



28 *Keywords:* excess volumes, compressibility, cavity, hydrophobic solute, TIP4P,  
29 simulations

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## 30 **1. Introduction**

31 The variation of volume in the solvation of a molecule at constant pressure, as well  
32 as in chemical reactions and in general processes occurring in a solution, is a quan-  
33 tity of fundamental importance within solvation thermodynamics [1, 2, 3, 4, 5].

34 Solutions are generally studied at ambient conditions, but there is great interest in  
35 studying processes under different conditions. The effect of pressure on the con-  
36 formational stability of a protein in an aqueous solution is a typical example [3].

37 When 1 mol of solute is added to an infinite amount of solution, the variation in  
38 volume defines the partial molar volume that is decomposed in an ideal solution  
39 contribution and the excess volume [3, 5]. This important intensive variable varies  
40 with solution composition. Excess volumes have been mainly obtained experi-  
41 mentally [6, 7, 1, 8] rather than from simulations [9, 10, 11, 12, 13, 14, 15, 16, 17],  
42 which are generally performed for an infinitely dilute solution.

43 According to the Kirkwood-Buff (KB) theory [18], excess volumes are defined in  
44 terms of integrals of pair distribution functions and therefore include a lot of infor-  
45 mation on intermolecular affinities. Inversion theory [2, 3, 19, 20] was developed  
46 to extract this information from experimental measures of partial molar volumes,  
47 while interaction potentials are a fundamental input of molecular simulations from  
48 which distribution functions are typical results [21, 22]. In this respect, simu-  
49 lations are a useful tool to understand how interactions affect macromolecules  
50 properties in aqueous solutions and in complex environments [23, 24, 25]. More  
51 recently, given the great interest in biological systems, molecular simulations have  
52 been used to compute KB integrals to study cosolvent interactions in aqueous so-  
53 lutions with solutes chosen as representative of hydrophilic and hydrophobic sites

54 on proteins [26]. With the aim of understanding pressure-induced protein denatu-  
55 ration, the different role of these sites has been discussed [27, 28], while volume  
56 dependence on pressure has been the object of various studies [29, 17, 30, 31, 32].  
57 A valid alternative approach based on simulations is the direct method [15, 17],  
58 whose reliability has been very recently demonstrated in a study of benzene in  
59 three solvents at several pressures [32]. The study of the free energy of solvation  
60 at various pressures is the basis for a less commonly investigated method that ob-  
61 tains excess volumes from the slope of the fitted curve [17, 32]. Generally, as the  
62 curves do not present clear curvature, linear fits are used, and excess volumes are  
63 considered almost constant in a wide range of P. On the other hand, the pressure  
64 dependence of partial molar volumes has been taken into account for the evalu-  
65 ation of excess compressibility from simulation [17] and experimental data [29].  
66 Unfortunately, the pressure derivative of apparent compressibility has been mea-  
67 sured only for very few compounds. Therefore, linear and quadratic descriptions  
68 have been assumed for excess volumes. Simulation results have been fitted with  
69 quadratic polynomials [17] or using the Tait equation [31], originally applied to  
70 pure liquids [33].

71 This work deals with the effect of increasing pressure on excess volumes of hard-  
72 sphere solutes in water at 298 K. The insertion of this simple modeled solute is  
73 equivalent to the formation of a cavity [34] and reference is made to the cor-  
74 responding quantity as cavity excess volumes. In this respect, it is important to  
75 recall that there is no size limitation so that cavities can or cannot host a real solute  
76 [34] [35].

77 In the following section, methods to compute excess volumes, either based on

78 simulations or on the pressure derivative of the excess chemical potential, are  
79 briefly outlined. Furthermore, some focus is on volume-derived quantities such  
80 as adsorption at the cavity surface and excess compressibility. Hence, excess vol-  
81 umes from simulations obtained by the direct method [15, 17, 32] are presented  
82 focusing on two main aspects of increasing pressure. Firstly, comparison is made  
83 between very high and atmospheric pressure conditions for the process of scaling  
84 the cavity radius. Secondly, excess volume and excess compressibility are shown  
85 along the isotherm for two specific cavities. Their sizes are appropriate to host  
86 approximately a water molecule and a hypothetical spherical solute slightly larger  
87 than a fullerene molecule. Results are compared with those from KB integrals,  
88 which can be analysed in terms of shell contributions. Finally, some heuristic  
89 expressions to fit simulation results are considered.

## 90 **2. Calculation**

### 91 *2.1. Excess Volumes from simulations*

92 In an infinitely dilute solution, solute-solute interactions can be neglected and ac-  
93 cording to the KB theory [18], for a spherical solute the excess volume is directly  
94 related to the radial distribution of the solvent (w) around the solute (s),

$$v_s^* = - \int_0^\infty [g_{sw}(r) - 1](4\pi r^2) dr \quad (1)$$

95 where the integral is known as the KB integral.

96 As the KB theory has been developed in the gran-canonical ensemble, the solute-  
97 solvent distribution functions should be computed from simulations in this ensem-  
98 ble, even if some studies have shown that the canonical (NVT) [9, 10, 11, 12, 14,

99 36] and the isothermal isobaric (NPT) [36, 37, 13, 15, 16, 38, 30] ensembles can  
 100 be used without serious problems. These problems can be effectively managed  
 101 [39, 15] by scaling for the correction due to the different asymptotic values of  $g(r)$   
 102 in the different ensembles [40, 41]. Nevertheless, irrespective of the statistical  
 103 ensemble,  $v_s^*$  from simulations obtained by the KB formula needs to be assessed  
 104 for accuracy because of the truncation of the integrals [11, 15].

105 Another method is based on the relation between excess volumes and partial molar  
 106 volumes,  $v_s$ , namely:

$$v_s^* = v_s - k_T^0 k_B T \quad (2)$$

107 where  $k_B$  is the Boltzmann constant,  $T$  is the temperature and  $k_T^0$  is the solvent  
 108 isothermal compressibility, and in accordance with the thermodynamic definition,  
 109  $v_s$ , the partial molar volume is

$$v_s = \left( \frac{\partial V}{\partial N_s} \right)_{P, T, N_w}, \quad (3)$$

110  $N_s$  and  $N_w$  being the numbers of solute and solvent molecules respectively. Fol-  
 111 lowing this definition,  $v_s$  can be computed from simulations in the NPT statistical  
 112 ensemble such as the variation in the average volumes ( $\langle V(N_s, N_w) \rangle$ ) when  
 113 the solute is introduced into the solvent [15]

$$v_s = \langle V(1, N_w) \rangle - \langle V(0, N_w) \rangle. \quad (4)$$

114 This method is known as the direct method. The term  $k_T^0 k_B T$  in Eq. (2) represents  
 115 the thermal contribution of the solute motion to  $v_s$  [3], so that if the solute is kept

