 0.017$ | $14.017 \pm 0.026$ | $13.987 \pm 0.051$ | ... | 0.637 | 0.428 | 0.328 | 0.266 | 22233 | RRc |
| V146 | $15.309 \pm 0.027$ | $14.996 \pm 0.024$ | $14.518 \pm 0.017$ | $14.138 \pm 0.013$ | $13.832 \pm 0.043$ | 0.806 | 1.381 | 1.070 | 0.833 | 0.688 | 12322 | RRab |
| V147 | $15.103 \pm 0.162$ | $14.776 \pm 0.026$ | $14.404 \pm 0.013$ | $13.941 \pm 0.015$ | $13.791 \pm 0.056$ |  | 0.432 | 0.409 | 0.317 | 0.245 | 22232 | RRc |
| V149 | $15.137 \pm 0.019$ | $14.953 \pm 0.007$ | $14.507 \pm 0.010$ | ... | $13.806 \pm 0.013$ | 0.901 | 0.889 | 0.704 | ... | 0.443 | 11101 | RRab |
| V150 | $15.057 \pm 0.011$ | $14.746 \pm 0.005$ | $14.282 \pm 0.003$ | ... | $13.435 \pm 0.114$ | 0.846 | 1.000 | 0.766 | ... | ... | 12303 | RRab |
| V153 | $15.163 \pm 0.043$ | $14.999 \pm 0.013$ | $14.657 \pm 0.011$ | $14.396 \pm 0.011$ | $13.936 \pm 0.013$ | 0.458 | 0.572 | 0.475 | 0.367 | 0.270 | 12232 | RRc |
| V154 | $15.083 \pm 0.022$ | $14.871 \pm 0.019$ | $14.579 \pm 0.008$ | $14.154 \pm 0.011$ | $14.005 \pm 0.032$ | 0.402 | 0.145 | 0.163 | 0.114 | 0.091 | 12232 | RRc |
| V155 | $15.258 \pm 0.164$ | $14.918 \pm 0.018$ | $14.490 \pm 0.010$ | $14.239 \pm 0.010$ | $13.866 \pm 0.026$ | ... | 0.447 | 0.419 | 0.301 | 0.235 | 22333 | RRc |
| V156 | ... | $14.926 \pm 0.004$ | $14.521 \pm 0.004$ | $15.429 \pm 0.043$ | ... | ... | 0.525 | 0.399 | 0.386 | $\ldots$ | 02310 | RRc |
| V157 | $15.221 \pm 0.021$ | $14.985 \pm 0.035$ | $14.590 \pm 0.018$ | $14.302 \pm 0.019$ | $13.973 \pm 0.049$ | 0.374 | 0.524 | 0.459 | 0.341 | 0.245 | 12332 | RRc |
| V158 | $15.077 \pm 0.118$ | $14.914 \pm 0.029$ | $14.478 \pm 0.024$ | $14.105 \pm 0.018$ | $13.985 \pm 0.033$ | ... | 0.465 | 0.406 | 0.327 | 0.250 | 22233 | RRc |
| V160 | $15.196 \pm 0.023$ | $14.870 \pm 0.011$ | $14.491 \pm 0.011$ | ... | $13.871 \pm 0.013$ | 0.413 | 0.576 | 0.490 | ... | 0.262 | 11101 | RRc |
| V163 | $15.191 \pm 0.114$ | $14.824 \pm 0.005$ | $14.538 \pm 0.007$ | $\ldots$ | $14.077 \pm 0.013$ | ... | 0.241 | 0.196 | $\ldots$ | 0.127 | 22302 | RRc |
| V165 | $15.493 \pm 0.025$ | ... | ... | $14.470 \pm 0.012$ |  | 0.671 |  |  | 0.510 |  | 10020 | RRab* |
| V166 | $\cdots$ | $14.922 \pm 0.015$ | $14.520 \pm 0.005$ | $14.284 \pm 0.012$ | $13.975 \pm 0.035$ | ... | 0.160 | 0.134 | 0.072 | 0.063 | 01111 | RRc |
| V168 | $15.691 \pm 0.022$ | $15.494 \pm 0.008$ | $15.135 \pm 0.011$ | $14.781 \pm 0.066$ | $14.597 \pm 0.015$ | 0.844 | 0.578 | 0.480 |  | 0.237 | 12232 | RRc |
| V169 | $15.204 \pm 0.126$ | $14.876 \pm 0.023$ | $14.588 \pm 0.009$ | $14.357 \pm 0.009$ | $14.082 \pm 0.064$ | ... | 0.275 | 0.229 | 0.140 | 0.145 | 21131 | RRc |
| V172 |  | ... | $14.175 \pm 0.060$ | ... | $\cdots$ | ... |  | 0.802 | ... | ... | 00200 | RRab |
| V184 | $15.256 \pm 0.110$ | $14.891 \pm 0.014$ | $14.594 \pm 0.017$ | ... | $14.138 \pm 0.041$ | ... | 0.263 | 0.206 | ... | 0.137 | 23302 | RRc |
| V185 | $15.071 \pm 0.147$ | $14.748 \pm 0.013$ | $14.465 \pm 0.013$ | ... | $14.021 \pm 0.018$ | ... | 0.162 | 0.137 | ... | 0.073 | 22202 | RRc |
| V261 | $15.137 \pm 0.091$ | $15.011 \pm 0.004$ | $14.562 \pm 0.004$ | ... | $13.855 \pm 0.011$ | ... | 0.076-0.272 | 0.040-0.130 | ... | 0.095 | 21102 | RRc* |
| V263 | $14.927 \pm 0.052$ | $14.837 \pm 0.012$ | $14.304 \pm 0.009$ | ... | $13.582 \pm 0.022$ | $\ldots$ | 0.275 | 0.222 | $\ldots$ | 0.137 | 22202 | RRab |
| V264 | $15.364 \pm 0.020$ | $15.070 \pm 0.021$ | $14.703 \pm 0.013$ | $\ldots$ | $14.165 \pm 0.047$ | 0.465 | 0.501 | 0.430 | ... | 0.230 | 13302 | RRc |
| V265 | $15.130 \pm 0.124$ | $14.882 \pm 0.024$ | $14.431 \pm 0.013$ | $14.067 \pm 0.010$ | $13.868 \pm 0.031$ | ... | 0.307 | 0.329 | 0.276 | 0.176 | 23232 | RRc |
| V266 | $15.180 \pm 0.075$ | $14.859 \pm 0.036$ | $14.519 \pm 0.012$ | $14.218 \pm 0.013$ | $13.980 \pm 0.038$ | ... | 0.284 | 0.184 | 0.175 | 0.146 | 22222 | RRc |
| V267 | $15.182 \pm 0.016$ | $14.773 \pm 0.078$ | $14.466 \pm 0.012$ | $14.216 \pm 0.013$ | $13.935 \pm 0.075$ | 0.287 | 0.336 | 0.244 | 0.165 | 0.151 | 12232 | RRc |
| V268 | $15.140 \pm 0.018$ | $14.957 \pm 0.004$ | $14.544 \pm 0.004$ | $14.641 \pm 0.133$ | $\cdots$ | 0.547 | 0.638 | 0.467 | ... | $\ldots$ | 13320 | RRab |
| V270 | $15.231 \pm 0.123$ | $14.810 \pm 0.037$ | $14.559 \pm 0.014$ | $14.213 \pm 0.016$ | $13.978 \pm 0.042$ | ... | 0.205 | 0.206 | 0.141 | 0.132 | 22332 | RRc |
| V271 | $15.181 \pm 0.233$ | $14.972 \pm 0.049$ | $14.492 \pm 0.063$ | $14.219 \pm 0.013$ | $13.869 \pm 0.071$ | $\ldots$ | 0.444 | 0.300 | 0.380 | 0.162 | 21121 | RRc |
| V272 | $15.222 \pm 0.083$ | $14.918 \pm 0.013$ | $14.594 \pm 0.019$ | ... | $14.113 \pm 0.038$ | ... | 0.223 | 0.166 | ... | 0.089 | 23302 | RRc |
| V273 | $15.094 \pm 0.096$ | $14.938 \pm 0.024$ | $14.575 \pm 0.034$ | $14.318 \pm 0.011$ | $13.991 \pm 0.035$ | ... | 0.491 | 0.291 | 0.240 | 0.250 | 22333 | RRc |
| V274 | $15.107 \pm 0.097$ | $14.889 \pm 0.016$ | $14.579 \pm 0.008$ | $14.381 \pm 0.008$ | $14.130 \pm 0.051$ | ... | 0.259 | 0.224 | 0.179 | 0.143 | 23332 | RRc |
| V275 | $15.344 \pm 0.178$ | $14.925 \pm 0.027$ | $14.504 \pm 0.014$ | $14.197 \pm 0.013$ | $13.910 \pm 0.041$ | ... | 0.409 | 0.144-0.358 | 0.129 | 0.209 | 22322 | RRc* |
| V276 | $15.142 \pm 0.105$ | $14.867 \pm 0.005$ | $14.549 \pm 0.007$ | $14.226 \pm 0.035$ | $14.078 \pm 0.013$ | $\ldots$ | 0.269 | 0.198 | ... | 0.111 | 22232 | RRc |
| V277 | $15.127 \pm 0.063$ | $14.797 \pm 0.040$ | $14.463 \pm 0.025$ | $14.158 \pm 0.015$ | $13.930 \pm 0.036$ | ... | 0.154 | 0.120 | 0.094 | 0.075 | 23333 | RRc |



## Notes.

${ }^{\text {a }}$ Mean UBVRI magnitudes. The means were computed as intensity averages and then transformed into magnitudes.
 maximum amplitudes of candidate Blazhko RRLs and of the candidate mixed-mode variable were estimated as the amplitudes of the lower and upper envelope of the observed data points.
${ }^{c}$ Photometric quality index of the light curves taking account of the phase coverage, uncertainties on individual measurements, and photometric scatter. The ranking is: 0 , not available; 1 , poor; 2 , decent; 3 , good.
${ }^{\mathrm{d}}$ Pulsation mode identification. RRab: fundamental; RRc: first overtone; RRd: mixed-mode. An asterisk marks the variables that are candidate Blazhko RRLs.
median of the measurements and their errors range from 0.04 (I band) to 0.11 mag ( $U$ band). The luminosity variation amplitudes in the UBVRI bands of the candidate RRLs for which we have either our photometry or literature photometry have been estimated as the difference between the minimum and the maximum of the spline fit. They are listed in columns 7-11 of Table 3. Note that the $U$-band amplitudes are available only for a limited number of variables. Moreover, the minimum and maximum amplitudes of the candidate Blazhko RRLs and of the candidate RRd variable were estimated as the amplitudes of the lower and the upper envelope of the observed data points.

### 3.4. Bailey Diagram

The Bailey diagram-period versus luminosity variation amplitude-is a powerful diagnostic for variable stars, being reddening- and distance-independent (Smith et al. 2011, p. 17). Moreover, the luminosity variation amplitudes are also minimally affected by possible uncertainties in the absolute photometric zero-point. These advantages become even more compelling when dealing with large cluster samples, and indeed $\omega$ Cen RRL provides the largest cluster sample after M3 and M62. The data in Figure 6 show, from top to bottom the amplitudes in the $B, V$, and $I$ band. The two solid lines overplotted on the RRab variables display the analytical relations for OoI and OoII clusters derived by Cacciari et al. (2005), while the solid line plotted over the RRc variables is the analytical relation for OoII clusters derived by (Kunder et al. 2013b).

The majority of the RRab of $\omega$ Cen lie along the OoII locus for periods longer than $\sim 0.6$ days, and along the OoI locus for shorter periods. On the other hand, RRab with periods longer than 0.80 days show, at fixed period, amplitudes that are systematically larger than typical for OoII clusters. Moreover, they also display a long-period tail not present in typical OoII clusters. The same distribution has already been observed in the $V$-band Bailey diagram provided by Clement \& Rowe (2000) and Kaluzny et al. (2004). More interestingly, there is evidence that a significant fraction ( $79 \%$ ) of candidate Blazhko RRLs ( 22 out of 28 ) have periods shorter than 0.6 days. This finding further supports the evidence originally presented by Smith (1981) concerning the lack of Blazhko RRLs with a period longer than $\approx 0.7$ days. Note that the Blazhkocity (Kunder et al. 2013b) among the RRab of $\omega$ Cen with periods shorter than 0.6 days is of the order of $46 \%$, thus suggesting that $\omega$ Cen is a cluster with a Blazhkocity that is on average $50 \%$ larger than other GGCs. However, this finding could be the consequence that time series data of GGCs do not cover with the appropriate cadence large time intervals (Jurcsik et al. 2012).

The above findings together with similar empirical evidence concerning the precise position of RRd variables (Coppola et al. 2015) shed new light on the topology of the RRL instability strip, and in particular on the color/effective temperature range covered by the different kinds of pulsators.

The RRc (light blue squares) plotted in Figure 6 display the typical "hairpin" or "bell" shape distribution. The OoII sequence from Kunder et al. (2013b) appears to be, at fixed pulsation period, the upper envelope of the RRc distribution. Moreover, they seem to belong to two different sub-groups (if we exclude a few long- and short-period outliers): (a) short-period-with periods ranging from $\sim 0.30$ to $\sim 0.36$ days and visual amplitudes ranging from a few hundredths of a
magnitude to a few tenths; (b) long-period-with periods ranging from $\sim 0.36$ to $\sim 0.45$ days and amplitudes clustering around $A V \sim 0.5$ mag. With the only exception of the metalrich clusters NGC 6388 (Pritzl et al. 2002), NGC 6441 (Pritzl et al. 2001), and V70 in M3 (Jurcsik et al. 2012), $\omega$ Cen is the only GGC where long-period RRc are found (Catelan 2004b). Theoretical and empirical evidence indicates that the RRc period distribution is affected by metallicity (Dall'Ora et al. 2003). An increase in metal content causes a steady decrease in the pulsation period (Bono et al. 1997b). The above evidence seems to suggest that the dichotomous distribution of RRc might be the consequence of a clumpy distribution in metal abundance (see Section 8). The reader interested in detailed insights on the metallicity dependence of the RRLs position in the Bailey diagram is referred to Navarrete et al. (2015).

To further constrain the fine structure of the Bailey diagram we plotted the same variables in a 3D plot. The distribution was smoothed with a Gaussian kernel. The top panel of Figure 7 shows that the distribution is far from being homogeneous, and indeed both the RRc and the RRab variables show double secondary peaks in the shorter- and longer-period range, respectively. This evidence is further supported by the isocontours plotted in the bottom panel of the same figure. These were estimated running a Gaussian kernel, with unit weight, over the entire sample. In this panel the long period of RRab variables can also be easily identified.

Despite the fact that the Bailey diagram for $\omega$ Cen RRL shows some peculiarities, these results fully support the OoII classification for $\omega$ Cen RRL suggested by Clement \& Rowe (2000) and more recently by Navarrete et al. (2015).

### 3.5. Luminosity Amplitude Ratio

The amplitude ratios are fundamental parameters together with the periods and the epoch of a reference phase (luminosity maximum, mean magnitude) for estimating the mean magnitude of variable stars using template light curves. This approach provides mean magnitudes with a precision of a few hundredths of a magnitude from just a few phase points (Jones et al. 1996; Soszyński et al. 2005; Inno et al. 2015). Two key issues that need to be addressed in using the amplitude ratios are possible differences between RRab and RRc variables and the metallicity dependence (Inno et al. 2015). The $\omega$ Cen RRLs play a key role in this context, for both the sample size and the well known spread in iron abundance.

Following the same approach adopted by Kunder et al. (2013b) and Stetson et al. (2014a), we estimated the amplitude ratios in different bands. Figure 8 shows the mean values of the amplitude ratios: $A B / A V$ (top), $A R / A V$ (middle) and $A I / A V$ (bottom) of $\omega$ Cen RRLs. We included only variables with the best-sampled light curves. We have quantified the goodness of the sampling of the light curve with a quality parameter, based on the number of phase points, the presence of phase gaps, and the uncertainties in the magnitudes of the individual phase points. The paucity of RRab variables in the middle panel is due to the fact that our $R$-band photometry was mostly collected during two single nights. Therefore, the $R$-band light curves of long-period RRLs are not well-sampled.

