

1 Electrical Production of a Small Size Concentrated
2 Solar Power Plant with Compound Parabolic Collectors

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6 **Abstract**

7 The use of the solar energy for electricity or useful heat generation has
8 been extensively investigated as an alternative to fossil fired energy conver-
9 sion. Particularly in the last decade, many studies have been carried out
10 on Concentrated Solar Power (CSP) which was developed worldwide with
11 Spain acting as the leading country in this field. Concentrating solar energy
12 requires complex mirror systems which continuously move to track the sun.
13 In comparison with flat mirrors, Parabolic Through Collectors (PTCs) have
14 allowed to reduce costs, but they still remain quite an expensive solution.
15 Instead, compound parabolic collectors (CPCs) are able to collect a higher
16 fraction of both the direct and the diffuse radiation, although they have a
17 lower efficiency at high temperature. Moreover, at least within certain limits,
18 they do not require a tracking system. Their employment is therefore suited
19 for the collection of medium temperature heat (up to 200 °C) and is useful
20 for the reduction of the installation cost of Concentrated Solar Power (CSP)
21 heating/cooling and energy generation systems. Small size plants (10 - 50
22 kW) were studied in this paper since they are more likely to be realized due
23 to their smaller initial investment cost and to the capability of being installed

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24 on the roof of existing buildings. While the Organic Rankine Cycle (ORC)
25 solution is well established to be the optimal for small size, distributed gen-
26 eration plants, the technology of the expansion device is still to be defined
27 for the investigated installed power range. Accordingly to previous studies,
28 an expansion device based on the Wankel mechanism was employed.

29 Based on these considerations and prior to more detailed analyses, a study
30 of the annual energy production of a small scale ORC power plant using
31 CPCs as a heat source and a volumetric machine as an expansion device
32 was carried out. The influence of the thermodynamic cycle parameters, the
33 working fluid, the concentration and the tilt angle of the collectors on the
34 electrical energy production were taken into account. The thermal module
35 delivered power, the expansion device isentropic efficiency and the overall
36 efficiency were evaluated by means of a numerical model developed within
37 the simulation tool AMESim v. 12.0.

38 The aim of this work is to provide a contribution in the assessment of
39 the optimal configuration of such kind of plants in terms of collectors con-
40 centration and tilt angle on one hand, and thermodynamic parameter of the
41 thermal module on the other. The annual electricity production was used as
42 a criterion of comparison among the various parameters combinations. The
43 number of operating hours per year was also taken into account for the sake
44 of ensuring a regular production of energy. A selection of commercial solar
45 tubes for the realization of the solar field was carried out and the optimal
46 configuration for both the solar field and the thermal module was found.
47 The results of this study are encouraging and constitute the basis for the
48 development of future analyses.

49 *Key words:*

50 solar energy; CPC; ORC; Wankel; volumetric expansion device; renewables;
51 evacuated collectors

52 **1. Introduction**

53 The attractiveness of the Organic Rankine Cycles (ORCs) mainly resides
54 in that they are able to use low temperature heat sources while operating at
55 relatively high efficiencies, thus enabling the construction of low and medium
56 scale power plants that may be suited to a large variety of applications. Most
57 of these advantages may also fit for solar applications, especially for small-size
58 power plants, in combination with low/medium temperature solar collectors
59 [1–3], where the integration with other resources is always an interesting
60 option (with biomass or geothermal energy for example [4]).

61 The nature of the working fluid has also been the object of several studies:
62 in the first research works [5, 6] high Ozone Depleting Potential (ODP) re-
63 frigerants such as R11 or R13 were used. In more recent studies other newly
64 developed refrigerants were used, such as R245fa [7]. The optimization of
65 the fluid selection for different cycle architectures and collectors' tempera-
66 tures was treated in more recent studies [8–13]. However, no single fluid has
67 been identified as optimal for the ORC, due to the strong interdependence
68 between the working fluid features, the operating conditions and the cycle
69 architecture. Most of the above mentioned studies show that the ORC ef-
70 ficiency is significantly improved by inclusion of a recuperator, of cascaded
71 cycles, or of reheating [9, 14, 15].