116 fixed during the simulation,  $v_s^*$  is actually computed by Eq. (4). Alternatively,  
 117 according to Maghaddam and Chan [17], it can be computed from simulations at  
 118 a fixed solute position by the expression,

$$v_s^* = \frac{\langle V^2(1, N_w) \rangle}{\langle V(1, N_w) \rangle} - \frac{\langle V^2(0, N_w) \rangle}{\langle V(0, N_w) \rangle}. \quad (5)$$

119 According to thermodynamics [3, 5], excess volumes can be obtained from a pres-  
 120 sure study of the excess chemical potential,  $\mu^*$ , which expresses how the Gibbs  
 121 free energy of the system changes as one solute molecule is added to the solvent  
 122 at a fixed position. Eq. (5) is based on this definition, namely

$$v_s^* = \left( \frac{\partial \mu^*}{\partial P} \right)_T. \quad (6)$$

123 We recall that excess quantities in this work are defined with respect to an ideal  
 124 solution in which all molecular interactions are turned off [3, 5], i.e. the ideal  
 125 gas, as shown in Eq. (2). Thus,  $\mu^*$  coincides with the pseudochemical potential  
 126 defined by Ben-Naim [3].

## 127 2.2. Decomposition of $v_s^*$ in exclusion volume and $\Delta V_{AIC}$

128 The formation of a cavity implies the definition of an exclusion volume ( $V_0$ ) for  
 129 the motion of solvent centers, from which there arises the natural following de-  
 130 composition of  $v_s^*$ , namely

$$v_s^* = V_0 + \Delta V_{AIC} \quad (7)$$

131 where  $\Delta V_{AIC}$  is the difference between  $v_s^*$  and the exclusion volume. On the  
 132 basis of the direct method (Eq. (4)),  $\Delta V_{AIC}$  can be seen as the variation in volume

133 between the solution and the pure solvent "measured" by the center of the solvent  
134 molecule. This quantity has been defined as a *non-ideal* contribution [11, 15],  
135 with reference to an ideal condition that cannot be confused with the conventional  
136 reference in thermodynamics [3].

137 The exclusion volume has been considered as an *intrinsic* contribution to the  
138 excess volume. However, as already discussed by Matubayasi and Levy [11], his-  
139 torically, the term *intrinsic volume* has been used to indicate the van der Waals  
140 volume of the solute. This is the reference [42] for the non-intrinsic contribution  
141 used by Graziano [43, 44], which does not correspond to the non-ideal contri-  
142 bution used in a previous work [15]. In order to avoid further confusion, in this  
143 work, a new notation is introduced, in which the acronym AIC stands for "all in-  
144 teractions coupled". Hence,  $\Delta V_{AIC}$  denotes the volume change when water-water  
145 interactions are coupled after an exclusion volume has been defined. This can be  
146 associated with a hard-sphere solute-solvent interaction potential defined by the  
147 contact distance  $R$ . In this case,  $R$  can be written as the sum of solute and sol-  
148 vent radii. For this reason, the study of cavity formation in water is relevant for  
149 hydrophobic solvation. However, here such an association is not strictly neces-  
150 sary, and one can think in terms of a void contained inside the exclusion region.  
151 Thus, in the present work, only when interpreting the results with reference to the  
152 "intrinsic volume of the solute", was a cavity void volume,  $V_{cv}$ , estimated as the  
153 spherical volume of radius  $R - r_w$  for an assumed value of  $r_w$ , the radius of a  
154 water molecule.

155 The decomposition of  $v_s^*$  according to Eq. 7 has been strongly criticized by  
156 Graziano [43, 44], but, once again, it is worthwhile stressing that this is natural

157 for the systems studied in the present and previous works [15, 45, 46]. The main  
 158 reason is that the cavity is defined by the exclusion volume. A clarification of the  
 159 meaning "non-ideal" when referring to  $\Delta V_{AIC}$  is given below.  
 160 Precisely, for a spherical cavity that excludes a solvent center from the spherical  
 161 volume  $V_0 = \frac{4\pi}{3}R^3$ , according to the KB integral (Eq. (1)),  $\Delta V_{AIC}$  is zero in  
 162 the case of a cavity-solvent correlation function described by a Heaviside step  
 163 function, which is expected for a cavity in an ideal gas [47]. Thus, it takes into  
 164 account the real cavity-solvent correlation function and is related to the excess  
 165 number of solvent molecules at the cavity surface, i. e. at the accessible surface  
 166 [45, 48, 46],

$$n_s(R, R) = -\rho\Delta V_{AIC} \quad (8)$$

167 where  $\rho$  is the solvent number density. From this quantity, the solvent adsorption  
 168 at the same reference surface is readily obtained,

$$\Gamma = \frac{n_s(R, R)}{4\pi R^2}. \quad (9)$$

169 This is an absolute adsorption and strongly depends on the position of the refer-  
 170 ence or dividing surface. Originally, this quantity has been introduced within the  
 171 thermodynamics of interfaces in the Gibbs approach, which assumes homogenous  
 172 phases up to the dividing surface [49]. As a real interface is dishomogenous, an  
 173 excess number of molecules is defined for a particular dividing surface. Here, this  
 174 surface excess quantity arises from the discrepancy between the real solvent dis-  
 175 tribution around the cavity with respect to an "ideal" distribution defined by the  
 176 position of the dividing surface, i.e. a Heaviside function.

177 *2.3. Solvent and Excess Compressibility*

178 An expression for the coefficient of isothermal compressibility can be derived  
 179 from density in accordance with the thermodynamic definition:

$$k_T^\circ = -\frac{1}{V} \left( \frac{\partial V}{\partial P} \right)_T = \frac{1}{\rho} \left( \frac{\partial \rho}{\partial P} \right)_T. \quad (10)$$

180 This can be compared with volume fluctuation obtained from NPT simulations,  
 181 namely,

$$k_T^\circ = -\frac{\langle V^2 \rangle_N - \langle V \rangle_N^2}{k_B T \langle V \rangle_N}. \quad (11)$$

182 Similar definitions apply to solutions. How solvent compressibility is affected by  
 183 the solute can be evaluated directly from the difference in compressibility between  
 184 the infinitely dilute solution and the pure solvent. When this difference refers to  
 185 the addition of 1 mol of solute it defines the partial molar compressibility [17].  
 186 However, as we are much more interested in the pressure derivative of volume  
 187 variation, we consider what it is known in biophysics as the change in apparent  
 188 volume compressibility [29]. In the case of a fixed solute position, this quantity  
 189 refers to the negative pressure derivative of the excess volume,

$$\Delta K_T = - \left( \frac{\partial v_s^*}{\partial P} \right)_T \quad (12)$$

190 and multiplied by the solvent density it corresponds to the excess compressibility  
 191 defined by Matubayasy and Levy [11]. According to the definition given above,  
 192  $\Delta K_T$  differs from the partial molar isothermal compressibility [17] only for con-  
 193 tributions of solute translational degrees of freedom, and it can be obtained from

194 simulation results on system volumes and isothermal compressibilities of pure  
195 solvent and solution,

$$\Delta K_T = k_T \langle V(1, N_w) \rangle - k_T^\circ \langle V(0, N_w) \rangle . \quad (13)$$

### 196 **3. RESULTS AND DISCUSSION**

#### 197 *3.1. Computational details*

198 NPT Monte Carlo (MC) simulations were run at 298 K for hard-sphere cavities in  
199 512 TIP4P waters. The center of the cavity was at a fixed position, so that in this  
200 case excess volumes were obtained by the direct method (Eq. (4)). To this end,  
201 the average volume occupied by the same number of TIP4P waters was used [35].  
202 KB integrals were computed from cavity-solvent rdfs relative to the water-oxygen  
203 center. In order to avoid systematic errors due to consideration of the whole vol-  
204 ume, including the exclusion volume  $V_0$ , rdfs from Boss [50] were renormalized  
205 by scaling them by  $\langle V(0, N_w) \rangle / \langle V(1, N_w) \rangle$ .