The amplitude ratios were estimated using the bi-weight to remove the outliers (Beers et al. 1990; Fabrizio et al. 2011; Braga et al. 2015). The individual values for RRab, RRc and for the global (All) samples are listed in Table 4 together with their errors and standard deviations. The errors account for the


Figure 2. Period distribution for RRab (red) and RRc (light blue) RRLs in $\omega$ Cen. The candidate RRd variable (V142) is plotted in green. The number of RRab, RRc and RRd candidate RRLs are labeled together with the mean periods of RRab and RRc and the ratio between the number of RRc and the total number of RRLs is $\left(N_{c} / N_{a b}+N_{d}+N_{c}\right)$. See the text for more details.
uncertainty in the photometry and in the estimate of luminosity maxima and minima. Estimates listed in Table 4 and plotted in Figure 8 indicate that there is no difference, within the errors, between the RRab and RRc amplitude ratios. Moreover, the data in Figure 8 show no clear dependence on the metal content: indeed metal-rich $([\mathrm{Fe} / \mathrm{H}]>-1.70$, blue and violet symbols) and metal-poor ( $[\mathrm{Fe} / \mathrm{H}] \leqslant-1.70$, light blue and red symbols) display quite similar amplitude ratios.

In passing we note that the RRc amplitude ratios have standard deviations that are larger than the RRab ones. The difference is mainly caused by the fact that short-period RRc are characterized by low amplitudes and small amplitude changes cause larger fractional variations. The standard deviations of RRab and RRc attain almost identical values if we consider only variables with $V$-band amplitudes larger than 0.35 mag. The difference is mainly caused by small uncertainties in the luminosity variation amplitudes causing a larger spread in the amplitude ratios.

In summary, the amplitude ratios of $\omega$ Cen RRLs agree quite well with similar estimates for other GGCs available in the literature (Di Criscienzo et al. 2011; Kunder et al. 2013b; Stetson et al. 2014a). To further characterize the possible dependence on metal content of the amplitude ratios we also estimated $A V / A I, A B / A I$ and $A B / A R$. The means, their errors and standard deviations are also given in Table 4. We found that the current ratio $A V / A I=1.60 \pm 0.02$ agrees quite well with the estimate provided by Kunder et al. (2013b, see their Tables 3 and 4). There is one outlier NGC 3201, but this cluster contains only four RRc. The ratio $A B / A I=2.00 \pm 0.02$ is also in reasonable agreement with literature values. There are two outliers, namely NGC 6715 and NGC 3201, that are classified as Oo Int clusters (see Section 5). The $A B / A V \sim 1.25$ ratio agrees well with literature values, but slightly larger values have been found for M22 and NGC 4147 ( $A B / A V \sim 1.37$ ). Finally, the ratio $A B / A R$ of the RRL in $\omega$ Cen is, within the errors, the same as in M4 (Stetson et al. 2014a).

On the whole the above findings indicate that F and FO amplitude ratios do not depend on the metal content in the range covered by RRL in $\omega$ Cen $([\mathrm{Fe} / \mathrm{H}]=-2.4 \div-1.0)$ and in the other clusters considered $([\mathrm{Fe} / \mathrm{H}]=-2.4 \div-1.2$, Harris 1996; Kunder et al. 2013b).

## 4. THE RRLS IN THE COLOR-MAGNITUDE DIAGRAM

Current photometry allowed us to derive an accurate CMD covering not only the bright region typical of RGB and AGB stars ( $V \sim 11-12 \mathrm{mag}$ ), but also $\sim 3$ mag fainter than the main sequence turn-off region. Figure 9 shows the optical $V, B-I$ CMD of $\omega$ Cen. The stars plotted in the above CMD have been selected using the photometric error ( $\sigma_{V} \sim 0.03$, $\sigma_{B-I} \sim 0.04 \mathrm{mag}$ ), the $\chi$ parameter $(<1.8)$, quantifying the deviation between the star profile and the adopted point-spread function (PSF), and the sharpness $(\mid$ sha $\mid<0.7)$ quantifying the difference in broadness of the individual stars compared with the PSF. In passing we note that PSF photometry of individual images is mandatory to improve the precision of individual measurements of variable stars. The identification and fitting of faint sources located near the variable stars provides an optimal subtraction of light contamination from neighboring stars.

On top of the cluster photometry, Figure 9 also shows the 170 out of the 195 RRLs for which we estimated both $B-, V-$ and $I$-band mean magnitudes. The light blue, red, and green symbols display RRc, RRab and the candidate RRd variable. The RRc are located, as expected, on the blue (hot) side of the instability strip, while the RRab are in the red (cool) region of the instability strip (Bono et al. 1997c). The crosses mark candidate Blazhko variables. The black plus sign identifies a candidate RRc field variable-V168-with a mean visual magnitude that is $\sim 0.6 \mathrm{mag}$ fainter than cluster variables.

To further define the range in magnitude and colors covered by cluster RRLs, the left panel of Figure 10 shows a zoom across the instability strip. The blue and red lines display the predicted hot (blue) edge for FO pulsators (FOBE) and the cool (red) edge for F pulsators (FRE). Note that the predicted edges are based on the analytical relations provided by Marconi et al. (2015) (see their Table 5). We assumed a metal content $\log Z=0.0006$ and an $\alpha$-enhanced chemical mixture ( $[\alpha /$ $\mathrm{Fe}]=0.4)$. This means an iron abundance of $[\mathrm{Fe} /$ $\mathrm{H}]=-1.81^{22}$ These iron and $\alpha$-element abundances are consistent with the peak in the metallicity distribution of evolved stars in $\omega$ Cen based on recent spectrophotometric (Calamida et al. 2009) and spectroscopic (Johnson \& Pilachowski 2010) measurements. The agreement between theory and observations is remarkable if we take account of the theoretical and empirical uncertainties at the HB luminosity level. The former include a $\sim 50 \mathrm{~K}$ uncertainty on the temperature of the computed models, taking account of the adopted step in temperature (Di Criscienzo et al. 2004), plus uncertainties in color-temperature transformations $\left(\sigma_{B-I} \approx 0.05 \mathrm{mag}\right)$. The empirical uncertainty on both the FRE and the FOBE is $\sigma_{B-I} \sim 0.05 \mathrm{mag}$. Note that the possible occurrence of differential reddening $(\Delta E(B-V)=0.04 \mathrm{mag}$, Moni Bidin et al. 2012) mainly causes an increase in the photometric dispersion across the boundaries of the instability strip. The distribution of the RRLs inside the instability strip shows two interesting empirical features worth discussing in more detail.

Magnitude distribution. To provide firm estimates of spread in visual magnitude of the $\omega$ Cen RRLs we performed an analytical fit of the observed distribution. The right panel of Figure 10 shows the observed $V$-magnitude distribution as a

[^2]

Figure 3. From left to right $U B V R I$ light curves of the RRab variable V100. Red lines show the spline fits adopted to calculate mean magnitudes, luminosity variation amplitudes and the epochs of mean magnitude and maximum light. Data and analytical fits cover two full pulsation cycles. The number of phase points per band are displayed in parentheses. The period is also labeled. The vertical error bars display intrinsic errors of individual data points.
blue histogram. To overcome deceptive uncertainties in the criteria adopted to bin the data, we smoothed the distribution, assigning to each RRL a Gaussian kernel (Di Cecco et al. 2010) with a $\sigma$ equal to the intrinsic error of the mean magnitude. The red curve was computed by summing the individual Gaussians over the entire data set. The main peak appears well defined and located at $\sim 14.5$ mag. To provide a more quantitative analysis, we fit the smoothed magnitude distribution with four Gaussian functions (purple curves). Note that the number of Gaussians is arbitrary: they were included only to minimize the residuals between analytical and observed distribution. The black solid curve shows the sum of the four Gaussians over the entire magnitude range. The data listed in Table 5 indicate that the two main peaks are located at $V \sim 14.47$ and $V \sim 14.56 \mathrm{mag}$ and include a significant fraction of the entire RRL sample, $\approx 51 \%$ and $\approx 25 \%$, respectively. The fainter and the brighter peaks are located at $V \sim 14.71$ and $V \sim 14.31$ mag and roughly include $\approx 11 \%$ and $\approx 13 \%$ of the RRL entire sample. This suggests the metal-rich and the metal-poor tail produce only a minor fraction of RRLs. The above spread in optical magnitude indicates, for a canonical $M_{V}^{R R}$ versus [Fe/H] relation (Bono et al. 1997a), that $\omega$ Cen RRLs cover a range in iron abundance of the order of 1.5 dex (see also Section 8).

Blazhko RRLs. The data in the left panel of Figure 10 indicate that a significant fraction ( $39 \%$ ) of candidate Blazhko RRLs belongs to the fainter peak ( $V \geqslant 14.6 \mathrm{mag}$ ). Preliminary evidence of clustering in magnitude and color of Blazhko RRLs has been found in M3 by Catelan (2004a), but a Kolmogorov-Smirnov test gave negative results. We performed the same test on the $B-V$ and $B-I$ color distributions of Blazhko RRLs versus RRab and RRc variables. We found that the probability of the color distribution of Blazhko RRLs being equal to the color distribution of RRab and RRc is on average smaller than $1 \%$. Moreover, we also confirm the preliminary empirical evidence based on the Bailey diagram (see Section 3.5): they are mainly located between the FO and the F instability regions. The above finding suggests that candidate Blazhko RRLs in $\omega$ Cen attain intermediate colors/ temperatures.

Moreover, the difference in mean visual magnitude between the fainter ( $V \geqslant 14.6 \mathrm{mag}$ ) and the brighter ( $V<14.6 \mathrm{mag}$ ) sample suggests that the former are slightly more metal-rich.

This working hypothesis is supported by metallicity estimates based on spectrophotometric indices (Rey et al. 2000) suggesting, for fainter and brighter Blazhko RRLs, mean metallicities of $-1.4 \pm 0.3$ and $-1.8 \pm 0.1$ dex (see, e.g., Section 8). Metallicity estimates based on spectroscopic measurements (Sollima et al. 2006a) support the same finding, and indeed the mean iron abundances for fainter and brighter Blazhko RRLs are $-1.2 \pm 0.1$ and $-1.7 \pm 0.2$ dex, respectively. In passing, we also note that empirical evidence indicates that the Blazhko phenomenon occurs with higher frequency in more metal-poor environments (Kunder et al. 2013b). Homogeneous and accurate spectroscopic iron abundances are required to further investigate this interesting preliminary result.

## 5. COMPARISON WITH RRLS IN GLOBULARS AND IN DWARF GALAXIES

The large number of RRLs in $\omega$ Cen allows us to perform a detailed comparison with pulsation and evolutionary properties of RRLs in nearby stellar systems. To overcome thorny problems caused by small number statistics we selected, following Fiorentino et al. (2015), only GGCs hosting at least 35 RRLs. These are 16 out of the $\sim 100$ GGCs hosting RRLs (Clement et al. 2001). To characterize the role played by the metallicity in shaping their pulsation properties they were divided, according to their metal content (Harris 1996), into four different groups:
$\mathrm{OoI}^{23}$ —including 402 RRab, 6 RRd and 165 RRc with iron abundances ranging from $[\mathrm{Fe} / \mathrm{H}]=-1.00$ to -1.50 ;
OoInt ${ }^{24}$-including 324 RRab , and 50 RRc with iron abundances ranging from $[\mathrm{Fe} / \mathrm{H}]=-1.50$ to -1.65 ;

OoII ${ }^{25}$-including $111 \mathrm{RRab}, 28 \mathrm{RRd}$ and 111 RRc with iron abundances ranging from $[\mathrm{Fe} / \mathrm{H}]=-1.65$ to -2.40 .

OoIII ${ }^{26}$-including 60 RRab, 1 RRd and 41 RRc belonging to the two metal-rich globulars (Pritzl et al. 2001, 2002, 2003) NGC $6388([\mathrm{Fe} / \mathrm{H}]=-0.55)$ and $\operatorname{NGC} 6441([\mathrm{Fe} / \mathrm{H}]=$

[^3]

Figure 4. Same as Figure 3, but for the RRc variable V103.
-0.46). Note that we did not include the RRLs recently identified in Terzan 10 and in 2MASS-GC 02 by AlonsoGarcía et al. (2015), since these two clusters still lack accurate spectroscopic measurements of the iron abundance.
The data for RRLs in GGCs were complemented with similar data for RRLs in nearby gas-poor stellar systems, namely dwarf spheroidal (dSph) and ultra-faint dwarf (UFD) galaxies. Note that we did not apply any selection criterion on the number of RRLs in building up this sample. We ended up with a sample of 1306 RRab, 50 RRd and 369 RRc with iron abundances ranging from $[\mathrm{Fe} / \mathrm{H}]=-2.6$ to $[\mathrm{Fe} / \mathrm{H}]=-1.4$ (McConnachie 2012; Kirby et al. 2013; Fabrizio et al. 2015).

The double-mode variables-RRd—pulsate simultaneously in two different radial modes, typically F and FO. However, the latter is, with only a few exceptions (V44 in M3, Jurcsik et al. 2015), the main mode. However, they were not plotted in the Bailey diagram, since the separation of F and FO light curves requires very accurate and well sampled light curves (Coppola et al. 2015). They were also excluded from the period distribution, but included in the RRL population ratio, i.e., the ratio between the number of RRc and the total number of RRLs $\left(N_{c} / N_{\text {tot }}\right)$. We plan to provide a more detailed analysis of RRd variables in a follow-up paper.

In this context it is worth mentioning that the RRLs that in the Clement catalog are classified as second overtones-RRewere treated as RRc variables. Theoretical and empirical evidence indicates that the steady decrease in the pulsation period of RRc variables is mainly caused by a steady increase in metal content (Bono et al. 1997b). Note that the conclusions concerning the comparison between RRLs in $\omega$ Cen and in the other stellar systems are minimally affected by the inclusion of double-mode and possible candidate second overtone RRLs.

We estimated the diagnostics adopted to describe the Oosterhoff dichotomy: mean RRab and RRc periods and RRL population ratio for the stellar systems considered here, and their values are listed in Table 6 together with their uncertainties. We have already mentioned in Section 3.4 that $\omega$ Cen RRLs follow quite closely OoII clusters. However, data listed in this table together with the amplitudes and the period distributions plotted in Figure 11 display several interesting trends worth being discussed.
(i) Linearity. The mean periods display a steady increase when moving from more metal-rich to more metal-poor stellar
systems. The exception in this trend is given by the two metalrich bulge clusters (NGC 6388, NGC 6441). They are at least a half dex more metal-rich than OoI clusters, but their mean periods are from $\sim 25 \%$ (RRc) to $\sim 35 \%$ (RRab) longer. In passing we note that the above findings suggest that metal-rich globulars hosting RRLs belong to the Oosterhoff type 0 clusters instead of the OoIII group. This is the reason why their amplitudes and periods were plotted at the top of Figure 11 (see also the discussion in Section 9). On the other hand, the RRL population ratio shows a nonlinear trend, and indeed the OoInt clusters display a well defined minimum when compared with OoI, OoII and OoIII/Oo0 clusters. The decrease ranges from more than a factor of two with OoI to more than a factor of three with OoII and $\mathrm{OoIII} / \mathrm{Oo} 0$ clusters. The RRLs in dwarf galaxies appear to attain values typical of stellar systems located between OoInt and OoII clusters. Note that the RRc mean period attains very similar values in dwarfs, in OoII clusters, and in $\omega$ Cen, thus suggesting a limited sensitivity of this parameter in the more metal-poor regime.
(ii) Nature. The results mentioned in (i) open the path to a long-standing question concerning the nature of $\omega$ Cen, i.e., whether it is a massive GC or the former core of a dwarf galaxy. To further investigate this interesting issue we performed a more quantitative comparison between RRLs in $\omega$ Cen and in the aforementioned gas-poor stellar systems. The data in the left panels of Figure 11 display two clear features: (a) $\omega$ Cen and dwarf galaxies lack high-amplitude short-period (HASP) RRLs, i.e., F variables with $P \lesssim 0.48$ days and $A V>0.75 \mathrm{mag}$ (Stetson et al. 2014b). Empirical and theoretical evidence indicates that they become more and more popular in stellar systems more metal-rich than $[\mathrm{Fe} /$ $\mathrm{H}] \approx-1.4 /-1.5$ (Fiorentino et al. 2015). Therefore, the paucity of HASPs in $\omega$ Cen is consistent with previous metallicity estimates available in the literature (Calamida et al. 2009; Johnson \& Pilachowski 2010), and with the current metallicity estimates (see Section 8). We estimated the marginals of the Bailey diagrams plotted in the left panels of the above figure plus $\omega$ Cen and the $\chi^{2}$ analysis indicates that the latter agrees with OoII clusters at the $94 \%$ confidence level. The agreement with the other Bailey diagrams is either significantly smaller (39\% OoIII/Oo0; 42\% dwarfs) or vanishing (OoI, OoInt).