72 At present, only one commercial solar ORC power plant is reported in the

73 technical literature: the 1 MWe Saguario Solar ORC plant in Arizona, which
74 uses n-pentane as working fluid and shows an overall efficiency of 12.1%, with
75 a collector efficiency of 59% [16]. The relatively high efficiency of this plant
76 is due to the employment of high concentration tracking parabolic trough
77 collectors.

78 The lowest efficiencies were in fact obtained with stationary collectors.
79 Some authors [7] reported a 3.2% overall efficiency in a 1.6 kWe solar ORC
80 with flat-plate collectors and 4.2% with evacuated tube collectors. A sim-
81 ilar efficiency (lower than 4%) was obtained in a 2 kWe low-temperature
82 solar ORC with R134a as working fluid and evacuated tube collectors [17].
83 In both those experiences, however, the collectors were used without any
84 prior optimization process concerning concentration, tilt angle and collectors
85 alignment. The collectors were aligned in the north-south direction and the
86 originally built-in concentrator was used. For the sake of comparison of the
87 previously mentioned solutions with those with a tracking system, a 7.7%
88 efficiency was reported in a 9 kWe ORC employing a linear Fresnel Collector
89 (collector efficiency of 57%).

90 Although solar ORCs feature lower efficiencies than photovoltaic (PV)
91 systems, the presence of a thermal storage and even the thermal inertia itself
92 of these plants provide a more stable electrical production, which make their
93 power generation more predictable and easy to dispatch than PV systems.
94 In addition, this technology does not require the employment of advanced
95 or rare materials such as pure silicon. Finally, the employment of commonly
96 available and reusable or recyclable materials (steel, plastics, aluminum, cop-
97 per, etc.) makes the end-life disposal of the plants easier than for PV panels.

98 Focusing the attention on mini and micro (up to 50 kW) solar applica-
99 tions, the absence of a tracking system and the use of compact design col-
100 lectors are useful for the reduction of the installation and maintenance costs.
101 In fact, if a maximum cycle temperature of 200 °C is considered, Compound
102 Parabolic Collectors (CPCs) can be used since they do not require a tracking
103 system and they allow a moderate concentration. These concentrators have
104 been studied for many years, both analytically and practically [18–24] as well
105 as solar ORCs, which reported overall efficiencies varying between 2.5% and
106 7% [5, 25, 26].

107 The aim of this work is to fill the gap observed in the related literature
108 about the analysis of the optimal combination of the operating parameters
109 of both the solar field (concentration, collectors tilt angle) and the thermal
110 module (thermodynamic parameters, plant configuration). The preliminary
111 study presented about the feasibility of such a system [27] was further ex-
112 tended in the present work through the investigation of the thermal cycle
113 optimal layout, the characterization of collectors built on the basis of com-
114 mercially available components and a more detailed analysis of the solar field
115 performance.

116 The optimal solution, to which type of expander is most suited, has not
117 been found yet: some studies proposed the use of vane expanders [5, 6], oth-
118 ers proposed a rolling piston expander [7] or a machine derived from a Scroll
119 compressor [28]. In the present work the authors propose to use a specif-
120 ically designed unit, based on the Wankel capsulism, which was described
121 in a previous publication [29–32] where they showed that such device is an
122 effective solution in the 10-50 kW size range. Such an expander, moreover,

123 is more compact than reciprocating devices and is able to rotate at higher
124 speeds with lower vibrations.

125 This first analysis was carried out at steady state, whereas a study of
126 transient operation is currently in progress and will be the subject of a future
127 paper.