#### 206 *3.2. Simulation Results*

207 Two main aspects of the effect of increasing pressure are focused on: (1) the scal-  
208 ing of the cavity radius at a constant high pressure, 8000 *atm*, shows significantly  
209 different features in comparison to the same process at 1 *atm*; (2) the profile  
210 along the isotherm of the excess volume and its slope is shown for two cavities  
211 with contact radius of 2.85 and 6.05 Å.

##### 212 *3.2.1. Radial scaling of the cavity: effect of increasing P on $\Delta V_{AIC}$ and asymp-* 213 *totic adsorption*

214 Results relative to the scaling of the cavity radius at 8000 *atm* are collected in  
215 Table 1 for  $v_s^*$  computed by using the direct method (Eq. (4)) together with com-  
216 pressibility deviation from pure water compressibility,  $k_T - k_T^\circ$ , and the excess

Table 1: Excess quantities of some hard-sphere cavities in water at 298.15 K and 8000 atm from NPT MC simulations in 512 TIP4P waters. Solutes were at a fixed position.  $v_s^*$  obtained by the direct method (Eq. 4). The numbers in parentheses are the statistical uncertainties in the last digit.

$r$	$v_s^*$	$\delta v_s^{*(a)}$	$10^6(k_T - k_T^\circ)^{(b)}$	$-\left(\frac{\partial v_s^*}{\partial P}\right)_T^{(c)}$
Å	$cm^3 mol^{-1}$	$cm^3 mol^{-1}$	$atm^{-1}$	$cm^3 mol^{-1} atm^{-1}$
1.60	0.6(4)	0.0047(5)	-0.19(2)	-0.0014(1)
1.75	1.6(4)	0.0041(5)	-0.17(2)	-0.0012(1)
1.90	2.3(5)	0.0050(5)	-0.21(2)	-0.0015(1)
2.25	5.4(4)	0.0048(5)	-0.20(2)	-0.0014(1)
2.55	10.0(4)	0.0047(5)	-0.19(2)	-0.0013(1)
2.85	17.7(4)	0.0039(5)	-0.16(2)	-0.0009(1)
3.30	33.6(4)	0.0030(5)	-0.12(2)	-0.0004(1)
3.65	51.2(4)	0.0038(5)	-0.16(2)	-0.0004(1)
4.05	78.5(4)	0.0022(5)	-0.09(2)	0.0005(1)
4.45	112.9(4)	0.0029(5)	-0.11(2)	0.0007(1)
5.05	182.4(4)	0.0031(5)	-0.13(2)	0.0017(1)
5.45	242.2(4)	0.0013(5)	-0.05(2)	0.0031(1)
6.05	353.7(4)	0.0052(5)	-0.21(2)	0.0035(1)

(a) systematic deviation of values obtained by Eq. 4 from values obtained by Eq. 5 evaluated as  $(k_T^\circ - k_T) * k_B T$  (see Eqs. 11-13 of Ref. [17])

(b)  $k_T$  and  $k_T^\circ$  from volume fluctuations (Eq. 11).

(c) obtained by Eq. 13.

Table 2: Excess volumes ( $v_s^*$ ) at 1 atm and 298.15 K for some cavities in water and effect of increasing the pressure up to 8000 atm ( $\Delta v_s^*$ ). Results obtained by Eq. 4 from NPT MC simulations in 512 TIP4P waters where oxygens were excluded from the spherical volume of radius  $R$  ( $V_0$ ). The additional contribution from correlations following the coupling of all interactions in the system ( $\Delta V_{AIC}$ ) is given for the system at 1 atm. Also contributions relative to the decomposition with reference to spherical volume of radius  $R - r_w$  ( $V_{cv}$ ) are for systems at atmospheric pressure. The numbers in parentheses are the statistical uncertainties in the last digit. Radii in Å and volumes in cc/mol.

$R$	$v_s^*$ <sup>(a)</sup>	$\Delta v_s^*$ <sup>(b)</sup>	$V_0$	$\Delta V_{AIC}$ <sup>(a)</sup>	$R - r_w$ <sup>(c)</sup>	$V_{cv}$ <sup>(d)</sup>	$v_s^* - V_{cv}$ <sup>(a)</sup>
2.85	24.9(7)	-7.2(8)	58.4	-33.5	1.47	8.0	16.9
3.30	47(3)	-13(3)	90.7	-44	1.92	17.9	29
4.05	108(2)	-29(2)	167.6	-60	2.67	48.0	60
4.45	162(2)	-49(2)	222.3	-60	3.07	73.0	89
5.05	252(1)	-69(1)	324.9	-73	3.67	124.7	127
5.45	335(1)	-93(1)	408.3	-73	4.07	170.1	165
6.05	485(2)	-131(2)	558.6	-74	4.67	256.9	228

(a)  $P = 1$  atm

(b)  $\Delta v_s^* = v_s^*(8000 \text{ atm}) - v_s^*(1 \text{ atm})$

(c)  $r_w = 1.38 \text{ \AA}$

(d) spherical volume of radius  $R - r_w$

217 volume compressibility defined by Eq. (12) and computed by Eq. (13). Discrep-  
218 ancies with respect to Eq. (5),  $\delta v_s^*$  (third column), were derived from  $k_T^\circ - k_T$ .  
219 These are systematically positive and very small with regard to statistical uncer-  
220 tainties on  $v_s^*$ . Similar results have been obtained for methane in water [17]. Data  
221 of  $\Delta K_T$  ( last column of Table 1) obtained from Eq. 13 give interesting depen-  
222 dence on the cavity radius for the slope of the excess volume (Eq. (12)). Ac-  
223 cording to these results, at 8000 atm, the excess volume of a specific radius can  
224 increase or decrease with increasing pressure depending on whether the radius is  
225 less or greater than about 3.9 Å, for which a stationary point may be expected.  
226 Throughout the range, excess volumes at 8000 atm are generally significantly

Figure 1: Dependence on the cavity radius ( $R$ ) at 1 atm (black filled circles) and 8000 atm (blue filled squares) for the excess volume ( $v_s^*$ ) obtained by the direct method (Eq. 4) from NPT MC simulations at 298 K. The green curve represents the excluded volume ( $V_0$ ) while the red line is the volume of the cavity void ( $V_{cv}$ ), i.e. the spherical volume of radius  $R - r_w$ .