Figure 5. Same as Figure 3, but for the candidate Blazhko variable V120.


Figure 6. Top: Bailey diagram, $B$-band amplitude vs. period, for candidate $\omega$ Cen RRLs. RRab and RRc stars are plotted as red squares and light blue open circles, respectively. The candidate RRd variable (V142) is marked with a green triangle. Its abscissa is fixed at the period of the main (FO) mode. Candidate Blazhko RRLs are marked with a black cross. The solid black lines overplotted on the RRab stars display the loci typical of OoI and OoII GCs (Cacciari et al. 2005). The solid black lines overplotted on the RRab stars display the loci typical of OoI and OoII GCs (Cacciari et al. 2005). The solid black line overplotted on the RRc stars shows the locus of RRc typical of OoII GCs (Kunder et al. 2013b). Note that the latter relation was originally provided by Kunder et al. (2013b) for the Vband. It was transformed into the $B$ band using $A B / A V=1.26$. Middle: same as the top, but for the $V$-band amplitude. The vertical red bars display the range in luminosity amplitude of candidate Blazhko RRLs. The Oosterhoff relations for RRab stars were originally provided by (Cacciari et al. 2005) for the $B$ band. They were transformed into the $V$ band using $A B / A V=1.25$. Bottom: same as the top, but for the $I$-band amplitude. The original Oosterhoff relations for RRc and RRab stars were transformed into the $I$ band using $A I / A V=0.63$ (see Section 3.5).


Figure 7. Top: 3D Bailey diagram for candidate $\omega$ Cen RRLs: pulsation period in days, $V$-band amplitude and the $Z$-axis in arbitrary units. Bottom: same as the top, but with the view from the top.

On the other hand, the comparisons of the period distributions plotted in the right panels of Figure 11 clearly display that $\omega$ Cen is similar to an OoII cluster. Moreover, RRLs in $\omega$ Cen and in dwarf galaxies also display similar metallicity distributions. However, the coverage of the RRL instability strip in the former system appears to be more skewed toward the FO region than toward the F region as in the latter ones. The above


Figure 8. Top: ratio between the $B$ - and the $V$-band amplitude vs. the pulsation period for candidate $\omega$ Cen RRLs. Metal-poor and metal-rich variables (threshold at $[\mathrm{Fe} / \mathrm{H}]=-1.7$ ) are shown with different colors. Light blue and red symbols display metal-poor RRc and RRab, while blue and violet symbols mark metal-rich RRc and RRab, respectively. Black symbols are for variables with no $[\mathrm{Fe} / \mathrm{H}]$ estimate. The iron abundances come from R00 and S06 and the adopted values are listed in column 4 of Table 10 (see text for more details concerning iron abundances). The average value of the amplitude ratio for RRab and RRc and the error on the mean are also labeled. The solid line shows the mean value of the global sample (All), while the dashed lines display the standard deviation. Middle: same as the top, but for the amplitude ratio between the $R$ and Vband. Bottom: same as the top, but for the amplitude ratio between the $I$ and Vband.
difference is further supported by the stark difference in the population ratio and in the peaks of RRab and RRc period distributions. We also performed a $\chi^{2}$ analysis of the period distributions plotted in the right panels of Figure 11 and we found that RRLs in $\omega$ Cen agree with OoII clusters at the $80 \%$ confidence level. The agreement with the other samples is either at a few percent level or vanishing (dwarfs). Therefore, the working hypothesis that $\omega$ Cen is the core remnant of a spoiled dwarf galaxy (Zinnecker et al. 1988; Freeman 1993; Bekki \& Freeman 2003) does not find solid confirmation by the above findings. This result is somehow supported by the lack of firm signatures of tidal tails recently found by (FernándezTrincado et al. 2015b, 2015a) using wide-field optical photometry covering more than $50 \mathrm{deg}^{2}$ around the cluster center.
(iii) Nurture. $\omega$ Cen RRLs display a well defined long-period tail ( $P>0.8$ days) that is barely present in the RRL samples of the other systems. The exception is, once again, given by the two metal-rich globulars hosting RRLs, namely NGC 6388 and NGC 6441. A detailed analysis of the HB luminosity function is beyond the aim of the current investigation; however, we note that $\omega$ Cen and the two bulge clusters share an indisputable common feature, i.e., the presence in the HB luminosity function of a well extended blue tail. This suggests that its presence is more nurture than nature. The environment, and in particular, the high central density, might play a crucial role in the appearance of the blue tail, and in turn in the appearance of long-period RRLs (Castellani et al. 2006). Indeed, it has been
suggested (Castellani et al. 2007; Latour et al. 2014) that either binarity or stellar encounters might explain the presence of extended blue tails, and in turn, an increased fraction of blue HB stars evolving from the blue to the red region of the CMD. However, it is worth noting that the above evidence is far from taking account of the current empirical evidence, and indeed the metal-intermediate $([\mathrm{Fe} / \mathrm{H}]=-1.14$ Carretta et al. 2009) globular NGC 2808 hosts 11 RRab variables, but they have periods shorter than 0.62 days (Kunder et al. 2013a). It has also been suggested that a possible spread in helium abundance might also take account for the HB morphology in $\omega$ Cen Tailo et al. (2016) and, in turn, of the period distribution of RRLs. However, the increase in helium content is degenerate with possible evolutionary effects (Marconi et al. 2011) and we still lack firm conclusions. The reader interested in a recent detailed discussion concerning the Oosterhoff dichotomy and the HB morphology is referred to Jang \& Lee (2015).
Finally, we would like to underline that the above results strongly support the idea that only a limited number of GCs are good laboratories to understand the origin of the Oosterhoff dichotomy, the main limitations being statistics and environmental effects. This evidence further suggests that metallicity is the main culprit in shaping the above empirical evidence, while the HB luminosity function appears to be the next more plausible candidate. In passing, we also mention that a steady increase in helium content has also been suggested to take account of the extended blue tail in Galactic globulars (NGC 2808, D'Antona et al. 2005). The increase in helium content causes a steady increase in the pulsation period of both RRc and RRab variables (Marconi et al. 2011). Firm constraints require detailed sets of synthetic HB models accounting for both the HB morphology and the period distribution (Salaris et al. 2013; Sollima et al. 2014; Savino et al. 2015). We plan to investigate this issue in a forthcoming paper, since $\omega$ Cen is the perfect laboratory to constrain the transition from RRLs to TIICs.

## 6. RRL DIAGNOSTICS

### 6.1. PL Relations

On the basis of both periods and mean magnitudes measured in Section 3.3 and in 3.2, we estimated the empirical I-band PL relations of $\omega$ Cen RRLs. Following Braga et al. (2015) and Marconi et al. (2015) we evaluated the PL relations for RRc, RRab and for the global (All) sample. In the global sample the RRc were "fundamentalized," i.e., we adopted $\log P_{\mathrm{F}}=\log P_{\mathrm{FO}}+0.127$ (Iben \& Huchra 1971; Rood 1973; Cox et al. 1983; Di Criscienzo et al. 2004; Coppola et al. 2015). The coefficients, their errors and the standard deviations of the empirical PL relations are listed in Table 7. The RRLs adopted to estimate the PL relations are plotted in Figure 12.

Note that we derived the PL relations only in the Iband because theoretical (Bono et al. 2001; Catelan et al. 2004; Marconi et al. 2015) and empirical (Benkő et al. 2011; Braga et al. 2015) evidence indicates that RRLs do not obey a well defined PL relation in the $U, B$, and $V$ bands. Moreover, in the $R$ band, the dispersion is large ( $\sim 0.15 \mathrm{mag}$ ) and the slope is quite shallow ( $\sim-0.5 \mathrm{mag}$ ).

The standard deviations plotted in the bottom right corner of Figure 12 and the modest intrinsic error on the mean I-band magnitude discussed in Section 3.3 clearly indicate that the dispersion of the empirical $I$-band PL relation is mainly caused

Table 4
Mean Amplitude Ratios for RRab, RRc and for the Global (All) Sample of $\omega$ Cen RRLs

|  | RRab |  | RRc |  | All |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | mean | $\sigma$ | mean | $\sigma$ | mean | $\sigma$ |
| $\overline{A B / A V}$ | $1.25 \pm 0.01$ | 0.11 | $1.26 \pm 0.02$ | 0.16 | $1.26 \pm 0.01$ | 0.12 |
| $A R / A V$ | $0.80 \pm 0.03$ | 0.10 | $0.77 \pm 0.02$ | 0.12 | $0.78 \pm 0.01$ | 0.11 |
| $A I / A V$ | $0.63 \pm 0.01$ | 0.07 | $0.63 \pm 0.01$ | 0.10 | $0.63 \pm 0.01$ | 0.08 |
| AV/AI | $1.57 \pm 0.02$ | 0.13 | $1.63 \pm 0.03$ | 0.23 | $1.60 \pm 0.02$ | 0.20 |
| $A B / A R$ | $1.59 \pm 0.07$ | 0.28 | $1.57 \pm 0.04$ | 0.23 | $1.57 \pm 0.03$ | 0.24 |
| $A B / A I$ | $1.96 \pm 0.02$ | 0.14 | $2.03 \pm 0.04$ | 0.32 | $2.00 \pm 0.02$ | 0.26 |



Figure 9. Optical ( $V, B-I$ ) color-magnitude diagram of $\omega$ Cen. Light blue circles and red squares mark FO and F RRLs. The candidate RRd variable V142 is marked in green. The candidate FO field variable (V168) is marked with a black plus, while the black crosses display candidate Blazhko stars.
by the spread in metal abundance of $\omega$ Cen RRLs (see Section 8). Indeed, pulsation and evolutionary predictions (Bono et al. 2003a; Catelan et al. 2004; Marconi et al. 2015) indicate that the zero-points of the $I$-band PL relations do depend on metal abundance. We will take advantage of this dependence to estimate individual RRL metal abundances (see Section 8).

### 6.2. PW Relations

The PW relations, when compared with the PL relations, have the key advantage of being reddening-free by construction (Van den Bergh 1975; Madore 1982). This difference relies on the assumption that the adopted reddening law is universal (Bono et al. 2010). The pseudo-Wesenheit magnitude is defined as

$$
\begin{equation*}
W(X, Y-Z)=X+\frac{A_{X}}{A_{Y}-A_{Z}}(Y-Z) \tag{1}
\end{equation*}
$$

where $X, Y$ and $Z$ are the individual magnitudes and $A_{X}, A_{Y}$ and $A_{Z}$ are the selective absorption coefficients provided by the reddening law (Cardelli et al. 1989; Fitzpatrick \& Massa 2007).

We have adopted the popular reddening law of Cardelli et al. (1989) with $R_{V}=3.06$ and $A_{B} / A_{V(\text { Johnson })}=1.348, A_{V} / A_{V}$ $($ Johnson $\left.)=1.016 A_{I} / A_{V(\text { Johnson })}=0.590\right)$. Note that, to match the current optical photometric system (Landolt 1983, 1992), the original $R_{V}$ value ( $R_{V}=3.1$ ) and the selective absorption ratios provided by Cardelli et al. (1989) were modified accordingly.
Figure 13 shows the dual and triple band empirical PW relations for $\omega$ Cen RRLs. The coefficients, their errors and the standard deviations of the PW relations are listed in Table 8. The slopes of the PW relations listed in this table agree, within the errors, remarkably well with the slope predicted by nonlinear, convective hydrodynamical models of RRLs (Marconi et al. 2015, see their Tables 7 and 8). Indeed, the predicted slopes for the metal-independent $\operatorname{PW}(V, B-V)$ relations range from -2.8 , ( FO ), to -2.7 ( F ) and to -2.5 (global), while for the metal-dependent $\operatorname{PW}(V, B-I)$ relations they range from $-3.1(\mathrm{FO})$, to $-2.6(\mathrm{~F})$ and to -2.5 (global). The comparison in the latter case is very plausible, since the coefficient of the metallicity term for the $\mathrm{PW}(V, B-I)$ relations is smaller than 0.1 dex. The predicted slope for FO variables is slightly larger, but this might be due to the limited sample of adopted FO models.
The current empirical slopes for the optical PW relations agree quite well with similar estimates recently provided by Coppola et al. (2015) for more than 90 RRLs of the Carina dSph . They found slopes of -2.7 [global, $\mathrm{PW}(V, B-V)$ ] and -2.6 [global, $\mathrm{PW}(V, B-I)$ ]. The outcome is the same if we take account of the thorough analysis performed by MartínezVázquez et al. (2015) for the 290 RRLs (clean sample) of Sculptor dSph, namely -2.5 [global, PW $(V, B-I)$ ] and -2.7 [global, $\mathrm{PW}(V, B-I)]$. The reader interested in a detailed discussion concerning the physical arguments supporting the universality of the above slope is referred to the recent investigation by Lub (2016).

The data in Figure 13 display that the standard deviation of the different PW relations steadily decrease if either the effective wavelength of the adopted magnitudes increases (see panels (c), (d), (e) and (f)) and/or the difference in effective wavelength of the adopted color increases (see panels (d) and (h)). Finally, we note that the standard deviations of the PW(V, $B-V$ ) relations are systematically larger than the other PW relations. The difference is mainly caused by the fact that this PW relation has the largest color coefficient (3.06) and, in turn, the largest propagation of the intrinsic errors on mean colors.

## 7. DISTANCE DETERMINATION

The $\omega$ Cen RRLs cover a broad range in metal abundance. This means that accurate distance determinations based on


Figure 10. Left: same as Figure 9, but zoomed on the RRL instability strip. The blue line shows the predicted first overtone blue edge (FOBE), and the red one the predicted fundamental red edge (FRE) of the instability strip (Marconi et al. 2015). Right: distribution of the $V$ magnitudes of RRLs. The red curve shows the smoothed histogram. The four components of the multi-Gaussian fit are plotted in purple, while the black curve is the sum of the multi-Gaussian fit.

Table 5
Parameters of the Four Gaussians Adopted to Fit the $V$-band Magnitude Distribution of $\omega$ Cen RRLs

| Fit $^{\mathrm{a}}$ | $\mu$ | $\sigma$ | $A$ | Relative Area |
| :--- | :---: | :---: | :---: | :---: |
| 1 | 14.47 | 0.06 | 29.95 | 0.51 |
| 2 | 14.56 | 0.07 | 12.62 | 0.25 |
| 3 | 14.71 | 0.08 | 4.81 | 0.11 |
| 4 | 14.31 | 0.11 | 4.01 | 0.13 |

Note.
${ }^{\text {a }}$ Gaussian fit of the form $A^{*} \exp \left(\left(x-x_{0}\right) / \sigma\right)^{2}$.
diagnostics affected by the metal content require accurate estimates of individual iron abundances (Del Principe et al. 2006; Bono et al. 2008a). The observational scenario concerning iron abundances of $\omega$ Cen RRLs is far from being ideal. Estimates of the iron abundance for 131 RRLs in $\omega$ Cen were provided by Rey et al. (2000, hereinafter R00) using the $h k$ photometric index introduced by Baird (1996). More recently, Sollima et al. (2006a, hereinafter S06) estimated iron abundances for 74 RRLs in $\omega$ Cen using moderately highresolution spectra collected with FLAMES at VLT. These iron abundances are listed in columns 1 and 2 of Table 10. The former sample is in the globular cluster metallicity scale provided by Zinn \& West (1984, hereinafter ZW84).