128 Nomenclature

a	Solar tube thermal loss coefficient
A	Area (m^2)
C	Concentration
D	Direct radiation (kW m^{-2})
I	Incident solar radiation (kW)
E	Energy amount (kJ)
\dot{E}	Energy flux (kW)
h	enthalpy (kJ kg^{-1})
H	Diffuse radiation (kW m^{-2})
K	Proportionality constant
N	Number of reflections
\dot{Q}	Heat flux (kW)
r	Radius (m)
R	Factor of inclination
T	Temperature (K)
U	Convective heat transfer (kW m^{-2})
V	Displacement (cm^3)
\dot{W}	Mechanical power (kW)
Z	Number of hours

subscripts

<i>a</i>	ambient
<i>ab</i>	aerocondenser blower
<i>ac</i>	acceptance
<i>ap</i>	approach point
<i>av</i>	average
<i>aux</i>	auxiliaries
<i>c</i>	collector
<i>cd</i>	condensation
<i>cg</i>	cover glass
<i>con</i>	convective
<i>d</i>	daily
<i>df</i>	diffuse
<i>di</i>	direct
<i>ed</i>	expansion device
<i>hf</i>	heat transfer fluid
<i>in</i>	incoming
<i>is</i>	isentropic
<i>l</i>	lost
<i>max</i>	maximum
<i>min</i>	minimum
<i>op</i>	optical
<i>out</i>	outgoing
<i>p</i>	pump

<i>pp</i>	pinch point
<i>r</i>	receiver
<i>ref</i>	reflected
<i>rad</i>	radiative
<i>rem</i>	removal
<i>s</i>	solar
<i>tc</i>	thermal cycle
<i>th</i>	thermal
<i>u</i>	useful
<i>wf</i>	working fluid

Greek

α	Sun elevation
β	Collectors tilt angle ($^{\circ}$)
ϵ	Emissivity
η	Efficiency
φ	Reflection efficiency
Φ	Heat removal factor
γ	Collectors azimuthal angle ($^{\circ}$)
ρ	Radial coordinate (m)
σ	Stefan-Boltzmann constant ($\text{kW m}^{-2} \text{K}^{-4}$)
θ	Angular coordinate ($^{\circ}$)

129 **2. Method**

130 The plant layout which has been taken as a reference is typical of the
131 small-scale solar systems (fig. 1). Here the solar field and the thermal mod-
132 ule were connected via a heat transfer fluid circulation (water in this case).
133 The working fluid condensation was supposed to happen through air-cooled
134 condensers with induced-draft fans.

135 INSERT FIG1 ABOUT HERE

136 The thermal module included the preheating section, the evaporator, the
137 eventual superheater, the expansion device, the recuperator and the con-
138 denser. Its annual electricity production was calculated by means of a nu-
139 merical model which is described hereinafter. The transient behavior of the
140 solar source was not taken into account here and an average insolation was
141 employed.

142 Since steady state conditions were investigated, the storage tank, which
143 is usually employed in solar systems, was not modeled. The cogeneration
144 was not taken into account as well since the aim of this study was evaluating
145 the optimal conditions for the electricity generation.

146 Under the hypothesis of steady state, averaged working conditions, the
147 annual electricity production was calculated as:

$$E_{an} = \sum_{i=1}^{12} \overline{I_i \cdot Z_i \cdot \eta_{s,i} \cdot \eta_{th,i}} \quad (1)$$

148 In order to separate the effects of variation of the solar field and the
149 thermal module parameters, the previous relationship was approximated as

$$E_{an} \simeq \sum_{i=1}^{12} \bar{I}_i \cdot \bar{Z}_i \cdot \bar{\eta}_{s,i} \cdot \bar{\eta}_{th,i} \quad (2)$$

150 in which \bar{I}_i denotes the solar radiation averaged over the generic i-th
 151 month, Z_i is the number of operating hours during the i-th month, $\bar{\eta}_{si}$ the
 152 solar field average efficiency and $\bar{\eta}_{th,i}$ the thermal cycle average efficiency.
 153 For the sake of brevity, in the following lines the superscripts denoting the
 154 operation of averaging will be omitted.

155 *2.1. Solar intensity and operating hours*

156 Since the investigated temperature range exceeded 100 °C, based on lit-
 157 erature [23] the axis of the absorbers was aligned in east-west direction. The
 158 disposition used in the present work enabled the employment of various con-
 159 centrations reflectors, differently from other papers found in literature in
 160 which the absorbers were aligned in nord-south direction [7, 17].