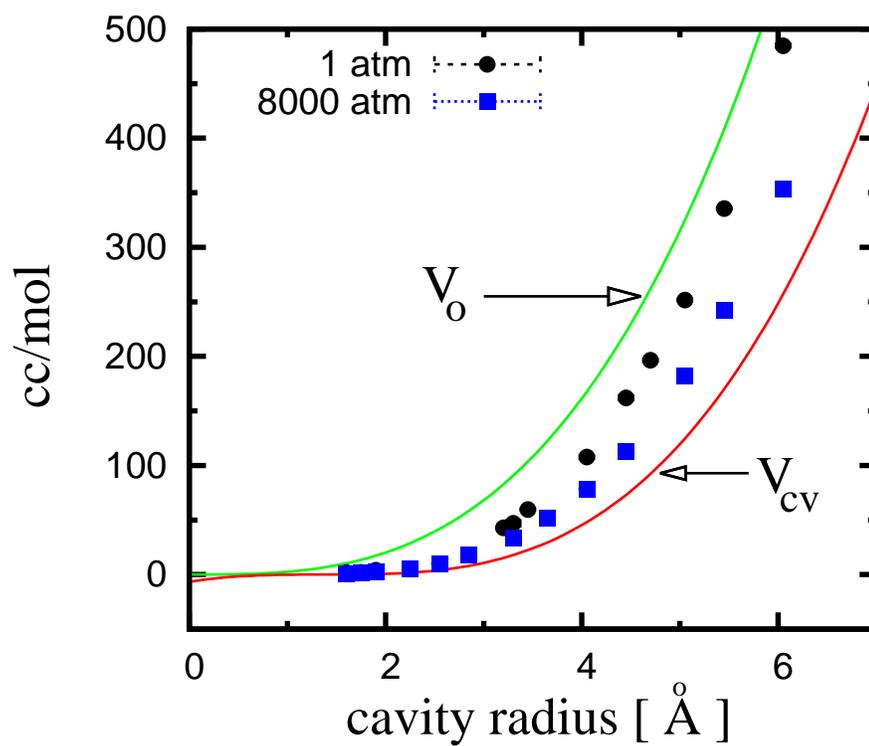
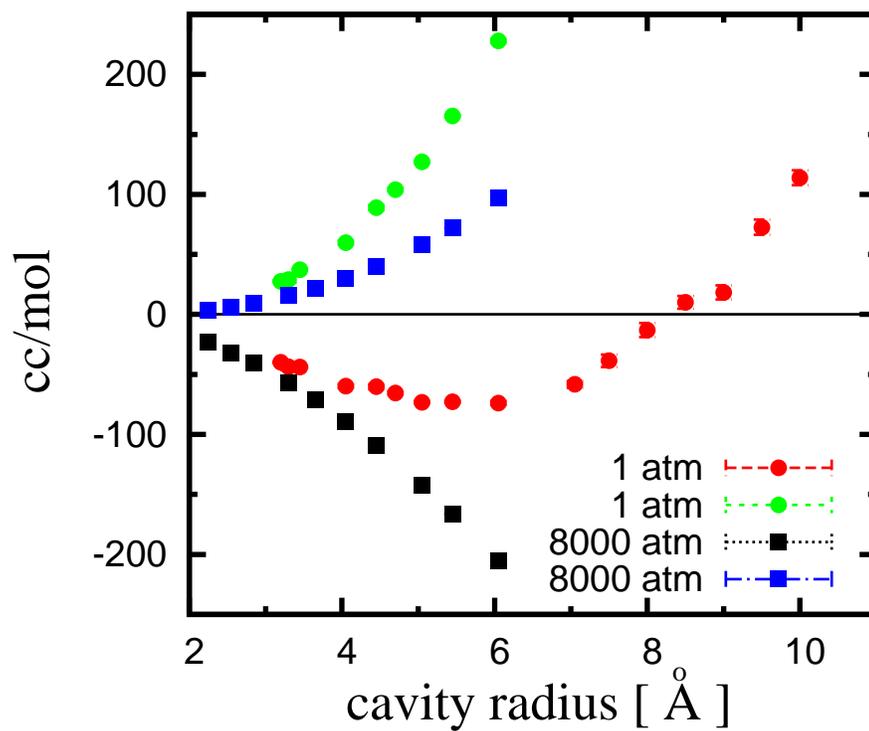


Figure 2: Dependence on the cavity radius ( $R$ ) of  $\Delta V_{AIC}$  (Eq. 7) at 1 atm (red filled circles) and 8000 atm (black filled squares). Contributions to the excess volume obtained as the difference  $v_s^* - V_{cv}$  are also shown at 1 atm (green filled circles) and 8000 atm (blue filled squares). In both decompositions,  $v_s^*$  were computed by the direct method (Eq. 4).



227 reduced with respect to those obtained at atmospheric pressure which were pre-  
228 sented and discussed in a previous work [15]. This is shown in the third column  
229 of Table 2 and in Fig. 1. For an excluding cavity radius  $R$  up to  $6.05 \text{ \AA}$ , results  
230 of both pressures are in between the volume of the cavity void ( $V_{cv}$ ) and the ex-  
231 clusion volume ( $V_0$ ). Thus, in the range plotted in the figure, results come up to  
232 Graziano’s expectations [43, 44], which have been based on empirical schemes  
233 employed in rationalizing partial molar volumes of various solutes [38]. For more  
234 discussion on this point, see also Section 3.3.1. The decomposition of  $v_s^*$  with  
235 respect to  $V_0$  or  $V_{cv}$  yields rather different contributions which for both pressures  
236 are plotted in Fig. 2. For  $R$  within  $6.05 \text{ \AA}$ , values at atmospheric pressure are also  
237 reported in the fourth and in the last column of Table 2, respectively. In this range,  
238 at both pressures, even the sign of the two ”non-intrinsic” contributions is differ-  
239 ent. This is not surprising, as the cavity void is much smaller than the exclusion  
240 volume.