They were transformed into the homogeneous and accurate metallicity scale provided by Carretta et al. (2009) using their linear transformation (see their Section 5). The iron abundances provided by S06 were estimated following the same approach adopted by Gratton et al. (2003) and Carretta et al. (2009). They were transformed into the Carretta's metallicity scale having accounted for the difference in the solar iron abundance ( $\log \epsilon_{\mathrm{Fe}_{\odot}}=7.52$ versus 7.54 ). Fortunately enough, the two samples have 52 objects in common. We estimated the difference between R00 and S06 and we found $\Delta[\mathrm{Fe} / \mathrm{H}]=$ $0.18 \pm 0.03(\sigma=0.20)$. We rescaled the R00 to the S06 iron abundances and computed the mean for the objects in common
(see column 4 in Table 10). Figure 14 shows the entire sample of $\omega$ Cen RRLs (153) for which a metallicity estimate is available in the $[\mathrm{Fe} / \mathrm{H}]-V$ plane. A glance at the data in this figure shows that the current uncertainties on individual iron abundances are too large to provide precise distance determinations. Indeed, the uncertainties on iron abundances range from less than 0.1 dex to more than 0.5 dex.
The above empirical scenario is further complicated by evidence that $\omega$ Cen might also be affected by differential reddening (Dickens \& Caldwell 1988; Calamida et al. 2005; Majewski et al. 2012) at a level of $\Delta E(B-V)=0.03-0.04 \mathrm{mag}$ (Moni Bidin et al. 2012).
To overcome the above thorny problems we decided to take advantage of recent findings concerning the sensitivity of optical and NIR diagnostics on metallicity and reddening to estimate RRL individual distances. Pulsation predictions indicate that the spread in magnitude of optical and NIR PW relations is smaller when compared with the spread typical of optical and NIR PL relations. This finding applies to both RRLs and classical Cepheids. The decrease in magnitude dispersion is mainly caused by the fact that the PW relations mimic a period-luminosity-color relation, thus taking account of the individual position of variable stars inside the instability strip (Bono \& Marconi 1999; Udalski et al. 1999; Soszyński et al. 2009; Marconi et al. 2015). Moreover, and even more importantly, theory and observations indicate that the $\mathrm{PW}(V$, $B-V$ and $V, B-I)$ relations display a minimal dependence on metallicity. Indeed, their metallicity coefficients are at least a factor of two smaller when compared with similar PW relations (Coppola et al. 2015; Marconi et al. 2015; Martínez-Vázquez et al. 2015).

For the reasons already mentioned in Section 6.2 (smaller standard deviation, smaller color coefficient) and above, we adopted the $\operatorname{PW}(V, B-I)$ relations to estimate the distance to $\omega$ Cen. To quantify possible uncertainties either on the zero-point or on the slope, we estimated the distance using the observed slope and the predicted zero-point (semi-empirical) and

Table 6
Pulsation Properties of RRLs in Different Gas-poor Stellar Systems and in $\omega$ Cen

| System | $\begin{aligned} & \left\langle P_{c}\right\rangle^{\mathrm{a}} \\ & \text { days } \end{aligned}$ | $N_{c}$ | $\begin{gathered} \left\langle P_{a b}\right\rangle^{\mathrm{a}} \\ \text { days } \end{gathered}$ | $N_{a b}$ | $N_{c} / N_{\text {tot }}{ }^{\text {b }}$ | $[\mathrm{Fe} / \mathrm{H}]^{\mathrm{c}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| OoIII/Oo0 |  |  |  |  |  |  |
| NGC 6388 | $0.384 \pm 0.017$ | 18 | $0.739 \pm 0.037$ | 13 | 0.58 | -0.55 |
| NGC 6441 | $0.380 \pm 0.016$ | 23 | $0.755 \pm 0.016$ | 47 | 0.32 | -0.45 |
| Total | $0.382 \pm 0.012$ | 41 | $0.752 \pm 0.015$ | 60 | 0.40 | $-0.55 /-0.45$ |
| OoI |  |  |  |  |  |  |
| NGC 5272 | $0.328 \pm 0.007$ | 46 | $0.564 \pm 0.005$ | 135 | 0.25 | $-1.50$ |
| NGC 5904 | $0.318 \pm 0.005$ | 38 | $0.551 \pm 0.008$ | 86 | 0.31 | -1.29 |
| NGC 6121 | $0.293 \pm 0.011$ | 14 | $0.548 \pm 0.014$ | 31 | 0.31 | -1.16 |
| NGC 6229 | $0.336 \pm 0.014$ | 8 | $0.552 \pm 0.009$ | 29 | 0.22 | -1.47 |
| NGC 6266 | $0.296 \pm 0.005$ | 35 | $0.556 \pm 0.008$ | 67 | 0.34 | -1.18 |
| NGC 6362 | $0.294 \pm 0.009$ | 17 | $0.547 \pm 0.016$ | 18 | 0.49 | -0.99 |
| NGC 6981 | $0.320 \pm 0.013$ | 7 | $0.568 \pm 0.009$ | 36 | 0.16 | -1.42 |
| Total | $0.312 \pm 0.003$ | 165 | $0.557 \pm 0.003$ | 402 | 0.29 | $[-1.50,-1.00]$ |
| OoInt |  |  |  |  |  |  |
| IC4499 | $0.342 \pm 0.008$ | 17 | $0.581 \pm 0.008$ | 59 | 0.22 | -1.53 |
| NGC 3201 | $0.330 \pm 0.015$ | 7 | $0.555 \pm 0.005$ | 72 | 0.09 | -1.59 |
| NGC 6715 | $0.335 \pm 0.011$ | 11 | $0.592 \pm 0.008$ | 72 | 0.13 | -1.49 |
| NGC 6934 | $0.308 \pm 0.014$ | 9 | $0.574 \pm 0.009$ | 68 | 0.12 | -1.47 |
| NGC 7006 | $0.333 \pm 0.016$ | 6 | $0.559 \pm 0.008$ | 53 | 0.10 | -1.52 |
| Total | $0.332 \pm 0.005$ | 50 | $0.573 \pm 0.004$ | 324 | 0.13 | $[-1.65,-1.50]$ |
| OoII |  |  |  |  |  |  |
| NGC 4590 | $0.368 \pm 0.007$ | 15 | $0.634 \pm 0.020$ | 12 | 0.39 | -2.23 |
| NGC 5024 | $0.344 \pm 0.007$ | 29 | $0.661 \pm 0.016$ | 19 | 0.60 | -2.10 |
| NGC 5286 | $0.333 \pm 0.008$ | 22 | $0.656 \pm 0.017$ | 30 | 0.42 | -1.69 |
| NGC 7078 | $0.369 \pm 0.006$ | 45 | $0.648 \pm 0.008$ | 50 | 0.40 | -2.37 |
| Total | $0.356 \pm 0.004$ | 111 | $0.651 \pm 0.007$ | 111 | 0.44 | $[-2.40,-1.70]$ |
| UFD+dSph |  |  |  |  |  |  |
| Bootes | $0.366 \pm 0.021$ | 5 | $0.684 \pm 0.032$ | 7 | 0.38 | -2.55 |
| Canes Venaticorum I | $0.378 \pm 0.012$ | 5 | $0.604 \pm 0.006$ | 18 | 0.22 | -1.98 |
| Canes Venaticorum II | 0.358 | 1 | 0.743 | 1 | 0.50 | -2.21 |
| Carina | $0.417 \pm 0.029$ | 17 | $0.634 \pm 0.006$ | 57 | 0.21 | -1.72 |
| Cetus | $0.378 \pm 0.004$ | 107 | $0.613 \pm 0.002$ | 506 | 0.17 | -1.90 |
| Coma Berenices | 0.320 | 1 | 0.670 | 1 | 0.50 | -2.60 |
| Draco | $0.375 \pm 0.006$ | 30 | $0.615 \pm 0.003$ | 214 | 0.11 | -1.93 |
| Hercules | $0.399 \pm 0.002$ | 3 | $0.678 \pm 0.013$ | 6 | 0.33 | -2.41 |
| Leo I | $0.352 \pm 0.007$ | 28 | $0.599 \pm 0.005$ | 136 | 0.17 | -1.43 |
| Leo IV | ... | 0 | $0.655 \pm 0.028$ | 3 | 0.17 | -2.54 |
| Leo T | ... | 0 | 0.603 | 1 | 0.17 | -2.02 |
| Sculptor | $0.336 \pm 0.004$ | 88 | $0.587 \pm 0.007$ | 133 | 0.40 | -1.68 |
| SEGUE 2 | $\cdots$ | 0 | 0.748 | 1 | 0.40 | -2.22 |
| Tucana | $0.353 \pm 0.004$ | 82 | $0.604 \pm 0.004$ | 216 | 0.28 | -1.95 |
| Ursa Major I | $0.402 \pm 0.005$ | 2 | $0.628 \pm 0.032$ | 5 | 0.29 | -2.18 |
| Ursa Major II | $\cdots$ | 0 | 0.780 | 1 | 0.29 | -2.47 |
| Total | $0.362 \pm 0.003$ | 369 | $0.610 \pm 0.001$ | 1306 | 0.21 | [-2.60, -1.40] |
| $\omega$ Cen | $0.359 \pm 0.005$ | 101 | $0.668 \pm 0.013$ | 85 | 0.54 | [-2.00, -0.60] |

## Notes.

${ }^{\text {a }}$ Mean FO and F period (days).
${ }^{\mathrm{b}}$ Ratio between the number of FO $\left(N_{c}\right)$ and the total $\left(N_{a b}+N_{d}+N_{c}\right)$ number of RRLs.
${ }^{c}$ Range in iron abundance covered by the selected stellar systems. Iron abundances for GCs come from the Harris (1996) catalog, while dSphs and UFDs from Kirby et al. (2013), McConnachie (2012), and Fabrizio et al. (2015).
predicted PW relation (theoretical, see Table 8 of Marconi et al. 2015).

Using the metal-independent semi-empirical calibrations obtained using the observed slopes and the predicted zero-points
(Marconi et al. 2015) we found that the distance modulus to $\omega$ Cen (see also Table 9) ranges from $13.74 \pm 0.08$ (statistical) $\pm 0.01$ (systematic) mag (FO) to $13.69 \pm 0.08 \pm 0.01 \mathrm{mag}$ (F) and to $13.71 \pm 0.08 \pm 0.01 \mathrm{mag}$ (global). The statistical error


Figure 11. Panel (a): Bailey diagram of the RRLs in the two OoIII/Oo0 metal-rich GGCs NGC 6388 and NGC 6441. Panel (b): comparison between the period distribution of RRLs plotted in panel (a) (black shaded area) and in $\omega$ Cen (red shaded area). The mean periods of RRab and RRc and the population ratio (number of RRc over the total number of RRLs) of the two GCs are also labeled. Panels (c) and (d): same as (a) and (b), but for OoI GGCs with more than 35 RRLs. Panels (e) and (f): same as (a) and (b), but for OoInt GGCs with more than 35 RRLs. Panels (g) and (h): same as (a) and (b), but for OoII GGCs with more than 35 RRLs. Panels (i) and (j): same as (a) and (b), but for dwarf spheroidals (dSph) and ultra-faint dwarf (UFD) galaxies.
is the dispersion of the distribution of the distance moduli of individual RRLs. The systematic error is the difference between the theoretical and the semi-empirical calibration of the $\operatorname{PW}(V, B-$ $I)$ relations. The current estimates agree within $1 \sigma$ and the mean weighted distance modulus is $13.71 \pm 0.08 \pm 0.01 \mathrm{mag}$. We estimated the distance modulus using also theoretical calibration and we found $13.74 \pm 0.08 \pm 0.01 \mathrm{mag} \quad$ (FO), $\quad 13.70 \pm$ $0.08 \pm 0.01 \mathrm{mag}(\mathrm{F})$ and $13.71 \pm 0.08 \pm 0.01 \mathrm{mag}$ (global). The new distance moduli agree with those based on the semiempirical calibration and the mean weighted distance modulus is $13.71 \pm 0.08 \pm 0.01 \mathrm{mag}$.

The distance moduli that we derived agree quite well with similar estimates based on the $K$-band PL relation of RRLs provided by Longmore et al. (1990) ( 13.61 mag ), Sollima et al. (2006b) ( 13.72 mag ), (Bono et al. 2008b) ( $13.75 \pm 0.11 \mathrm{mag}$ ), Del Principe et al. (2006) ( $13.77 \pm 0.07 \mathrm{mag}$ ), and Navarrete et al. (2016) ( $13.70 \pm 0.03 \mathrm{mag}$ ).

A similar remarkable agreement is also found when comparing the current distance moduli with those based on the TRGB provided by Bellazzini et al. (2004) ( $13.70 \pm 0.11 \mathrm{mag}$ ) and by Bono et al. (2008b) ( $13.65 \pm 0.09 \mathrm{mag}$ ). The current estimates also agree within $1 \sigma$ with both distance moduli provided by

Table 7
Empirical $I$-band Period-Luminosity Relations of the Form $M_{I}=a+b \log P$ for $\omega$ Cen RRLs

| $a^{\mathrm{a}}$ <br> $(\mathrm{mag})$ | $\mathrm{b}^{\mathrm{a}}$ <br> $(\mathrm{mag})$ | $\sigma^{\mathrm{a}}$ <br> $(\mathrm{mag})$ | $\mathrm{a}^{\mathrm{b}}$ <br> $(\mathrm{mag})$ | $\mathrm{b}^{\mathrm{b}}$ <br> $(\mathrm{mag})$ | $\sigma^{\mathrm{b}}$ <br> $(\mathrm{mag})$ | $\mathrm{a}^{\mathrm{c}}$ <br> $(\mathrm{mag})$ | $\mathrm{b}^{\mathrm{c}}$ <br> $(\mathrm{mag})$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | RRc |  |  | RRab |  |  |  |
| 13.252 | -1.624 | 0.058 | 13.485 | -1.955 | 0.078 | $\sigma^{\mathrm{c}}$ |  |
| $\pm 0.047$ | $\pm 0.105$ |  | $\pm 0.026$ | $\pm 0.129$ |  | 13.563 |  |

## Notes.

${ }^{\text {a }}$ Zero-point (a), slope (b) and standard deviation ( $\sigma$ ) for first overtone (RRc) variables. The errors on the zero-point and on the slope are listed in the second row.
${ }^{\mathrm{b}}$ Zero-point (a), slope (b) and standard deviation $(\sigma)$ for fundamental (RRab) variables. The errors on the zero-point and on the slope are listed in the second row. ${ }^{c}$ Zero-point (a), slope (b) and standard deviation ( $\sigma$ ) for the global RRL sample (All). The periods of RRc variables were fundamentalized by adopting $\log P_{\mathrm{F}}=\log P_{\mathrm{FO}}+0.127$. The errors on the zero-point and on the slope are listed in the second row.

Kaluzny et al. (2007) using cluster eclipsing binaries-namely $\mu$ $=13.49 \pm 0.14$ and $\mu=13.51 \pm 0.12$ mag-and with the kinematic distance to $\omega$ Cen provided by van de Ven et al. (2006, $\mu=13.75 \pm 0.13 \mathrm{mag})$. The kinematic distance method applied to GCs is a very promising and independent primary distance indicator based on the ratio between the dispersions in proper motion and in radial velocity of cluster stars. The key advantage of this diagnostic is that its accuracy is only limited by the precision of the measurements and by the sample size (King \& Anderson 2002). The above difference seems to suggest the possible unrecognized systematic errors. The reader interested in a more detailed discussion concerning the different diagnostics adopted to estimate cluster distances is referred to Bono et al. (2008b).

Note that we are not providing independent distance estimates to $\omega$ Cen using the zero-point based on the five field RRLs for which trigonometric parallaxes are available (Benedict et al. 2011). The reason is twofold: (a) preliminary empirical evidence based on optical, NIR and MIR measurements indicates that their individual distances might require a mild revision (J. Neeley et al. 2016, in preparation); (b) we plan to address on a more quantitative basis the accuracy of $\omega$ Cen distance, using optical, NIR and MIR mean magnitudes of RRLs (V. F. Braga et al. 2016, in preparation).