161 The solar intensity on the collector was calculated at the latitude of the
 162 Central Italy (43°) through the model of Liu and Jordan [33] which takes
 163 into account the distribution of direct, diffuse and reflected solar radiation:

$$I = R_{di} \cdot D + R_{df} \cdot H + R_{ref} \cdot (D + H) \quad (3)$$

164 The average number of operating hours per month was calculated by
 165 considering the sunrise and the sunset time relative to a surface tilted by β
 166 (fig. 2) with respect to the horizontal and oriented toward the south. The
 167 operating hours are furthermore limited by the angle of the collectors.

168 INSERT FIG2 ABOUT HERE

169 In order to collect the solar radiation at noon, for each value of θ_{ac} , the
 170 maximum collectors tilt angle β_{max} was calculated as:

$$\beta_{max}(C) = \alpha_{max} - (90^\circ + \theta_{ac}) \quad (4)$$

171 At the same time, for each value of β , the minimum angle α_{min} at which
172 the sun radiation was collected by the collectors was calculated as:

$$\alpha_{min} = 90^\circ - (\beta + \theta_{ac}) \quad (5)$$

173 2.2. Collectors average efficiency

174 Focusing the attention on small-scale power systems and aiming at the
175 maximum reduction of the installation costs, widely commercially available
176 components such as the U-pipe evacuated tubes were considered (fig. 3).

177 INSERT FIG3 ABOUT HERE

178 The efficiency of the collectors was calculated by taking into account the
179 performances of commercially available components. Four types of tubular U-
180 pipe collectors were considered. In order to avoid any form of commercialism,
181 the brand name of these components will not be explicitly mentioned and
182 the the various types will be identified by capital letters.

183 The efficiency of the collectors was calculated through a balance between
184 the incoming and the outgoing energy, namely the solar radiation on one
185 hand, the useful and the lost heat on the other.

$$\dot{E}_{s,in} = \dot{Q}_u + \dot{Q}_l \quad (6)$$

186 The energy collected by the solar tube $\dot{E}_{s,in}$ was evaluated as the product
187 of the solar radiation by the optical efficiency and the heat removal factor Φ
188 that takes into account the non-constant temperature of the receiver.

$$\dot{E}_{s,in} = \dot{E}_s \cdot \eta_{op} \cdot \Phi = I \cdot C \cdot A_c \cdot \eta_{op} \cdot \Phi \quad (7)$$

189 The solar field was discretized in a series of collectors in which the tem-
190 perature variation effect was negligible from the point of view of the collector
191 efficiency. The factor Φ consequently had a unit value.

192 As far as the collector's efficiency is concerned, the technical documenta-
193 tion reports the coefficients η_0 (optical efficiency), a_1 and a_2 (linear and the
194 quadratic terms coefficients, respectively), according to EN 12975 [34] (Tab.
195 1). Those coefficients however include the effect of the built-in reflector which
196 usually has a concentration in the range $C = 0.6 - 0.8$.

197 INSERT TAB1 ABOUT HERE

198 In order to take into account the influence of C on the optical efficiency,
199 a simplified approach, with respect to other models described in literature
200 [35], was employed. The effect of the reflections number N , which is usually
201 provided by well-known datasets for both untruncated and truncated reflec-
202 tors [1], was accounted here by considering that a generic sunray entering the
203 collector may directly impinge the glass tube or be reflected one time by the
204 reflector and attenuated by the factor φ . In addition, since a U-pipe solar
205 tube was employed instead of a trough collector, the sunrays pass through
206 the glass two times and therefore the relative loss was accounted twice.

207 The values of the optical efficiency obtained with this approach by ap-
208 plying the original values of C were compared with the values of η_0 reported
209 in tab. 1, showing quite a good agreement (tab. 2).

210 INSERT TAB2 ABOUT HERE

211 This approach also accounted for a slight decrease of the optical efficiency
212 with C , with a certain correspondence with theory (fig. 4).

213 INSERT FIG. 4 ABOUT HERE

214 The efficiency of the solar collector was evaluated by calculating the con-

215 vective and the radiating losses to the ambient air:

$$\begin{aligned}\dot{Q}_l &= \dot{Q}_{l,con} + \dot{Q}_{l,rad} = \\ &= U_l \cdot \frac{A_c}{C} (T_r - T_a) + \sigma \epsilon_r \cdot \frac{A_c}{C} (T_r^4 - T_a^4)\end{aligned}\tag{8}$$

216 The tuning of the numerical model coefficients was carried out by varying
217 the convective heat transfer coefficient U_l and the emissivity of the receiver
218 ϵ_r (tab. 3).