241 For cavities at  $1 \text{ atm}$  [15, 51], comparison between methods to compute  $v_s^*$  re-  
242 vealed the importance of  $\Delta V_{AIC}$  ( $v_s^* - V_0$ ), as this *non - ideal* contribution is  
243 related to solvent correlation around the cavity. The scaling of cavity radius pro-  
244 duces interesting features regarding the radial profile of this quantity, with a crit-  
245 ical point between  $5$  and  $6 \text{ \AA}$  and an inversion of sign between  $8$  and  $10 \text{ \AA}$  (Fig.  
246 2). Although in quantitative disagreement in this range, methods based on sim-  
247 ulations give the same trend of results with  $R$ , while methods based on models  
248 [15, 30], can or cannot reproduce such behaviour. This mainly shows a positive  
249  $\Delta V_{AIC}$  for nanometric-sized cavities to which there corresponds a negative ad-  
250 sorption at the accessible reference surface [45, 46]. This can be justified on the

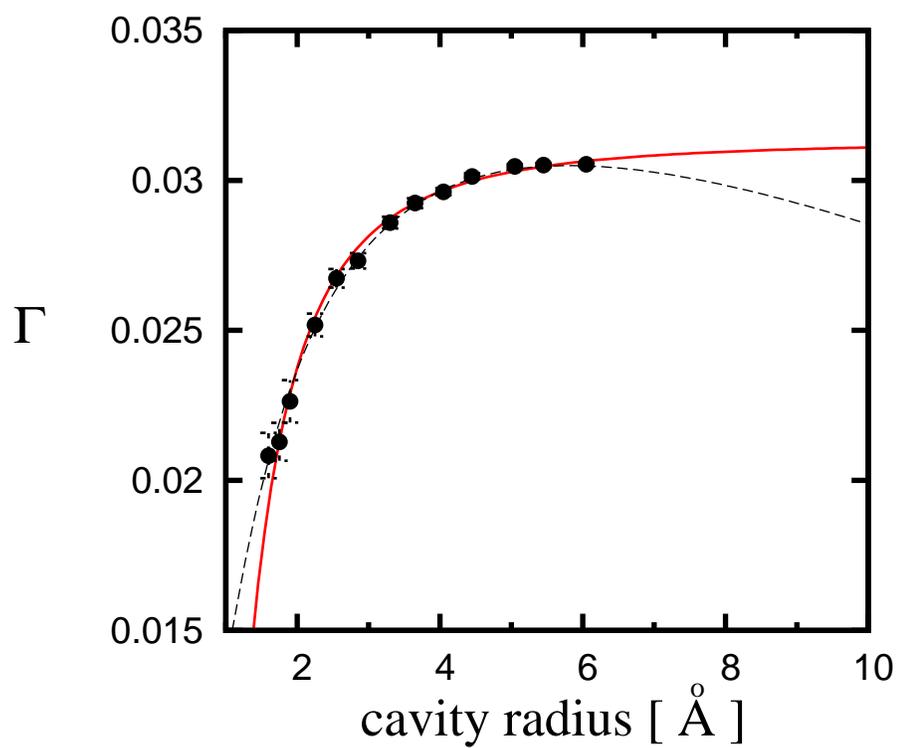
251 basis of conditions near to vapor-liquid equilibrium, and transition to positive ad-  
252 sorption appears reasonable when increasing pressure [30]. This view has been  
253 proven valid for cavities in water [15, 45, 30], and in LJ liquids [30]. Thus, fitting  
254  $\Delta V_{AIC}$  against the cavity radius at atmospheric pressure [45], negative adsorp-  
255 tion at the cavity accessible surface was extrapolated for nanometric and larger  
256 cavities. At the same time, the sign of this quantity was confirmed by examining  
257 two possible evolutions of the cavity-water rdf in the limit of a very large cav-  
258 ity. The extrapolated profile was compared with gas/liquid and wall/liquid density  
259 profiles, showing that it is sharper, but with a thickness similar to that obtained for  
260 a phobic wall. In the same limit, LCW [52] theoretical results obtained by Huang  
261 and Chandler [53] have shown a density profile with a thickness very similar to  
262 those obtained from simulations of the gas/liquid interface obtained with TIP4P  
263 and SPC/E models. Hence, as a consequence of a more dewetted density profile,  
264 adsorption at the accessible dividing surface is more negative than that extrapo-  
265 lated from our data [15, 45]. For a detailed comparison of cavity-water rdfs see  
266 [45]. Such a discrepancy has already been evident for a cavity radius  $R$  of 100 Å.  
267 However, the opposite occurs for  $R$  less than 20 Å, at which profiles are very sim-  
268 ilar. On the basis of this, when inserting these rdfs in the KB integrals a change  
269 of sign for  $\Delta V_{AIC}$  is also expected for LCW theoretical results, even if this likely  
270 occurs at  $R$  between 8 Å and 20 Å .  
271 In the previous work [15], it was shown that SPT and BMCLS never predict such a  
272 change of sign. This has been claimed by Graziano [43, 44] as a fundamental point  
273 in contrast with conclusions of previous works [15, 45]. However, as already noted  
274 [15], when enlarging the cavity radius, SPT disagrees with simulation results also

275 for thermodynamic quantities, such as the enthalpic and the entropic contribution  
276 to the change of free energy associated with the cavity formation in TIP4P water  
277 [54]. To be precise, these simulation results indicate that for  $R$  larger than 4  
278 Å, the cost of cavity formation is dominated by a positive variation of enthalpy.  
279 This is in line with ideas expressed in the literature for the process at ambient  
280 conditions [55]. The change of sign of  $\Delta V_{AIC}$  is clearly related to dewetting  
281 and a nanometric sized cavity is considered dewetted. It seems well founded  
282 that around 8-10 Å there is the crossover between "wet" and "dewetted" cavities,  
283 which is accompanied by a change in the thermodynamic of the process [55].  
284 Turning to the scaling of the cavity radius at 8000 atm,  $\Delta V_{AIC}$  (Fig. 2) shows  
285 a monothonic decrease and is expected to be always a negative quantity, and a  
286 positive adsorption of water-oxygen centers is obtained at the cavity surface (Fig.  
287 3). As for the contact value of rdf observed at this pressure [15], it seems reason-  
288 able to consider that at  $\sim 6$  Å also this quantity practically converges to a constant  
289 value. On the basis of this assumption, the asymptotic value of adsorption would  
290 be positive in contrast with that predicted for the scaling at 1 atm. This very  
291 different behaviour was observed in conjunction with very "wet" cavity surfaces  
292 at high pressure [35]. Therefore, KB integrals provide a useful interpretation of  
293 these results (see Section 3.2.2).  
294 The effect of increasing pressure on the thermodynamics of cavity formation re-  
295 quires further investigation and is beyond the scope of this work. However, it  
296 is worthwhile mentioning results from the analysis made by Kalinichev et al.  
297 [56] on pure water described by the same intermolecular potential used in this  
298 work (TIP4P). They have observed that the structure and the energy of hydrogen