## 8. METALLICITY OF RRLS STARS

Dating back to the spectroscopic surveys of giant stars by Norris et al. (1996) and Suntzeff \& Kraft (1996), we have clear and quantitative evidence that $\omega$ Cen hosts stellar populations characterized by a broad spread in iron abundances. More recently, Fraix-Burnet \& Davoust (2015), by analyzing the abundances provided by Johnson \& Pilachowski (2010), confirmed the presence of three main populations as originally suggested by Norris \& Da Costa (1995), Smith et al. (2000), Pancino et al. (2002), and Vanture et al. (2002). The general accepted scenario is that of a globular with a dominant metalpoor primordial population $(-2.0<[\mathrm{Fe} / \mathrm{H}]<-1.6)$ plus a metal-intermediate $(-1.6<[\mathrm{Fe} / \mathrm{H}]<-1.3)$ and a relatively metal-rich $(-1.3<[\mathrm{Fe} / \mathrm{H}]<-0.5$ ) population. The reader is also referred to Calamida et al. (2009) for a detailed discussion concerning the spread in iron abundance based on the Stroemgren metallicity index for a sample of $\sim 4000$ stars.

To further constrain the plausibility of the theoretical framework adopted to estimate the distances and to validate the current metallicity scale we compared theory and observations in the $\log P-I$ plane. Figure 15 shows the predicted $I$-band empirical PL relation at different iron abundances (see labeled values) together
with $\omega$ Cen RRLs. Note that the objects for which iron abundance estimates are available (R00, S06) were plotted using a color code: more metal-poor ( $[\mathrm{Fe} / \mathrm{H}]<-1.7$ ) RRLs are marked with light blue (RRc) and red (RRab), and more metal-rich ([Fe/ $\mathrm{H}]>-1.7$ ) with blue (RRc) and violet (RRab). The adopted iron values are based on the $\mathrm{R} 00+\mathrm{S} 06$ homogenized sample, listed in column 4 of Table 10. The data in this figure display two interesting features worth being discussed.
(i) The predicted PL relation at different iron abundances and the observed range in iron abundance of RRLs agree quite well, and indeed the former bracket the bulk $(\sim 80 \%)$ of the RRL sample. Moreover, there is mild evidence of a ranking in metallicity; indeed more metal-rich RRLs appear, on average, fainter than metal-poor ones. This applies to both RRab ( $\Delta I_{\text {poor-rich }} \sim 0.15 \mathrm{mag}$ ) and to RRc ( $\left.\Delta I_{\text {poor-rich }} \sim 0.09 \mathrm{mag}\right)$ variables.
(ii) Blazhko variables are mostly located between RRc and RRab variables. Moreover, they also appear to be more associated with more metal-poor (14) than with more metalrich (11) RRLs, the ratio being 1.27 . The trend is similar to non-Blazhko RRLs, for which the more metal-poor sample (78) is even larger than the more metal-rich one (50, the ratio is 1.56). Note that we did not take account of RRLs for which iron abundance is not available ( 35 non-Blazhko and three Blazhko RRLs). It is clear that $\omega$ Cen is the right laboratory to delineate the topology of the instability strip, due to sample size and the broad spread in iron abundance. Its use is currently hampered by the lack of accurate and precise elemental abundances for the entire RRL sample.

On the basis of the above empirical evidence, we decided to take advantage of the accuracy of the distance modulus to $\omega$ Cen and of the sensitivity of the I-band PL relation to provide a new estimate of the iron abundance of individual RRLs. A similar approach was adopted by Martínez-Vázquez et al. (2015) and by Coppola et al. (2015) to estimate the metallicity distribution of RRLs in Sculptor and in Carina, respectively. The absolute $I$-band magnitudes ( $M_{I}$ ) of RRLs were estimated using the true distance modulus ( $\mu=13.70 \pm 0.02 \mathrm{mag}$ ) based on theoretical PW relations (see Section 7). In particular, $M_{I}=I-A_{I}-\mu$, where $\mu$ is the true distance modulus and $A_{I}$ the selective absorption in the $I$-band. We adopted, according to Thompson et al. (2001) and Lub (2002), a cluster reddening of $E(B-V)=0.11$ mag. We also took account of the spread in $E(B-V)$ measured by Moni Bidin et al. (2012). According to the reddening law provided by Cardelli et al. (1989), we adopted a ratio $A_{I} / A_{V}=0.590$. Note that the current value accounts for the current photometric system (see for more details Section 6.2).


Figure 12. Left: empirical I-band PL relation for $\omega$ Cen RRLs. Light blue and red squares mark RRc and RRab variables. The light blue and red lines display the linear fits, while the vertical bars show the standard deviations, $\sigma$, of the fits. The number of variables adopted in the fits are also labeled. Right: same as left, but for the global (RRc+RRab) RRL sample. The periods of RRc variables were fundamentalized using $\log P_{\mathrm{F}}=\log P_{\mathrm{FO}}+0.127$.

Finally, theoretical I-band PLZ relations for F and FO pulsators were inverted to estimate the metallicities of $\omega$ Cen RRLs:

$$
\begin{equation*}
[\mathrm{Fe} / \mathrm{H}]=\frac{M_{I}-b \log P-a}{c} \tag{2}
\end{equation*}
$$

where $a, b$, and $c$ are the zero-point, the slope, and the metallicity coefficient of the predicted PLZ relations in the form $M_{I}=a+b \log P+c[\mathrm{Fe} / \mathrm{H}]$. The values of the coefficients $a, b$, and $c$ are listed in Table 6 of Marconi et al. (2015). Note that we adopted this relation because theory and observations indicate that PL relations are less prone to systematic uncertainties introduced by a spread in stellar mass and/or in stellar luminosity due to evolutionary effects (Bono et al. 2001; Bono 2003). To estimate the iron abundance, we only took into account RRLs with photometric error in the $I$ band smaller than 0.1 mag . To provide a homogeneous metallicity scale for $\omega$ Cen the above estimates (solar iron abundance in number $\log \epsilon_{\mathrm{Fe}_{\odot}}=7.50$, Pietrinferni et al. 2006; Marconi et al. 2015) were rescaled to the homogeneous cluster metallicity scale provided by Gratton et al. (2003) and Carretta et al. (2009) ( $\log \epsilon_{\mathrm{Fe}_{\odot}}=7.54$ ).

The metallicity distribution based on 160 RRLs is plotted in Figure 16 as a black shaded area together with the metallicity distribution based on iron abundances provided by R00 and by S06 (red shaded area). We fit the two iron distributions with a Gaussian and we found that current distribution is slightly more metal-poor; indeed the difference in the peaks is $\Delta[\mathrm{Fe} / \mathrm{H}]=$ 0.09 . The $\sigma$ of the current distribution is larger- 0.36 versus 0.27 -than the literature value. The difference is mainly caused by the fact that the iron distribution based on S06 and R00 abundances displays a sharp cut-off at $[\mathrm{Fe} / \mathrm{H}] \sim-2.3$, while the current one attains iron abundances that are 0.5 dex more metal-poor. We double checked the objects located in the
metal-poor tail. Nine out of twelve are RRc stars and we found that they mainly belong to the brighter group. There is also marginal evidence for a slightly more extended metal-rich tail, but the difference is caused by a few objects.

In passing, we note that the metal-poor tail is only marginally supported by both spectroscopic and photometric investigations based on cluster red giant stars. Indeed, Calamida et al. (2009), using Stroemgren photometry for $\sim 4000$ red giants, found that the metallicity distribution can be fit with seven Gaussians. Their peaks range from $[\mathrm{Fe} /$ $\mathrm{H}] \sim-1.7$ to $[\mathrm{Fe} / \mathrm{H}] \sim+0.2$. A similar result was also obtained by Johnson \& Pilachowski (2010) using highresolution spectra of 855 red giants, suggesting iron abundances ranging from $[\mathrm{Fe} / \mathrm{H}] \sim-2.3$ to $[\mathrm{Fe} / \mathrm{H}] \sim-0.3$ (see also Fraix-Burnet \& Davoust 2015).

As a consequence of the reasonable agreement in the iron distributions, we applied to the current iron distribution the difference in the main peaks and provided a homogeneous metallicity scale. For the objects in common with $\mathrm{R} 00+\mathrm{S} 06$ we computed a mean weighted iron abundance and the final values are listed in column 6 of Table 10.

It is worth mentioning that the current approach to estimate RRL iron abundances depends on the adopted distance modulus. A modest increase of 0.05 mag in the true distance modulus implies a systematic shift of $\sim 0.30$ dex in the peak of the metallicity distribution. However, the current approach is aimed at evaluating the relative and not the absolute difference in iron abundance. This means that we are mainly interested in estimating either the spread (standard deviation) in iron abundance or the possible occurrence of multiple peaks in the metallicity distribution (Martínez-Vázquez et al. 2015).

## 9. SUMMARY AND FINAL REMARKS

We present new, accurate, and homogeneous optical, multi-band-UBVRI—photometry of the Galactic globular cluster $\omega$


Figure 13. Panel (a): empirical dual-band period-Wesenheit $(\mathrm{PW})(V, B-V)$ relation for $\omega$ Cen RRLs. Light blue and red squares mark RRc and RRab variables. The light blue and red lines display the linear fits, while the vertical bars show the standard deviations, $\sigma$, of the fits. The number of variables adopted in the fits are also labeled. Panel (b): same as panel (a), but for the global (RRc+RRab) RRL sample. The periods of RRc variables were fundamentalized using $\log P_{\mathrm{F}}=\log P_{\mathrm{FO}}+0.127$. Panels (c) and (d): same as (a) and (b), but for the PW(I, $B-I$ ) relation. Panels (e) and (f): same as (a) and (b), but for the PW( $I$, $V-I$ ) relation. Panels (g) and (h): same as (a) and (b), but for the triple-band PW(V,B-I) relation.

Cen. We collected 8202 CCD images that cover a time interval of 24 years and a sky area of $84 \times 48$ arcmin across the cluster center. The bulk of these images were collected with the Danish telescope at ESO La Silla as time-series data in three main long runs (more than 4500 images). The others were collected with several telescopes ranging from the 0.9 m at CTIO to the VLT at ESO Cerro Paranal. The final photometric catalog includes more than 180,000 (Danish) and 665,000 (other) stars with at least one measurement in two different photometric bands. The above data sets were complemented with optical time series photometry for RRLs available in the
literature. The global photometric catalog allowed us to accomplish the following scientific goals.
Homogeneity. We provide new, homogeneous pulsation parameters for 187 candidate $\omega$ Cen RRLs. All in all the photometry we collected (proprietary+literature) covers a time interval of 36 years and the light curves of RRLs have a number of phase points per band that ranges from $\sim 10-40(U)$, to $\sim 20-770(B)$, to $\sim 20-2830(V)$, to $\sim 10-280(R)$ and to $\sim 10-445$ (I). These numbers sum up to more than 300,000 multi-band phase points for RRLs, indicating that this is the largest optical photometric survey ever performed for cluster

Table 8
Empirical Optical Period-Wesenheit Relations for $\omega$ Cen RRLs

| PW ${ }^{\text {a }}$ | $\zeta^{\text {b }}$ | $\begin{gathered} \mathrm{a}^{\mathrm{c}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \mathrm{b}^{\mathrm{c}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \sigma^{\mathrm{c}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \mathrm{a}^{\mathrm{d}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \mathrm{b}^{\mathrm{d}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \sigma^{\mathrm{d}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \mathrm{a}^{\mathrm{e}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \mathrm{b}^{\mathrm{e}} \\ (\mathrm{mag}) \end{gathered}$ | $\begin{gathered} \sigma^{\mathrm{e}} \\ (\mathrm{mag}) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | RRc |  |  | RRab |  |  | All |  |
| Dual-band PW Relations |  |  |  |  |  |  |  |  |  |  |
| $V, B-V$ | 3.06 | 12.242 | -2.750 | 0.136 | 12.622 | -2.919 | 0.122 | 12.670 | -2.574 | 0.132 |
|  |  | $\pm 0.110$ | $\pm 0.243$ |  | $\pm 0.041$ | $\pm 0.204$ |  | $\pm 0.031$ | $\pm 0.112$ |  |
| $I, B-I$ | 0.78 | 12.070 | -2.734 | 0.081 | 12.460 | -2.868 | 0.075 | 12.511 | -2.503 | 0.079 |
|  |  | $\pm 0.065$ | $\pm 0.144$ |  | $\pm 0.025$ | $\pm 0.124$ |  | $\pm 0.019$ | $\pm 0.068$ |  |
| $I, V-I$ | 1.38 | 11.990 | -2.765 | 0.093 | 12.442 | -2.658 | 0.086 | 12.460 | -2.443 | 0.089 |
|  |  | $\pm 0.074$ | $\pm 0.165$ |  | $\pm 0.030$ | $\pm 0.149$ |  | $\pm 0.021$ | $\pm 0.077$ |  |
|  | Triple-band PW Relations |  |  |  |  |  |  |  |  |  |
| $V, B-I$ | 1.34 | 12.120 | -2.725 | 0.083 | 12.514 | -2.844 | 0.079 | 12.561 | -2.486 | 0.084 |
|  |  | $\pm 0.067$ | $\pm 0.147$ |  | $\pm 0.026$ | $\pm 0.131$ |  | $\pm 0.020$ | $\pm 0.071$ |  |

Notes.
${ }^{\text {a }}$ PW relations of the form: $W(X, Y-Z)=a+b \log P$, where $W(X, Y-Z)=X+\left(A_{X} /\left(A_{Y}-A_{Z}\right)\right)(Y-Z)$ is the Wesenheit magnitude. $Z \neq X$ only for tripleband relations.
${ }^{\mathrm{b}}$ Color coefficient in Wesenheit magnitude: $\zeta=A_{X} /\left(A_{Y}-A_{Z}\right)$.
${ }^{\mathrm{c}}$ Zero-point (a), slope (b) and standard deviation ( $\sigma$ ) for first overtone ( RRc ) variables. The errors on the zero-point and on the slope are listed in the second row.
${ }^{\mathrm{d}}$ Zero-point (a), slope (b) and standard deviation ( $\sigma$ ) for fundamental (RRab) variables. The errors on the zero-point and on the slope are listed in the second row.
${ }^{\mathrm{e}}$ Zero-point (a), slope (b) and standard deviation $(\sigma)$ for for the global RRL sample (All). The periods of RRc variables were fundamentalized by adopting $\log P_{\mathrm{F}}=\log P_{\mathrm{FO}}+0.127$. The errors on the zero-point and on the slope are listed in the second row.


Figure 14. $V$ vs. $[\mathrm{Fe} / \mathrm{H}]$ distribution of $\omega$ Cen RRLs. We adopted iron abundances available in the literature (Rey et al. 2000; Sollima et al. 2006a) rescaled into the Carretta et al. (2009) metallicity scale. The vertical error bars display errors in the mean visual magnitude, while the horizontal ones display either the intrinsic error (single measurement) or the standard deviation (two measurements). See the text for more details.

RRLs (Jurcsik et al. 2012, 2015). The above data allowed us to provide new and accurate estimates of their pulsation parameters (mean magnitudes, luminosity variation amplitudes, epoch of maximum, and epoch of mean magnitude).

Period distribution. The key advantage in dealing with $\omega$ Cen is that its RRL sample is the third largest after M3 (237 RRLs) and M62 (217) among the globulars hosting RRLs. On the basis of the current analysis we ended up with a sample of 187 candidate cluster RRLs; among them, 101 pulsate in the first overtone (RRc), 85 in the fundamental (RRab) mode, and a single object is a candidate mixed-mode variable (RRd). We estimated the mean periods for RRab and RRc variables and found that they are $\left\langle P_{a b}\right\rangle=0.668$ days, $\left\langle P_{c}\right\rangle=0.359$ days. The above mean periods and the population ratio, i.e., the ratio between the number of RRc and the total number of RRLs $\left(N_{c} /\left(N_{a b}+N_{d}+N_{c}\right)\right)$, support previous findings suggesting that $\omega$ Cen is an OoII cluster.

Bailey diagram. The luminosity variation amplitude versus period plane indicates a clear lack of HASP RRLs, i.e., RRab
variables with $P \lesssim 0.48$ days and $A V>0.75 \mathrm{mag}$ (Fiorentino et al. 2015). These objects become more popular in stellar systems more metal-rich than $[\mathrm{Fe} / \mathrm{H}] \approx-1.4$, thus suggesting that RRLs in $\omega$ Cen barely approach this metallicity range. The RRab variables that, from our investigation, appear to be more metal-rich than -1.4 , have periods ranging from 0.49 to 0.72 days.