219 INSERT TAB3 ABOUT HERE

220 The resulting efficiencies of the various collectors were consistent with
221 the ones declared by the companies (fig. 5) and with other data reported in
222 literature [36–39]. The deviation between the declared and the recalculated
223 efficiency is lower than 1% for all but model C.

224 INSERT FIG. 5 ABOUT HERE

225 All these relationships were finally summarized to evaluate the collectors
226 efficiency as a function of the solar radiation I , the concentration C , the
227 inlet $T_{r,in}$ and outlet $T_{r,out}$ temperature of the heat transfer fluid and the
228 ambient air temperature T_a , thus allowing the model of the solar collector to
229 be included into the model of the whole plant.

230 As for the inlet and outlet collectors temperature $T_{hf,in}$ and $T_{hf,out}$, their
231 evaluation was carried out by considering (fig. 2) a fixed value for the tem-
232 perature difference at the pinch ΔT_{pp} and at the approach point ΔT_{ap} (5
233 and 10K, respectively).

234 *2.3. Thermal cycle modeling*

235 The thermal plant efficiency η_{th} was calculated as the ratio of the net
236 power over the heat flux provided by the solar field.

$$\eta_{th} = \frac{\dot{W}_{net}}{\dot{Q}_u} = \frac{\dot{W}_{net}}{\eta_s I} \quad (9)$$

237 The net power delivered by the plant was evaluated as the difference
238 between the power generated by the expander minus the power employed by
239 the auxiliaries (pump, condenser blowers).

$$\dot{W}_{net} = \dot{W}_{ed} - \dot{W}_p - \dot{W}_{ab} \quad (10)$$

240 The isentropic efficiency of the pump was assumed to be constant and
241 equal to $\eta_p = 0.7$, from which the power required by the pump was calculated
242 as:

$$\dot{W}_p = \frac{\dot{m}_{wf}(p_{vap} - p_{cd})}{\eta_p \rho_{wf}} \quad (11)$$

243 The power required by the aerocondenser blowers was evaluated as pro-
244 portional to the rejected heat. The proportionality constant K_{ab} was eval-
245 uated through a survey of the commercially available components and its
246 value was set at 25 W per thermal kW of rejected thermal power \dot{Q}_{rj} (at the
247 design point, that is to say ΔT between condensing fluid and ambient air
248 equal to 15 °C).

$$\dot{W}_{ac} = K_{ab} \dot{Q}_{rj} = K_{ab} (\dot{Q}_u - \dot{W}_{ed}) \quad (12)$$

249 As for the expansion device, the proposed machine was already analyzed
250 in previously published papers [31, 32, 40]. Although this machine is a rotary
251 device, the thermodynamic limit cycle is the same of a reciprocating one (fig.
252 6).

253 INSERT FIG6 ABOUT HERE

254 The numerical analysis was carried out using a numerical model built us-
255 ing the simulation tools AMESim v.12.0, simulating the in-chamber pressure
256 as a function of the crank angle. The numerical model of the Wankel expan-
257 sion machine was developed in previous works [31], but in this analysis the
258 two-phase fluids library of the code was used to analyze this device operated
259 with organic fluids. The volume variation of the chamber was calculated by
260 the crank-conrod model, whose mathematical formulation was modified in
261 accordance with the variation of volume of a Wankel engine using the AME-
262 Set utility. The pressure drop across the intake and the exhaust valves was
263 accounted by modeling the valves themselves as variable area orifices. The
264 numerical model of the device was validated by comparing the results with
265 experimental data [40].

266 Since the available solar heat was obviously variable along the year, the
267 working fluid mass flow rate was supposed to be variable too by means of
268 the expansion device rotating speed variation. This regulation strategy in
269 facts proved to be effective for this kind of machines, although a certain
270 decrease of η_{is} with the rotating speed was observed [40, 41]. Conservatively,
271 η_{is} was supposed to depend on p_2/p_3 and T_2 only and, for every combination
272 of these two parameters, the value assumed at the maximum rotating speed
273 (3000 rpm) was considered.