299 bonds is only slightly affected by compression up to 10000 atm along the 298  
300 K isotherm. In addition, a redistribution of interaction energies has been found,  
301 with increase in the number of pairs with repulsive and "weakly-bonded" inter-  
302 actions. This suggests that the unfavourable entropic contribution due to packing  
303 might be much more important when creating the cavity at high pressure. Under  
304 the assumption that this is the dominant effect, SPT would be able to describe the  
305 properties of cavities in water. However, it was found [35] that SPT gives incor-  
306 rect radial scaling of the contact value of the cavity-oxygen rdf for cavities with  
307 excluding radii  $R$  up to  $\sim 6 \text{ \AA}$ . In contrast, at larger radii a strong reduction of the  
308 the parameter defining the size of a water molecule is necessary to converge to the  
309 curve that correctly describes simulation results. From this it may be inferred that  
310 the packing effect would be dominant for nanometric and larger cavities, differ-  
311 ently from what has been supposed at atmospheric pressure [57, 58, 59, 60].  
312 At the same time, at high pressure, the energetic contribution can be supposed  
313 to be less unfavourable than at atmospheric pressure. Nevertheless, this needs  
314 to be ascertained by a direct analysis on the cavity-water system. Certainly, in-  
315 stead there is a striking effect on the variation of enthalpy included in the variation  
316 of the pressure-volume term. It is well known that enlarging the cavity at atmo-  
317 spheric pressure [55, 35], the pressure-volume term is negligible up to  $R$  of several  
318 nanometers. In contrast, for the same process at 8000 atm, even a variation of the  
319 excluding cavity radius  $R$  from  $\sim 4 \text{ \AA}$  to  $\sim 6 \text{ \AA}$  would involve a pressure-volume  
320 increase of some hundreds of KJ/mol, which is likely greater than the variation in  
321 energy [54].

322

Figure 3: Adsorption  $\Gamma$  ( $\text{\AA}^{-2}$ ) at the cavity surface versus the cavity radius ( $\text{\AA}$ ) obtained by using the direct method to compute  $v_s^*$  (points with error bars). Lines represent results from fitting  $v_s^*$  with Eq. 14 (dashed black lines) and with Eq. 15 (red line).



323 *3.2.2. Radial scaling of the cavity: analysis of  $\Delta V_{AIC}$  from KB integrals*

324 For cavities at 8000 atm,  $\Delta V_{AIC}$  obtained by using the direct method is compared  
325 in Fig. 4 with results from KB integrals. As in the case of cavities at 1 atm, these  
326 methods based on simulations agree on the radial dependence of this quantity and  
327 generally show small discrepancies, even though these were found to be signifi-  
328 cant for a nanometric cavity. Approximations based on a different truncation of  
329 the integral are possible. Among these are hydration shell models [11, 36, 15]  
330 corresponding to the truncation at the first, second, and, when possible, the third  
331 minimum of the rdf. The results shown in the figure were obtained by using the  
332 alternative model proposed in [15]. This approximation can be justified by the  
333 oscillatory behaviour of the integral versus the truncation radius, and it estimates  
334  $\Delta V_{AIC}$  at the average value between the distances corresponding to the last critical  
335 points of the integral.

336 Interestingly, as depicted in Fig. 5 for different cavity radii  $R$ , the integrals show  
337 very close positions for critical points when plotted versus  $R_t - R$ ,  $R_t$  being the  
338 truncation radius. At the first minimum of each curve, the integral includes con-  
339 tributions due to centers closer to the center of the cavity, more precisely, those  
340 with distances up to that at which the cavity-solvent rdf crosses the ideal correla-  
341 tion (see Section 2.2). All the other critical points of curves similarly correspond  
342 to distances of water-oxygens from the center of the cavity at which  $g(r) = 1$ .  
343 Mainly, the damped oscillating curves differ for amplitude, which is greater for  
344 larger cavities. At each level of approximation,  $\Delta V_{AIC}$  is negative, as was ob-  
345 served at atmospheric pressure for  $R$  up to 9 Å, while for larger cavities, this  
346 was found only at the first shell approximation level. Indeed, the inclusion of the

347 second shell contribution was determinant in the inversion of sign. For a more  
348 detailed analysis see Ref. [15].

349 It can be noted (see Fig. S1 in Supplementary Data (SD)) that the first hydration  
350 shell gives a large contribution to  $\Delta V_{AIC}$ . Discrepancies with respect to the best  
351 estimated values can be negative or positive and are within 10-25 %. However,  
352 a high pressure determines very well defined shells that bring to very significant  
353 negative contributions also from the second peak of the rdf. Still more impor-  
354 tant than that found at atmospheric pressure [15, 51] is that, even if more distant  
355 solvent centers are less correlated to the cavity center, the corresponding smaller  
356 deviations of  $g(r)$  from 1 have weights in the integral that increase as  $4\pi r^2$ .

357 In the NPT ensemble, the excess volume is a local quantity [11, 36, 15, 5], i.e.  
358 molecules very far from the center of the solute do not give any contribution.  
359 This applies also to cavities in water and is clearly shown by examining  $\delta V_{AIC}$ ,  
360 which represents  $\Delta V_{AIC}(R_t)$  normalized to the average number of molecules ly-  
361 ing within the truncation radius  $R_t$ . As an example, in Fig. 6, profiles are shown  
362 for some cavity radii at 1 and 8000 *atm*. The quantity is very sensitive to the  
363 cavity-solvent correlation and is reduced to a small value for molecules which are  
364 three molecular diameters away from the cavity surface. The striking effect of in-  
365 creasing pressure is particularly evident for the larger cavity studied at 8000 atm,  
366 with a significant increase of the negative contribution for solvent centers closer  
367 to the cavity center. This is a consequence of a very different cavity-oxygen rdf,  
368 which has higher contact values [45, 35] at 8000 atm. The arrows in the figure  
369 indicate the direction of increasing  $R$ , which is opposite at the two pressures.  
370 When this is done at atmospheric pressure, the cavity surface becomes less wet

371 and  $\delta V_{AIC}$  is less negative for centers closer to the cavity. For a nanometric cav-  
372 ity, this quantity is positive as a consequence of  $g(R) < 1$ . Nevertheless, when  
373 increasing the truncation radius, it becomes negative and then again positive. The  
374 first change in sign is due to contributions related to the peak of the rdf, which in  
375 this case is shifted with respect to the contact distance. When the truncation radius  
376 coincides with the first minimum of the rdf,  $\delta V_{AIC}$  is small and negative, while  
377 at a slightly larger  $R_t$  it becomes positive. In all other cases shown, which corre-  
378 spond to cavities for which the excess volume is less than the exclusion volume,  
379 the contribution per molecule is instead always negative.

### 380 3.2.3. *Dependence on pressure of excess volumes and excess compressibility*

381 Here, simulation results of  $v_s^*$  and its slope along the isotherm (298 K) are dis-  
382 cussed for two specific cavities. These can host a spherical solute approximately  
383 as large as a water molecule ( $R = 2.85 \text{ \AA}$ ) and slightly larger than a fullerene  
384 molecule ( $R = 6.05$ ).