Moreover, we also found evidence that RRc can be split into two different groups: (a) short-period-with periods ranging from $\sim 0.30$ to $\sim 0.36$ days and visual amplitudes ranging from a few hundreths of a magnitude to a few tenths; (b) long-period -with periods ranging from $\sim 0.36$ to $\sim 0.45$ days and amplitudes clustering around $A V \sim 0.5$ mag. Theoretical and empirical arguments further support a well defined spread in iron abundance.

Amplitude ratios. The well known spread in iron abundance of $\omega$ Cen stars makes its RRL sample a fundamental test-bench to characterize the possible dependence of amplitude ratios on metal content. We performed a detailed test and found that both RRab and RRc attain similar ratios: $A B / A V=1.26 \pm 0.01$; $A R / A V=0.78 \pm 0.01 ; A I / A V=0.63 \pm 0.01$. Moreover, they do not display any clear trend with iron abundance.

Visual magnitude distribution. We performed a detailed analysis of the visual magnitude distribution of RRLs and we found that they can be fit with four Gaussians. The two main peaks included a significant fraction of RRL ( $\sim 76 \%$ ) and attain similar magnitudes ( $V \sim 14.47,14.56 \mathrm{mag}$ ). The fainter ( $V$ $\sim 14.71 \mathrm{mag})$ and the brighter ( $V \sim 14.31 \mathrm{mag}$ ) peak include a minor fraction $(11 \%, 13 \%)$ of the RRL sample. The above finding is suggestive of a spread in iron abundance of the order of 1.5 dex and paves the way for new solid estimates on the absolute age of the different stellar populations in $\omega$ Cen.

Blazhko RRLs. Empirical evidence based on the location of candidate Blazhko RRLs in the Bailey diagram and in the CMD clearly indicates that they are located between RRc and RRab variables. Indeed, we found that a significant fraction (79\%) of them ( 22 out of 28 ) have periods shorter than 0.6 days. Moreover, their location inside the instability strip indicates that a significant fraction (39\%) of them belongs to

Table 9
True Distance Moduli to $\omega$ Cen: Literature and Current Estimates

| $\mu_{0}$ <br> $(\mathrm{mag})$ | $E(B-V)^{\mathrm{a}}$ <br> $(\mathrm{mag})$ | Reference |
| :--- | :--- | :--- | :--- |
| 13.61 | 0.11 | Notes ${ }^{\mathrm{b}}$ |
| $13.65 \pm 0.12$ | 0.13 | Longmore et al. (1990) |
| $13.70 \pm 0.11$ | $0.11 \pm 0.01$ | Thompson et al. (2001) |
| $13.77 \pm 0.07$ | $0.11 \pm 0.01$ | Bellazzini et al. (2004) |
| 13.72 | $0.11 \pm 0.01$ | Del Principe et al. (2006) |
| $13.75 \pm 0.13$ | 0.11 | Sollima et al. (2006b) |
| $13.49 \pm 0.14 / 13.51 \pm 0.12$ | 0.131 | van de Ven et al. (2006) |
| $13.65 \pm 0.09$ | $0.11 \pm 0.02$ | Kaluzny et al. (2007) |
| $13.75 \pm 0.11$ | $0.11 \pm 0.02$ | Bono et al. (2008b) |
| $13.70 \pm 0.03$ | 0.12 | Bono et al. (2008b) |
| $13.71 \pm 0.08 \pm 0.01$ | $\ldots$ | Navarrete et al. (2016) |
| $13.71 \pm 0.08 \pm 0.01$ | $\ldots$ | This paper |

## Notes.

${ }^{\text {a }}$ Reddening toward $\omega$ Cen adopted in distance determinations. (1): Buonanno et al. (1989), (2, 5): Schlegel et al. (1998), (3, 4): Lub (2002), (6, 7): Kaluzny et al. (2002); Calamida et al. (2005), (8, 9): This paper.
${ }^{\text {b }}$ (1) Longmore et al. (1990) derived $\mu$ using the $K$-band PL relation. They calibrated the relation by adopting $M_{K, o,-0.3}=0.06[\mathrm{Fe} / \mathrm{H}]-0.24$, where $M_{K, o,-0.3}$ is the reddening-corrected $K$ magnitude at $\log P=-0.3$. (2) Thompson et al. (2001) used the surface brightness method applied to the detached eclipsing binaryOGLEGC 17-to derive the absolute distance to $\omega$ Cen. They found $d=5360 \pm 300 \mathrm{pc}$. (3) Bellazzini et al. (2004) using a new calibration of the Tip of the Red Giant Branch (TRGB) in the $I J H K$ bands as a function of the global metallicity [M/H]. (4) Distance modulus to $\omega$ Cen derived by Del Principe et al. (2006) using the semi-empirical calibration of the $K$-band PL relation by Bono et al. (2003a). (5) Distance modulus to $\omega$ Cen derived by Sollima et al. (2006b) using a new calibration of the $K$-band PL relation. Their zero-point is based on the trigonometric parallax of the prototype RR Lyr (Benedict et al. 2011)). (6) Distance to $\omega$ Cen derived by constructing axisymmetric dynamical models of the cluster. The models were fitted to the proper motion and radial velocity measurements to provide an estimate of the distance ( $4.8 \pm 0.3 \mathrm{kpc}$ ). (7) Distance to $\omega$ Cen estimated by Kaluzny et al. (2007) using the detached eclipsing binary (V209). The two distance moduli are for the primary (closest) and for the secondary (farthest) star of the binary system. (8,9) Distances to $\omega$ Cen estimated by Bono et al. (2008b), using the calibration of the TRGB provided by Lee et al. (1993). The latter estimate is based on the empirical $K$-band PL relation provided by (Sollima et al. 2008). (10) Distance modulus to $\omega$ Cen derived by Navarrete et al. (2016) using the $J$ - and $K$-band PL relations (Alonso-García et al. 2015) for both RRLs and Type II Cepheids. (11, 12) Distances to $\omega$ Cen based on the current semi-empirical and theoretical calibration of the reddening independent $\mathrm{PW}(V, B-I)$ relations. See the text (Section 7 ) for more details.
the fainter peak ( $V \geqslant 14.6 \mathrm{mag}$ ), thus suggesting that this subsample is more associated with the more metal-rich stellar component.

Oosterhoff dilemma. Dating back to the seminal investigation by Oosterhoff (1939) in which he recognized that cluster RRLs can be split, according to their mean periods, into two different groups, the astronomical community undertook a paramount observational effort in order to constrain the physical mechanism(s) driving the empirical evidence. We performed a detailed comparison between the period distribution and the Bailey diagram of $\omega$ Cen RRLs with globulars hosting a sizable sample ( $>35$ ) of RRLs and with RRLs in nearby dSphs and UFDs. We found, as expected, that the mean F and FO periods display a steady decrease when moving from the more metal-rich (Oosterhoff I) to the more metal-poor (Oosterhoff II) clusters. In this context dSphs and UFDs attain values that are intermediate between the OoInt and the OoII clusters, while $\omega$ Cen appears as the upper envelope of the distribution. On the other hand, the population ratio $-N_{c} /\left(N_{a b}+N_{d}+N_{c}\right)$-has a nonlinear trend, since it attains a well defined minimum for OoInt clusters. In spite of the possible differences, the iron abundance appears to be the key parameter in driving the transition from short mean period to long mean period stellar systems. The above results do not support the working hypothesis that $\omega$ Cen is the core remnant of a dwarf galaxy (Bekki \& Freeman 2003). Moreover, there is mounting empirical evidence that cluster RRLs might not be the appropriate sample to address the Oosterhoff dichotomy, since they might be either biased by statistics or affected by environmental effects.
$\omega$ Cen disguised as a dwarf galaxy. The number of globulars hosting long-period ( $0.82-0.85 \lesssim P \lesssim 1$ days) RRLs is quite limited. Three honorable exceptions are $\omega$ Cen and the two metal-rich bulge globulars, namely NGC 6388 and NGC 6441. The mean periods of the metal-rich clusters appear as an extreme case of OoI clusters. This is the reason why we suggest they should be classified as Oosterhoff type 0 instead of Oosterhoff type III. We note that the main common feature among these clusters is that the HB luminosity function shows a well developed blue tail. This indicates that the appearance of long-period RRLs is more from nurture than nature. The environment, and in particular the high central stellar density, might play a crucial role in the presence of a blue tail and, in turn, of long-period RRLs. However, the observational scenario appears much more complex, since the RRLs in the metal-intermediate cluster NGC 2808 host 11 RRab variables, but they have periods shorter than 0.62 days (Kunder et al. 2013a).

Distance determination. We took advantage of optical PW relations that are reddening independent by construction and minimally dependent on iron abundance to provide new estimates of the distance to $\omega$ Cen. We adopted both a semiempirical and a theoretical calibration and we found a true distance modulus of $13.71 \pm 0.08 \pm 0.01$ mag. These agree quite well with similar estimates available in the literature. In particular, we found that the agreement is within $1 \sigma$ with the geometrical distances based on eclipsing binaries ( $13.49 \pm 0.14 / 13.51 \pm 0.12$, Kaluzny et al. 2007)

Metallicity distribution. We inverted the I-band PLZ relation for F and FO pulsators to provide individual metallicity estimates for 160 cluster RRLs. We found that the metallicity


Figure 15. Left: empirical $I$-band PL relation for $\omega$ Cen RRLs. Light blue circles and red squares mark variables more metal-poor than $[\mathrm{Fe} / \mathrm{H}]=-1.7$, while blue circles and violet squares mark variables more metal-rich than $[\mathrm{Fe} / \mathrm{H}]=-1.7$. Candidate Blazhko stars are marked with a black cross. The black lines display the predicted (Marconi et al. 2015) I-band PLZ relation for F (solid) and FO pulsators at fixed metal abundance $[\mathrm{Fe} / \mathrm{H}]=-2.4$ (brighter) and $[\mathrm{Fe} / \mathrm{H}]=-1.3$ (fainter). Right: same as left, but for the global (RRc+RRab) RRL sample. The periods of RRc variables were fundamentalized using $\log P_{\mathrm{RRab}}=\log P_{\mathrm{RRc}}+0.127$.
distribution agrees quite well with the metallicity distribution of RRLs based on spectroscopic measurements (74, S06) and on photometric indicators (131, R00). We also found evidence of a metal-poor tail that is not present in previous spectroscopic investigations of $\omega$ Cen RRLs.
The current long-term photometric surveys are providing new and homogeneous measurements concerning field and cluster stars. The current status is going to experience a quantum jump as soon as the ongoing (Gaia) and near-future ground-based experiments will release their data. The project we started more than 15 years ago on $\omega$ Cen may be defined as a local survey. The number of optical images adopted to individuate main sequence and evolved variable stars have been discussed in detail in Section 2. In dealing with the Danish data set we analyzed 4539 images and we performed $\approx 2.5 \times 10^{8}$ measurements, which means roughly 55,000 stars per image. In dealing with all the other optical data sets we analyzed 3663 images and performed $\approx 1.1 \times 10^{8}$ measurements, which means roughly 27,000 stars per image. A similar number of measurements have been also performed in dealing with NIR images. The above numbers indicate, after accounting for the preliminary steps in approaching the final photometric catalog, that we are dealing with an experiment that included more than one giga measurement. The results concerning variable and static stars will be addressed in a series of future papers in which we plan to use homogeneous multiband optical, NIR, and MIR photometry.

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## APPENDIX <br> NOTES ON INDIVIDUAL RRLs STARS

V4, V25, V44, V88, V90, V91, V271, V272, V273, V276, NV340, NV341, NV349, NV350, NV352. We estimate the pulsation parameters neglecting either the danish95 and/or the danish98 and/or the danish99 data sets, since they are noisy.

V5, V9, V11, V56, V67, V69, V74, V106, V112, V115, V120, V130, V140, V141. We confirm the Blazhko modulations suggested by Kaluzny et al. (2004) and Weldrake et al. (2007) and provide preliminary estimates of $B$ - and/or $V$-band Blazhko amplitudes (see Table 3).

V10, V24, V32, V47, V58, V64, V70, V71, V77, V81, V82, V87, V89, V95, V123, V124, V126, V131, V136, V145, V147, V153, V155, V156, V157, V158, V166, V270, V275, V289, NV340, NV346, NV347, NV353, NV354. There is mild evidence of a period change.

V11, V94. There is evidence that these variables might be affected by a phase shift. Owing to these variations, the $B$ - and $V$-band mean magnitudes and amplitudes are based either on the danish 95 or on the OGLE data set.

V22, V30, V32, V94, V261, V275, V280, V291. The current photometry suggests that these objects are new candidate Blazhko variables. The current data do not allow us to support the multi-modality for V261, suggested by Kaluzny et al. (2004) and/or possible variations in the pulsation period. The variables V280 and V291 sow also evidence for a secondary modulations and/or for a phase shift.

V45, V165. Candidate Blazhko variable according to Kaluzny et al. (2004). The current light curves, based only

Table 10
Metallicity Estimates ( $[\mathrm{Fe} / \mathrm{H}]$ ) of Candidate $\omega$ Cen RRLs Based on Spectroscopy (S06) and on Photometric Indices (R00, ours)