274 **3. Numerical results and discussion**

275 As pointed out in the literature [42], the choice of the optimal tempera-
276 ture in the receivers is a tradeoff between collector efficiency and ORC effi-

277 ciency. Increasing the temperature leads to higher thermal losses but also to
278 a higher thermal module conversion efficiency. The optimal conditions may
279 furthermore vary along the year due to the different insolation and ambi-
280 ent temperature. The optimal operating conditions were therefore evaluated
281 respect to the annual electricity production.

282 3.1. Working fluid and introduction grade

283 Based on previously published work [27], R-600a was considered as work-
284 ing fluid because, in in one hand it provided a somewhat lower delivered
285 power than other fluids (like R-134a and R-152a), in the other it also yielded
286 a better efficiency over a wider temperature range.

287 Since the performance of a volumetric expansion device is affected by
288 the introduction grade (eq.13), an appropriate value has to be chosen as a
289 tradeoff between isentropic efficiency and delivered power.

$$\sigma = \frac{V_b - V_a}{V_{ud}} \quad (13)$$

290 Based on the performed analysis, an introduction grade equal to 0.2 en-
291 abled the device isentropic efficiency to be equal or above 0.8 over the entire
292 range of the expansion grades p_3/p_4 (ratio of the upstream over the down-
293 stream pressure) included between 3 to 8 (fig. 7).

294 INSERT FIG7 ABOUT HERE

295 In these conditions the expansion was almost complete (fig. 8, dashed
296 line). Lower pressure ratios led to over-expanded cycles (continuous line),
297 with a loss represented by the counter-clock wise area, and higher pressure
298 ratios obviously led to under-expanded cycles (dotted line).

299 INSERT FIG8 ABOUT HERE

300 The resulting isentropic efficiency was comparable and in several cases
301 even higher than a radial turbine of the same power range [43] or than a
302 volumetric expansion device of other type (Scroll as an example) [44–48]
303 over the most part of the investigated working conditions.

304 As for the delivered power, at 3000 rpm it was included within the range
305 10-50 kW, which is interesting for this research (fig. 9). Based on these
306 considerations, the value of 0.2 was therefore retained acceptable.

307 INSERT FIG9 ABOUT HERE

308 *3.2. Collectors concentration and tilt angle*

309 As it is well known, a high concentration of the collectors improves the
310 direct irradiation captating efficiency at high temperature, however the em-
311 ployment of a low concentration also implies the capability of captating more
312 diffuse radiation and enables the plant to operate for a larger number of hours.
313 In the present work concentrations up to 3 were considered, since for higher
314 values at least one seasonal replacement is needed.

315 The optimal annual electrical production conditions were practically the
316 same whatever the thermodynamic parameters of the plant (fig. 10 and
317 11). This trend was also found when changing the tube type, although with
318 different values of the value of the annual generated energy (fig. 12 and
319 13). In every case, values of the generated energy greater than 90% of the
320 maximum were found in a region which is delimited at the left by $C \simeq 1.2$
321 and at the right by a slanted line intersecting the first in a point whose
322 ordinate is $\beta = 15\text{-}20^\circ$. On the right side of the graph the annual production
323 is nearly proportional to the number of operating hours, while on the left
324 side it depends on the concentration.

325 INSERT FIG10 ABOUT HERE

326 INSERT FIG11 ABOUT HERE

327 INSERT FIG12 ABOUT HERE

328 INSERT FIG13 ABOUT HERE

329 The largest annual production per unit surface of panel was yield when
330 the tilt angle of the collectors is larger than 20-25°. However when the tilt
331 angle is further increased, as widely recognized, the employed ground surface
332 becomes greater and greater. The choice of the optimal tilt angle is therefore
333 a tradeoff between annual energy income per unit surface of panel and ground
334 occupation.