385 Data of  $v_s^*$  obtained by the direct method at several values of pressure along the  
386 isotherm are plotted in Fig. 7 (a) and Fig. 8 (a). In both cases this quantity mainly  
387 decreases when pressure increases, even if there is a strong dependence on cavity  
388 size regarding the range of variation. Over 10000 atm, this range changes from  
389 about 10 to 130 cc/mol in passing from a contact radius of 2.85 to 6.05  $\text{\AA}$ . These  
390 data suggest that profiles of  $v_s^*$  along the isotherm should have a negative slope and  
391 this is much larger for the larger cavity. This implication is confirmed by slopes  
392 obtained by Eq. (13) from simulation results of isothermal compressibilities of  
393 pure water and the solution of hard-sphere solutes (see Fig. 7 (b) and Fig. 8 (b)).  
394 Looking more in detail, it can be noted that the decreasing of  $v_s^*$  along the

Figure 4: Dependence on the cavity radius ( $R$ ) at 8000 atm for  $\Delta V_{AIC}$ , the non-ideal correlation contribution to the excess volume ( $v_s^*$ ). NPT Monte Carlo simulation results from the direct method (Eq. 4) (filled circles) are fitted with (Eq. 15) and compared with results from KB integrals (Eq. 1).

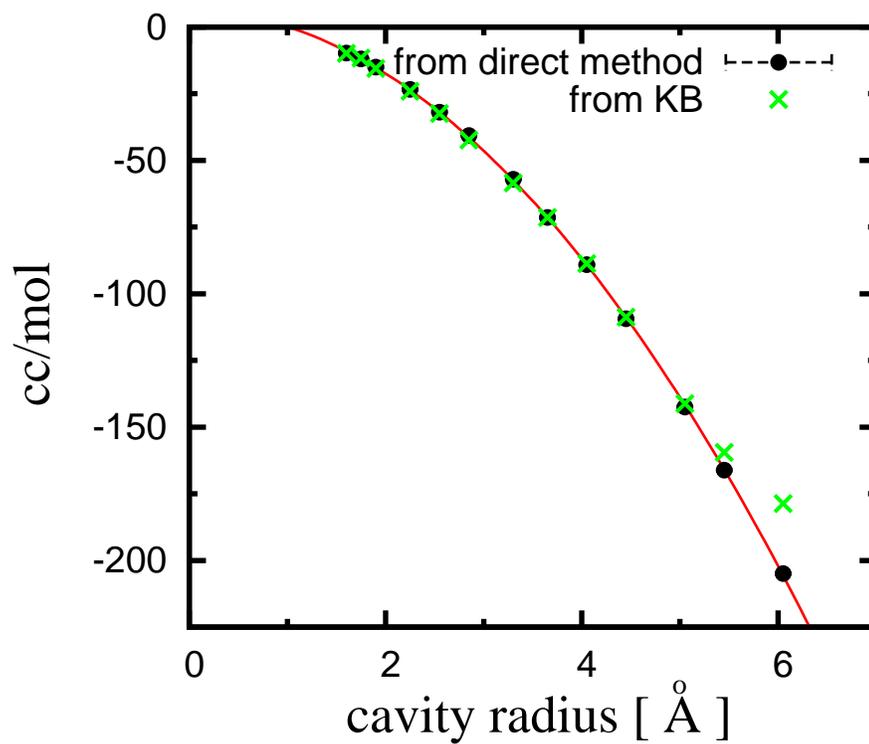


Figure 5: Results of  $\Delta V_{AIC}$  at 8000 atm from the KB integral ( $\Delta V_{AIC} = -KB - V_0$ ) as function of the truncation radius ( $R_t$ ) in the integral plotted versus  $R_t - R$  for cavity radii ( $R$ ) from 1.6, to 6.05 Å. The arrow shows the direction of increasing  $R$ . For the largest cavity, points give values relative to the first (A), the second (B) and the third (C) shell approximations, and the value read at the average between the distances corresponding to the last critical points of the integral (D).

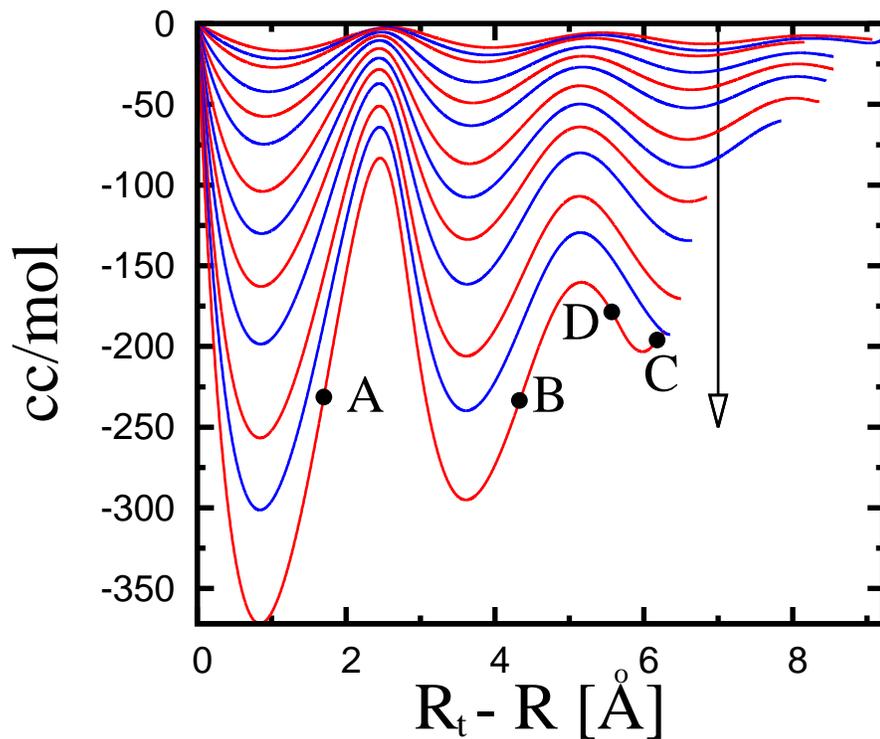
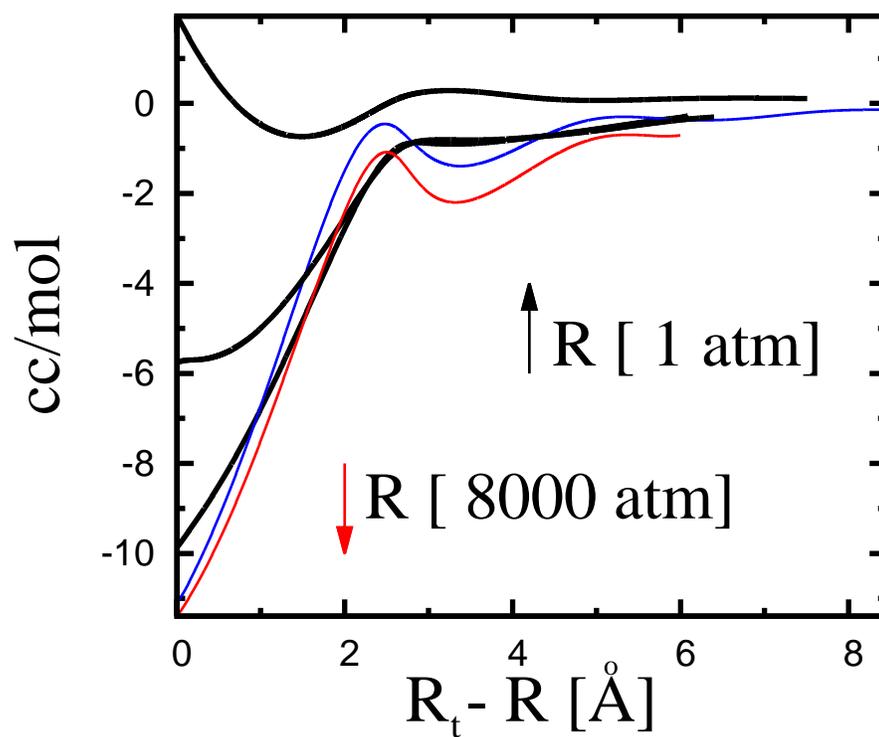