| ID | [ $\mathrm{Fe} / \mathrm{H}$ ] |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | S06 ${ }^{\text {a }}$ | Rey ${ }^{\text {b }}$ | S06+Rey ${ }^{\text {c }}$ | PLI ${ }^{\text {d }}$ | $\mathrm{S} 06+\mathrm{Rey}+\mathrm{PLI}^{\text {e }}$ |
| V3 | ... | $-1.54 \pm 0.05$ | $-1.73 \pm 0.05$ | -1.59 | $-1.72 \pm 0.04$ |
| V4 | $\ldots$ | $-1.74 \pm 0.05$ | $-1.95 \pm 0.05$ | -2.24 | $-1.96 \pm 0.08$ |
| V5 | $-1.24 \pm 0.11$ | $-1.35 \pm 0.08$ | $-1.43 \pm 0.17$ | -0.78 | $-1.22 \pm 0.43$ |
| V7 | ... | $-1.46 \pm 0.08$ | $-1.64 \pm 0.08$ | -1.80 | $-1.66 \pm 0.07$ |
| V8 | $\ldots$ | $-1.91 \pm 0.28$ | $-2.13 \pm 0.28$ | -1.49 | $-1.77 \pm 0.45$ |
| V9 | ... | $-1.49 \pm 0.06$ | $-1.67 \pm 0.06$ | -0.70 | $-1.62 \pm 0.31$ |
| V10 |  | $-1.66 \pm 0.10$ | $-1.86 \pm 0.10$ | -1.90 | $-1.87 \pm 0.02$ |
| V11 | $-1.61 \pm 0.22$ | $-1.67 \pm 0.13$ | $-1.81 \pm 0.15$ | -2.09 | $-1.89 \pm 0.18$ |
| V12 | ... | $-1.53 \pm 0.14$ | $-1.71 \pm 0.14$ | -1.71 | $-1.71 \pm 0.00$ |
| V13 | ... | $-1.91 \pm 0.50$ | $-2.13 \pm 0.50$ | -1.71 | $-1.80 \pm 0.23$ |
| V14 | $\ldots$ | $-1.71 \pm 0.13$ | $-1.91 \pm 0.13$ | -1.33 | $-1.79 \pm 0.34$ |
| V15 | $-1.68 \pm 0.18$ | $-1.64 \pm 0.39$ | $-1.72 \pm 0.07$ | -1.74 | $-1.72 \pm 0.01$ |
| V16 | $-1.65 \pm 0.46$ | $-1.29 \pm 0.08$ | $-1.46 \pm 0.05$ | -1.88 | $-1.48 \pm 0.11$ |
| V18 |  | $-1.78 \pm 0.28$ | $-1.99 \pm 0.28$ | -1.90 | $-1.94 \pm 0.06$ |
| V19 | ... | $-1.22 \pm 0.05$ | $-1.37 \pm 0.05$ | ... | $-1.37 \pm 0.05$ |
| V20 | $-1.52 \pm 0.34$ |  | $-1.54 \pm 0.34$ | -1.66 | $-1.62 \pm 0.08$ |
| V21 | ... | $-0.90 \pm 0.11$ | $-1.02 \pm 0.11$ | -1.87 | $-1.16 \pm 0.44$ |
| V22 | $-1.60 \pm 0.99$ | $-1.63 \pm 0.17$ | $-1.82 \pm 0.05$ | -1.51 | $-1.81 \pm 0.09$ |
| V23 | $-1.35 \pm 0.58$ | $-1.08 \pm 0.14$ | $-1.23 \pm 0.05$ | -0.71 | $-1.21 \pm 0.14$ |
| V24 | ... | $-1.86 \pm 0.03$ | $-2.08 \pm 0.03$ | -1.14 | $-2.07 \pm 0.16$ |
| V25 | $\ldots$ | $-1.57 \pm 0.14$ | $-1.76 \pm 0.14$ | -1.88 | $-1.79 \pm 0.07$ |
| V26 | $-1.81 \pm 0.12$ | $-1.68 \pm 0.10$ | $-1.86 \pm 0.04$ | -1.36 | $-1.85 \pm 0.11$ |
| V27 | $-1.16 \pm 0.14$ | $-1.50 \pm 0.26$ | $-1.29 \pm 0.30$ | -1.24 | $-1.26 \pm 0.03$ |
| V30 | $-1.62 \pm 0.28$ | $-1.75 \pm 0.17$ | $-1.87 \pm 0.20$ | -1.65 | $-1.79 \pm 0.15$ |
| V32 |  | $-1.53 \pm 0.16$ | $-1.71 \pm 0.16$ | -1.77 | $-1.73 \pm 0.04$ |
| V33 | $-1.58 \pm 0.42$ | $-2.09 \pm 0.23$ | $-2.16 \pm 0.44$ | -1.66 | $-1.78 \pm 0.30$ |
| V34 | ... | $-1.71 \pm 0.50$ | $-1.91 \pm 0.50$ | -1.72 | $-1.76 \pm 0.11$ |
| V35 | $-1.63 \pm 0.36$ | $-1.56 \pm 0.08$ | $-1.74 \pm 0.03$ | -1.42 | $-1.74 \pm 0.05$ |
| V36 | ... | $-1.49 \pm 0.23$ | $-1.67 \pm 0.23$ | -1.86 | $-1.76 \pm 0.14$ |
| V38 | $-1.64 \pm 0.40$ | $-1.75 \pm 0.18$ | $-1.91 \pm 0.16$ | -1.50 | $-1.79 \pm 0.26$ |
| V39 | $\ldots$ | $-1.96 \pm 0.29$ | $-2.19 \pm 0.29$ | -1.37 | $-1.72 \pm 0.57$ |
| V40 | $-1.62 \pm 0.19$ | $-1.60 \pm 0.08$ | $-1.77 \pm 0.08$ | -1.72 | $-1.77 \pm 0.02$ |
| V41 |  | $-1.89 \pm 0.48$ | $-2.11 \pm 0.48$ | -1.97 | $-2.00 \pm 0.08$ |
| V44 | $-1.29 \pm 0.35$ | $-1.40 \pm 0.12$ | $-1.54 \pm 0.11$ | -0.90 | $-1.44 \pm 0.33$ |
| V45 | ... | $-1.78 \pm 0.25$ | $-1.99 \pm 0.25$ | -1.97 | $-1.98 \pm 0.02$ |
| V46 | $\ldots$ | $-1.88 \pm 0.17$ | $-2.10 \pm 0.17$ | . | $-2.10 \pm 0.17$ |
| V47 | ... | $-1.58 \pm 0.31$ | $-1.77 \pm 0.31$ | -1.16 | $-1.40 \pm 0.42$ |
| V49 | $\ldots$ | $-1.98 \pm 0.11$ | $-2.21 \pm 0.11$ | -1.35 | $-2.07 \pm 0.45$ |
| V50 | ... | $-1.59 \pm 0.19$ | $-1.78 \pm 0.19$ | -1.44 | $-1.65 \pm 0.23$ |
| V51 | $-1.84 \pm 0.23$ | $-1.64 \pm 0.21$ | $-1.85 \pm 0.02$ | -1.75 | $-1.85 \pm 0.01$ |
| V52 | ... | $-1.42 \pm 0.04$ | $-1.59 \pm 0.04$ | -2.40 | $-1.61 \pm 0.18$ |
| V54 | $-1.80 \pm 0.23$ | $-1.66 \pm 0.12$ | $-1.85 \pm 0.02$ | -1.75 | $-1.85 \pm 0.01$ |
| V55 | ... | $-1.23 \pm 0.31$ | $-1.38 \pm 0.31$ | . | $-1.38 \pm 0.31$ |
| V56 | $\ldots$ | $-1.26 \pm 0.15$ | $-1.42 \pm 0.15$ | -0.52 | $-1.18 \pm 0.56$ |
| V57 | ... | $-1.89 \pm 0.14$ | $-2.11 \pm 0.14$ | -2.04 | $-2.09 \pm 0.04$ |
| V58 | $-1.91 \pm 0.31$ | $-1.37 \pm 0.18$ | $-1.64 \pm 0.24$ | -1.78 | $-1.71 \pm 0.10$ |
| V59 | ... | $-1.00 \pm 0.28$ | $-1.13 \pm 0.28$ | -1.54 | $-1.36 \pm 0.29$ |
| V62 | $\ldots$ | $-1.62 \pm 0.29$ | $-1.81 \pm 0.29$ | -2.13 | $-1.99 \pm 0.22$ |
| V63 | $\ldots$ | $-1.73 \pm 0.09$ | $-1.94 \pm 0.09$ | -1.32 | $-1.87 \pm 0.28$ |
| V64 | $\ldots$ | $-1.46 \pm 0.23$ | $-1.64 \pm 0.23$ | -1.66 | $-1.65 \pm 0.01$ |
| V66 | ... | $-1.68 \pm 0.34$ | $-1.88 \pm 0.34$ | -1.61 | $-1.70 \pm 0.18$ |
| V67 | $-1.19 \pm 0.23$ | $-1.10 \pm 0.50$ | $-1.22 \pm 0.02$ | -0.94 | $-1.22 \pm 0.03$ |
| V68 | ... | $-1.60 \pm 0.01$ | $-1.79 \pm 0.01$ | -1.57 | $-1.79 \pm 0.01$ |
| V69 | ... | $-1.52 \pm 0.14$ | $-1.70 \pm 0.14$ | -1.75 | $-1.71 \pm 0.03$ |
| V70 | $-1.74 \pm 0.30$ | $-1.94 \pm 0.15$ | $-2.09 \pm 0.23$ | -1.57 | $-1.85 \pm 0.36$ |
| V71 | $-1.74 \pm 0.28$ |  | $-1.76 \pm 0.28$ | -2.01 | $-1.90 \pm 0.17$ |
| V72 | ... | $-1.32 \pm 0.22$ | $-1.48 \pm 0.22$ | -1.54 | $-1.51 \pm 0.04$ |
| V73 | $\ldots$ | $-1.50 \pm 0.09$ | $-1.68 \pm 0.09$ | -0.95 | $-1.60 \pm 0.33$ |
| V74 | ... | $-1.83 \pm 0.36$ | $-2.05 \pm 0.36$ | -2.18 | $-2.14 \pm 0.09$ |
| V75 | $-1.82 \pm 0.99$ | $-1.49 \pm 0.08$ | $-1.67 \pm 0.02$ | -1.92 | $-1.67 \pm 0.03$ |
| V76 | $\cdots$ | $-1.45 \pm 0.13$ | $-1.63 \pm 0.13$ | -1.93 | $-1.69 \pm 0.17$ |
| V77 | $-1.84 \pm 0.43$ | $-1.81 \pm 0.50$ | $-1.93 \pm 0.11$ | -1.48 | $-1.86 \pm 0.23$ |
| V79 |  | $-1.39 \pm 0.18$ | $-1.56 \pm 0.18$ | -2.37 | $-1.84 \pm 0.54$ |

Table 10
(Continued)

| ID | [ $\mathrm{Fe} / \mathrm{H}$ ] |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | S06 ${ }^{\text {a }}$ | Rey ${ }^{\text {b }}$ | S06+Rey ${ }^{\text {c }}$ | PLI ${ }^{\text {d }}$ | S06+Rey+PLI ${ }^{\text {e }}$ |
| V81 | $-1.99 \pm 0.43$ | $-1.72 \pm 0.31$ | $-1.95 \pm 0.06$ | -1.15 | $-1.91 \pm 0.26$ |
| V82 | $-1.71 \pm 0.56$ | $-1.56 \pm 0.20$ | $-1.75 \pm 0.01$ | -1.91 | $-1.75 \pm 0.01$ |
| V83 | ... | $-1.30 \pm 0.22$ | $-1.46 \pm 0.22$ | -1.73 | $-1.58 \pm 0.19$ |
| V84 | $\ldots$ | $-1.47 \pm 0.10$ | $-1.65 \pm 0.10$ | ... | $-1.65 \pm 0.10$ |
| V85 |  | $-1.87 \pm 0.31$ | $-2.09 \pm 0.31$ | -1.56 | $-1.77 \pm 0.37$ |
| V86 | $-1.99 \pm 0.23$ | $-1.81 \pm 0.18$ | $-2.02 \pm 0.01$ | -1.96 | $-2.02 \pm 0.00$ |
| V87 | ... | $-1.44 \pm 0.19$ | $-1.62 \pm 0.19$ | -1.53 | $-1.59 \pm 0.06$ |
| V88 |  | $-1.65 \pm 0.23$ | $-1.85 \pm 0.23$ | -1.46 | $-1.67 \pm 0.28$ |
| V89 | $-1.66 \pm 0.23$ | $-1.37 \pm 0.28$ | $-1.62 \pm 0.10$ | -0.88 | $-1.52 \pm 0.36$ |
| V90 | $-1.78 \pm 0.31$ | $-2.21 \pm 0.50$ | $-1.98 \pm 0.42$ | -1.16 | $-1.37 \pm 0.51$ |
| V91 | $-1.81 \pm 0.30$ | $-1.44 \pm 0.17$ | $-1.67 \pm 0.13$ | -1.97 | $-1.73 \pm 0.18$ |
| V94 | ... | $-1.00 \pm 0.11$ | $-1.13 \pm 0.11$ | -1.72 | $-1.23 \pm 0.31$ |
| V95 | $\ldots$ | $-1.84 \pm 0.55$ | $-2.06 \pm 0.55$ | ... | $-2.06 \pm 0.55$ |
| V96 | .. | $-1.22 \pm 0.50$ | $-1.37 \pm 0.50$ | -2.12 | $-1.97 \pm 0.43$ |
| V97 | $-1.74 \pm 0.17$ | $-1.56 \pm 0.37$ | $-1.76 \pm 0.01$ | -1.85 | $-1.76 \pm 0.00$ |
| V98 | ... | $-1.05 \pm 0.12$ | $-1.18 \pm 0.12$ | ... | $-1.18 \pm 0.12$ |
| V99 | $-1.91 \pm 0.25$ | $-1.66 \pm 0.14$ | $-1.88 \pm 0.04$ | -2.20 | $-1.89 \pm 0.07$ |
| V100 | ... | $-1.58 \pm 0.14$ | $-1.77 \pm 0.14$ | -1.80 | $-1.78 \pm 0.02$ |
| V101 | ... | $-1.88 \pm 0.32$ | $-2.10 \pm 0.32$ | -1.63 | $-1.81 \pm 0.32$ |
| V102 | $-1.65 \pm 0.16$ | $-1.84 \pm 0.13$ | $-1.90 \pm 0.27$ | -1.58 | $-1.73 \pm 0.23$ |
| V103 | $-1.78 \pm 0.27$ | $-1.92 \pm 0.11$ | $-2.10 \pm 0.17$ | -2.50 | $-2.23 \pm 0.26$ |
| V104 | ... | $-1.83 \pm 0.18$ | $-2.05 \pm 0.18$ | -1.36 | $-1.81 \pm 0.46$ |
| V105 | $\ldots$ | $-1.24 \pm 0.18$ | $-1.39 \pm 0.18$ | -0.94 | $-1.24 \pm 0.30$ |
| V106 | $-1.90 \pm 0.26$ | $-1.50 \pm 0.23$ | $-1.79 \pm 0.17$ | -1.83 | $-1.80 \pm 0.03$ |
| V107 | $\ldots$ | $-1.36 \pm 0.11$ | $-1.53 \pm 0.11$ | -1.13 | $-1.46 \pm 0.21$ |
| V108 | $-1.63 \pm 0.13$ | $-1.93 \pm 0.23$ | $-1.77 \pm 0.31$ | -1.72 | $-1.74 \pm 0.03$ |
| V109 | $-1.70 \pm 0.07$ | $-1.51 \pm 0.25$ | $-1.72 \pm 0.01$ | -1.64 | $-1.72 \pm 0.00$ |
| V110 | $-1.65 \pm 0.52$ | $-2.14 \pm 0.16$ | $-2.33 \pm 0.29$ | -1.51 | $-1.86 \pm 0.57$ |
| V111 | $-1.79 \pm 0.09$ | $-1.66 \pm 0.04$ | $-1.85 \pm 0.03$ | -1.68 | $-1.85 \pm 0.03$ |
| V112 | ... | $-1.81 \pm 0.26$ | $-2.02 \pm 0.26$ | -2.16 | $-2.09 \pm 0.10$ |
| V113 | ... | $-1.65 \pm 0.34$ | $-1.85 \pm 0.34$ | -1.49 | $-1.62 \pm 0.24$ |
| V114 | $-1.61 \pm 0.99$ | $-1.32 \pm 0.30$ | $-1.49 \pm 0.06$ | -1.78 | $-1.51 \pm 0.09$ |
| V115 | $-1.64 \pm 0.32$ | $-1.87 \pm 0.01$ | $-2.09 \pm 0.02$ | -1.78 | $-2.09 \pm 0.03$ |
| V116 | $-1.11 \pm 0.17$ | $-1.27 \pm 0.44$ | $-1.17 \pm 0.14$ | -2.41 | $-1.47 \pm 0.75$ |
| V117 | ... | $-1.68 \pm 0.25$ | $-1.88 \pm 0.25$ | -1.18 | $-1.53 \pm 0.49$ |
| V118 | $-2.04 \pm 0.14$ | $-1.62 \pm 0.23$ | $-1.99 \pm 0.15$ | -2.66 | $-2.17 \pm 0.42$ |
| V119 | ... | $-1.61 \pm 0.10$ | $-1.80 \pm 0.10$ | -2.03 | $-1.83 \pm 0.11$ |
| V120 | $-1.15 \pm 0.16$ | $-1.39 \pm 0.06$ | $-1.51 \pm 0.18$ | -1.24 | $-1.42 \pm 0.18$ |
| V121 | $-1.83 \pm 0.40$ | $-1.46 \pm 0.13$ | $-1.66 \pm 0.09$ | -2.41 | $-1.75 \pm 0.34$ |
| V122 | $-1.79 \pm 0.21$ | $-2.02 \pm 0.18$ | $-2.07 \pm 0.31$ | -1.71 | $-1.85 \pm 0.25$ |
| V123 | ... | $-1.64 \pm 0.01$ | $-1.84 \pm 0.01$ | -0.53 | $-1.84 \pm 0.07$ |
| V124 | $\ldots$ | $-1.33 \pm 0.23$ | $-1.49 \pm 0.23$ | -0.97 | $-1.25 \pm 0.37$ |
| V125 | $-1.81 \pm 0.38$ | $-1.67 \pm 0.22$ | $-1.86 \pm 0.02$ | ... | $-1.86 \pm 0.02$ |
| V126 | ... | $-1.31 \pm 0.13$ | $-1.47 \pm 0.13$ | -1.83 | $-1.55 \pm 0.21$ |
| V127 | ... | $-1.59 \pm 0.08$ | $-1.78 \pm 0.08$ | -1.88 | $-1.79 \pm 0.04$ |
| V128 | $\ldots$ | $-1.88 \pm 0.04$ | $-2.10 \pm 0.04$ | -1.82 | $-2.09 \pm 0.06$ |
| V130 | ... | $-1.46 \pm 0.17$ | $-1.64 \pm 0.17$ | -1.14 | $-1.48 \pm 0.33$ |
| V131 | $-1.66 \pm 0.48$ | $-1.56 \pm 0.20$ | $-1.74 \pm 0.03$ | -1.88 | $-1.74 \pm 0.02$ |
| V132 | ... | $-1.91 \pm 0.20$ | $-2.13 \pm 0.20$ | -2.35 | $-2.22 \pm 0.15$ |
| V134 | $\ldots$ | $-1.80 \pm 0.41$ | $-2.01 \pm 0.41$ | -2.51 | $-2.38 \pm 0.32$ |
| V135 | $-1.57 \pm 0.18$ | $-2.20 \pm 0.50$ | $-1.69 \pm 0.39$ | -2.34 | $-2.15 \pm 0.42$ |
| V136 | $-1.64 \pm 0.37$ | $-1.83 \pm 0.47$ | $-1.81 \pm 0.27$ | -2.27 | $-2.06 \pm 0.33$ |
| V137 |  | $-1.19 \pm 0.18$ | $-1.34 \pm 0.18$ | -1.86 | $-1.52 \pm 0.35$ |
| V139 | $-1.83 \pm 0.20$ | $-1.46 \pm 0.04$ | $-1.65 \pm 0.06$ | ... | $-1.65 \pm 0.06$ |
| V140 | $-1.72 \pm 0.15$ | ... | $-1.74 \pm 0.15$ | -2.24 | $-1.87 \pm 0.31$ |
| V141 | $-2.20 \pm 0.36$ | $-1.55 \pm 0.36$ | $-1.98 \pm 0.34$ | -1.85 | $-1.89 \pm 0.09$ |
| V142 | $-1.81 \pm 0.24$ | ... | $-1.83 \pm 0.24$ | ... | $-1.83 \pm 0.24$ |
| V143 | ... | $-1.87 \pm 0.14$ | $-2.09 \pm 0.14$ | -2.41 | $-2.17 \pm 0.19$ |
| V144 | $\ldots$ | $-1.71 \pm 0.12$ | $-1.91 \pm 0.12$ | -1.62 | $-1.86 \pm 0.16$ |
| V145 | ... | $-1.58 \pm 0.07$ | $-1.77 \pm 0.07$ | -1.43 | $-1.75 \pm 0.12$ |
| V146 | $\ldots$ | ... | ... | -1.93 | $-1.93 \pm 0.25$ |
| V147 | ... | $-1.66 \pm 0.14$ | $-1.86 \pm 0.14$ | -2.00 | $-1.89 \pm 0.08$ |
| V149 | ... | $-1.21 \pm 0.24$ | $-1.36 \pm 0.24$ | -1.76 | $-1.55 \pm 0.28$ |