335 Tilt angle and concentration also affected the plant average specific (per
336 panel unit surface) power even when the annual generated energy was the
337 same, because the number of operating hours was different (fig. 14). There-
338 fore it was possible to reduce the average delivered power without reducing
339 the generated energy, with significant implications on the size of the compo-
340 nents and hence on the initial investment costs.

341 INSERT FIG14 ABOUT HERE

342 *3.3. Thermal cycle layout*

343 The employment of saturated or superheated cycles was deeply studied in
344 the literature. Some authors [49] expressed some doubts about superheating
345 a dry fluid, but they did not take into account the regeneration of the residual
346 heat at the outlet of the expansion device. Moreover the use of regeneration
347 enables the partial recovery of the energy loss due to the under-expansion of
348 the working fluid which is typical of volumetric machines.

349 As expected, the increase of recuperated heat produced different effects
350 on the thermal cycle and solar field efficiency (positive effect on the first and
351 negative on the second), since the heat transfer fluid entered the solar field
352 at a higher temperature (fig. 15). Since the first effect was prevailing on
353 the second, the overall efficiency was increased even in the less favourable
354 conditions (winter season). In addition, the partial removal of the residual
355 sensible heat by the recuperator reduced the condenser thermal load and
356 consequently a lower energetical consumption was required by the blowers.

357 INSERT FIG15 ABOUT HERE

358 In order to compare saturated and superheated cycles, the results were
359 related to the collectors efficiency degradation with temperature: although
360 the collector model "A" had the highest optical efficiency (fig. 7), the annual
361 production yield was lower than collector "D", even at a very low saturation
362 pressure and without superheating. The second model not only allowed the
363 global efficiency (solar + thermal) to be higher, but also made convenient
364 the use of superheating (fig. 16 and 17). For these two tube models, the
365 optimal conditions respectively were $p_3 = 20$ bar and saturated conditions
366 and $p_3 = 30$ bar and $T_3 = 160^\circ\text{C}$.

367 INSERT FIG16 and FIG 17 ABOUT HERE

368 4. Conclusions

369 This paper summarizes the results of a research carried out to evaluate
370 the optimal average operating conditions for a small-size solar power plant
371 that employs stationary Compound Parabolic Collectors and a volumetric
372 rotary expansion machine.

373 The proposed Wankel expansion machine allowed the use of the most
374 suited introduction grade by means of a proper choice of the intake valves
375 timing choice. This feature allowed to keep the isentropic efficiency equal
376 or higher than 0.8 over the majority of the assumed working conditions and
377 namely when the expansion ratio was within the range 3-8.

378 The features of the solar tubes played a fundamental role in determin-
379 ing the annual energy yield, since the collectors efficiency decrease rate with
380 the temperature not only affected the amount of energy collected, but also
381 changed the optimal thermal cycle features (saturated or superheated) and
382 operating conditions (saturation pressure and eventual superheating temper-
383 ature). The best performance was attained with $p_{sat} \simeq 30$ bar and $T_{sh} \simeq$
384 160°C and employing the tube model D, which showed the highest insula-
385 tion properties amongst the investigated commercial types. Based on the
386 comparison between some commercial models, in facts the annual energy
387 production was more affected by the insulation properties than by optical
388 efficiency, which appeared to play a secondary role when temperatures above
389 $80 - 90^\circ\text{C}$ were needed.

390 As for the solar field optimal parameters, the best performance was
391 yielded with a concentration ensuring at least 3000 operating hours per year:
392 the energy production was maximized when concentration was in the range
393 1.1 - 1.4, which in fact allowed the plant to be operated for 3000 - 3500 hours
394 per year. Although an amount of energy close to the maximum may be col-
395 lected with different combinations of C and β , a reasonable tradeoff between
396 energy yield per collectors' unit surface and occupied ground surface may be
397 achieved by using a tilt angle smaller than $20-25^\circ$.

398 The importance of C and β was not limited only to the amount of gener-
399 ated energy. A proper choice of these two parameters maximized the number
400 of operating hours without an appreciable reduction of the energy specific
401 production. This feature enables the reduction of the initial investment cost
402 because the size of the various components (heat exchangers, pumps, aero-
403 condensers and relative blowers, connection pipes) can be decreased.

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