Table 10
(Continued)

| ID | [Fe/H] |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | S06 ${ }^{\text {a }}$ | Rey ${ }^{\text {b }}$ | S06+Rey ${ }^{\text {c }}$ | PLI ${ }^{\text {d }}$ | S06+Rey+PLI ${ }^{\text {e }}$ |
| V150 |  | $-1.76 \pm 0.34$ | $-1.97 \pm 0.34$ |  | $-1.97 \pm 0.34$ |
| V151 | $\ldots$ | ... | $-1.46 \pm 0.24$ | ... | $-1.46 \pm 0.24$ |
| V153 | $\ldots$ | $-1.38 \pm 0.19$ | $-1.55 \pm 0.19$ | -1.58 | $-1.56 \pm 0.02$ |
| V154 | $-1.49 \pm 0.23$ | $-1.39 \pm 0.12$ | $-1.55 \pm 0.03$ | -2.31 | $-1.56 \pm 0.13$ |
| V155 |  | $-1.46 \pm 0.09$ | $-1.64 \pm 0.09$ | -1.61 | $-1.64 \pm 0.02$ |
| V156 | $-1.51 \pm 0.38$ | $-1.40 \pm 0.04$ | $-1.57 \pm 0.01$ | ... | $-1.57 \pm 0.01$ |
| V157 |  | $-1.49 \pm 0.10$ | $-1.67 \pm 0.10$ | -0.98 | $-1.57 \pm 0.34$ |
| V158 | $-1.64 \pm 0.49$ | $-1.25 \pm 0.06$ | $-1.41 \pm 0.04$ | -1.57 | $-1.41 \pm 0.03$ |
| V160 | ... | $-1.66 \pm 0.50$ | $-1.86 \pm 0.50$ | -1.84 | $-1.85 \pm 0.01$ |
| V163 | $\ldots$ | $-1.18 \pm 0.27$ | $-1.33 \pm 0.27$ | -1.99 | $-1.68 \pm 0.46$ |
| V166 | $\ldots$ | ... |  | -2.15 | $-2.15 \pm 0.25$ |
| V169 | $-1.65 \pm 0.19$ | $\ldots$ | $-1.67 \pm 0.19$ | -1.83 | $-1.73 \pm 0.11$ |
| V184 | ... | $\ldots$ | ... | -1.78 | $-1.78 \pm 0.25$ |
| V185 | ... | $\ldots$ | $\ldots$ | -1.98 | $-1.98 \pm 0.25$ |
| V261 | $-1.50 \pm 0.35$ | $\ldots$ | $-1.52 \pm 0.35$ | -1.87 | $-1.75 \pm 0.23$ |
| V263 | $-1.73 \pm 0.19$ | $\ldots$ | $-1.75 \pm 0.19$ | -1.41 | $-1.62 \pm 0.23$ |
| V264 | ... | $\ldots$ |  | -1.20 | $-1.20 \pm 0.25$ |
| V265 | $-2.00 \pm 0.29$ | $\ldots$ | $-2.02 \pm 0.29$ | -1.47 | $-1.70 \pm 0.39$ |
| V266 | ... | $\ldots$ |  | -1.89 | $-1.89 \pm 0.25$ |
| V267 | $-1.62 \pm 0.63$ | $\ldots$ | $-1.64 \pm 0.63$ | -2.93 | $-2.76 \pm 0.63$ |
| V268 | $-1.76 \pm 0.24$ | $\ldots$ | $-1.78 \pm 0.24$ | ... | $-1.78 \pm 0.24$ |
| V270 | ... | $\ldots$ |  | -2.69 | $-2.69 \pm 0.25$ |
| V271 | $-1.80 \pm 0.21$ | $\ldots$ | $-1.82 \pm 0.21$ | -1.12 | $-1.53 \pm 0.48$ |
| V272 | ... | $\ldots$ | ... | -1.78 | $-1.78 \pm 0.25$ |
| V273 | $\ldots$ | $\ldots$ | $\ldots$ | -1.53 | $-1.53 \pm 0.25$ |
| V274 | $\ldots$ | $\ldots$ | ... | -1.67 | $-1.67 \pm 0.25$ |
| V275 | $-1.66 \pm 0.36$ | $\ldots$ | $-1.68 \pm 0.36$ | -1.91 | $-1.83 \pm 0.15$ |
| V276 | ... | $\ldots$ | ... | -2.10 | $-2.10 \pm 0.25$ |
| V277 | $\ldots$ | $\ldots$ | $\ldots$ | -2.26 | $-2.26 \pm 0.25$ |
| V280 | $\ldots$ | ... | $\ldots$ | -1.56 | $-1.56 \pm 0.25$ |
| V285 | $\ldots$ | $\ldots$ | $\ldots$ | -1.70 | $-1.70 \pm 0.25$ |
| V288 | $\ldots$ | $\ldots$ | $\ldots$ | -2.17 | $-2.17 \pm 0.25$ |
| V289 | $\ldots$ | ... | $\ldots$ | -2.25 | $-2.25 \pm 0.25$ |
| V291 | $\ldots$ | $\ldots$ | $\ldots$ | -2.09 | $-2.09 \pm 0.25$ |
| NV339 | $\ldots$ | $\ldots$ | $\ldots$ | -3.00 | $-3.00 \pm 0.25$ |
| NV340 |  | $\ldots$ |  | -2.38 | $-2.38 \pm 0.25$ |
| NV341 | $-1.78 \pm 0.59$ | ... | $-1.80 \pm 0.59$ | -2.61 | $-2.48 \pm 0.41$ |
| NV342 | $-1.71 \pm 0.55$ | $\ldots$ | $-1.73 \pm 0.55$ | -1.80 | $-1.79 \pm 0.04$ |
| NV343 | ... | $\ldots$ |  | -2.91 | $-2.91 \pm 0.25$ |
| NV344 | $-1.52 \pm 0.54$ | $\ldots$ | $-1.54 \pm 0.54$ | -2.04 | $-1.95 \pm 0.27$ |
| NV346 | $-1.66 \pm 0.27$ | $\ldots$ | $-1.68 \pm 0.27$ | -2.82 | $-2.29 \pm 0.80$ |
| NV350 | $-1.45 \pm 0.40$ | $\ldots$ | $-1.47 \pm 0.40$ | -2.12 | $-1.94 \pm 0.41$ |
| NV352 | ... | $\ldots$ | ... | -1.97 | $-1.97 \pm 0.25$ |
| NV353 | $-1.93 \pm 0.31$ | $\ldots$ | $-1.95 \pm 0.31$ | -2.31 | $-2.17 \pm 0.25$ |
| NV354 | $-1.73 \pm 0.23$ | $\ldots$ | $-1.75 \pm 0.23$ | -1.29 | $-1.54 \pm 0.33$ |
| NV357 | $-1.64 \pm 0.99$ | $\ldots$ | $-1.66 \pm 0.99$ | -2.08 | $-2.05 \pm 0.14$ |
| NV366 | $-1.61 \pm 0.14$ | $\ldots$ | $-1.63 \pm 0.14$ | ... | $-1.63 \pm 0.14$ |
| NV399 | $-1.70 \pm 0.67$ | $\ldots$ | $-1.72 \pm 0.67$ | -1.80 | $-1.79 \pm 0.04$ |

[^4]

Figure 16. Iron distribution of $\omega$ Cen RRLs. The black shaded area shows iron estimates based on the inversion of theoretical I-band PLZ relations for RRab and RRc variables. The red shaded area shows iron distribution based on measurements available in the literature and is based on both spectroscopic (Sollima et al. 2006a) and photometric (Rey et al. 2000) estimates. The current and the literature iron abundances are in the homogeneous cluster metallicity scale provided by Carretta et al. (2009). The red and black curves display the Gaussian fits of the observed distributions. The means and the $\sigma \mathrm{s}$ of the two Gaussians are also labeled.
on the other data set, are poorly sampled and do not allow us to deduce the occurrence of a Blazhko modulation.

V52. The pulsation parameters are based on the other data set, since the variable is blended in all Danish data sets. Moreover, according to Navarrete et al. (2015), a neighboring star is located at $\sim 0!5$ from the RRL variable.

V55. Period, mean magnitudes and amplitudes are based on photometry by J. Lub and Sturch (1978).

V59, V82, V97. Candidate Blazhko variables according to Kaluzny et al. (2004). The current light curves are well sampled, but they do not show evidence of Blazhko modulation. No firm conclusion can be reached on their Blazhko nature.

V68. This is the brightest ( $V \sim 14.24$ mag) and the longestperiod ( 0.53476174 days) RRc variable. This is an interesting object worth being investigated in more detail.

V73-Candidate Blazhko variable according to Martin (1938). The current light curves are only based on the other data set. They are poorly sampled and do not allow us to deduce the occurrence of a Blazhko modulation.

V80, V177, NV411, NV433. These stars lie outside the area covered by our images. We only provide a new estimate of the periods from the $V+R$ band light curve by Weldrake et al. (2007). NV433 is also a candidate field variable and the current data do not allow us to address whether it is an RRL (Weldrake et al. 2007; Navarrete et al. 2015).

V84. This star lies outside the area covered by our images. The pulsation parameters are based on Walraven $B V$-band photoelectric photometry performed by J . Lub, on $U B V$
photoelectric photometry provided by Sturch (1978) and on OGLE $V$-band photometry (Kaluzny et al. 1997).

V142. Preliminary results concerning the mode identification of V142 indicate that it is the first radial double-mode pulsator in $\omega$ Cen. Note that the double-mode variables found by Olech \& Moskalik (2009) are not F+FO pulsators.

V168. This RRL is a candidate field variable (van Leeuwen et al. 2000; Bellini et al. 2009). On the basis of the current $V$ band mean magnitude we confirm its non-membership. There is mild evidence of a period change.

V172, NV457, NV458. These stars lie outside the area covered by our images. The period, mean magnitude, amplitude, and epochs of maximum and minimum light have been derived from $V$ photometry by the CATALINA survey (Drake et al. 2009, 2013a, 2013b, 2014; Torrealba et al. 2015).

V181, V183. These stars lie outside the area covered by our images. On the basis of their position in the $K, J-K C M D$, these were classified as candidate field variable stars (Navarrete et al. 2015).

V263, NV366. These variables have periods of 1.01215500 and 0.99992364 days and are located on the transition between RRLs and TIICs. The RRL-TIIC transition will be discussed in a forthcoming paper.

V281, V283. These stars lie outside the area covered by our images. The periods, mean magnitudes, amplitudes, and epochs of maximum and minimum light have been derived from $V$ photometry by OGLE (Kaluzny et al. 1997). V283 is also a candidate field variable.

NV351. This variable on our images is heavily blended and we could not derive the mean magnitudes and amplitudes.

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[^1]:    ${ }^{21}$ This data set also includes 140 CCD images that were collected in 1996. They were included in the danish 95 data set due to the limited sample size.

[^2]:    ${ }^{22}$ The reader is referred to Pietrinferni et al. (2006) and to the BASTI data base (http://albione.oa-teramo.inaf.it) for a more detailed discussion concerning the evolutionary framework adopted in constructing the pulsation models.

[^3]:    ${ }^{23}$ Oosterhoff type I clusters: NGC 5272, NGC 5904, NGC 6121, NGC 6229, NGC 6266, NGC 6362, NGC 6981.
    ${ }^{24}$ Oosterhoff intermediate clusters: IC 4499, NGC 3201, NGC 6715, NGC 6934, NGC 7006.
    ${ }^{25}$ Oosterhoff type II clusters: NGC 4590, NGC 5024, NGC 5286, NGC 7078.
    ${ }^{26}$ Oosterhoff type III/Oosterhoff type 0 clusters: NGC 6388, NGC 6441.

[^4]:    Notes.
    ${ }^{\mathrm{a}}$ Spectroscopic iron abundances provided by Sollima et al. (2006a).
    ${ }^{\mathrm{b}}$ Metallicity estimates provided by Rey et al. (2000) using the $h k$ photometric index.
    ${ }^{c}$ Mean iron abundances based on S06 and R00 abundances. The original iron abundances provided by S06 and by R00 were rescaled to the homogeneous cluster metallicity scale provided by Carretta et al. (2009). The R00 abundances were transformed into this metallicity scale using the linear relation (ZW84 to UVES) given in Section 5 of Carretta et al. (2009). The S06 abundances were transformed into the the same scale by accounting for the difference in solar iron abundance in number $\log \epsilon_{\mathrm{Fe}}=7.52$ versus 7.54 (Gratton et al. 2003, Carretta et al. 2009).
    ${ }^{\mathrm{d}}$ Iron abundances based on the inversion of the I-band PLZ relations for RRab and RRc variables (for more details see Section 8 ). The solar iron abundance log $\epsilon_{\mathrm{Fe}}$ was rescaled from 7.50 (pulsation and evolutionary models) to 7.54 of the Carretta's metallicity scale. The typical relative error on the abundance of RRLs based on the PLZ relations ranges from 0.2 to 0.3 dex. The error budget accounts for uncertainties in the $I$-band mean magnitude, in the differential reddening and in the standard deviation of the PLZ relations. The mean weighted metallicities listed in the last column, were estimated by adopting for the current estimates a mean error of 0.25 dex.
    ${ }^{\mathrm{e}}$ Mean iron abundances based on S06, R00 and on the current estimates. The iron abundances listed in column 5 were shifted by 0.09 dex, to take account of the difference in the metallicity distributions plotted in Figure 16.