Figure 6: Pressure effect on  $\delta V_{AIC}$  for for some cavity radii as a function of  $R_t - R$ , being  $R_t$  the truncation radius in the KB integral and  $R$  the cavity radius. Results at 1 atm are represented by back lines ( $R = 2.85 \text{ \AA}$ ,  $6.05 \text{ \AA}$ ,  $10 \text{ \AA}$ ). Results at 8000 atm are represented by blue ( $R = 2.85 \text{ \AA}$ ) and red ( $R = 6.05 \text{ \AA}$ ) lines. The two arrows indicate the opposite directions of increasing  $R$ .



395 isotherm is not linear and presents, in both cases, a strong variation of slope in  
 396 the limit of low pressure. However, for  $R = 2.85 \text{ \AA}$ , dependence on pressure  
 397 appears non-monothonic, even if it is difficult to ascertain the existence of critical  
 398 points from the data. Also, results from Eq. (13) give positive slopes at 6000  
 399 and 8000 atm and this can indicate some possible inversion of slope's sign in the  
 400 curve (Fig. 7 (b)). On the contrary, for  $R = 6.05 \text{ \AA}$  slopes are negative in the  
 401 same range, even if much smaller than values obtained in the limit of low pres-  
 402 sure. This behaviour is in line with what is mentioned in Section 3.2.1 regarding  
 403 the dependence of  $\Delta K_T$  on the cavity radius when pressure is 8000 atm (Tab. 1).  
 404 Finally, some consideration must be taken of possible systematic errors in simu-  
 405 lation results of compressibility of pure water, for data at 200 and 6000 atm [35].  
 406 Moreover, in these two cases, statistical uncertainties were greater than for other  
 407 pressures. In particular,  $k_T^0$  at 200 atm is underestimated. This error brings about  
 408 overestimated values of  $\Delta K_T$ , which are out of the range shown in the figures.

### 409 3.3. Describing how $v_s^*$ depends on cavity radius and pressure

410 Models which have some theoretical foundation to compute  $v_s^*$  are based on the  
 411 pressure derivative of the pseudochemical potential ( Eq. (6)). The particular  
 412 features of the radial scaling of  $\Delta V_{AIC}$  observed in simulation results at 1 atm  
 413 are predicted neither by the approximate Scaled Particle Theory (SPT) [61] nor  
 414 by BMCLS [62, 63] expressions [15]. However, these quantities are well repro-  
 415 duced when  $\mu^*$  is described by the revised SPT expression [30]. This section deals  
 416 instead with simple heuristic models in order to fit simulation results of excess  
 417 volumes.

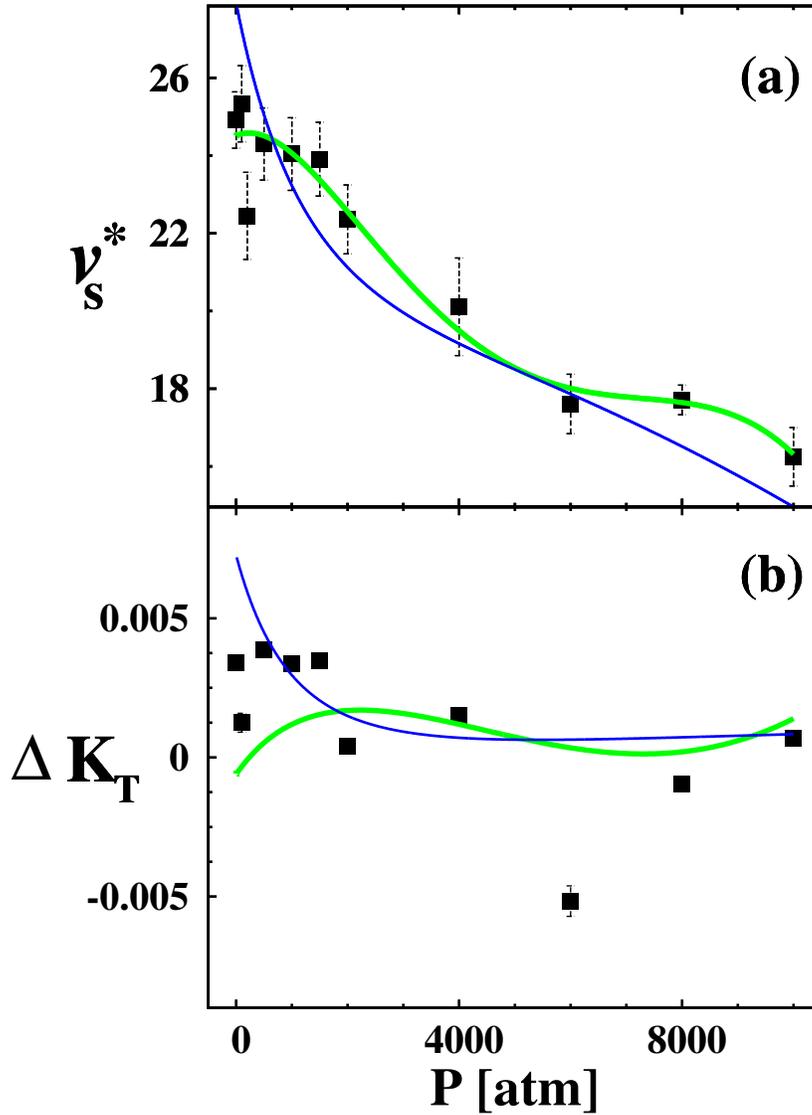


Figure 7: (a) Simulation results of  $v_s^*$  (cc/mol) computed by the direct method (points with error bars) for a cavity radius of 2.85 Å in TIP4P water plotted versus pressure. Lines represent results from fits of quantities related to average accessible volumes in pure water and in the solution with Eq. (16) (line green) and with Eq. (17) (line blue). (b) The negative pressure derivative of  $v_s^*$  (cc/(mol atm)) vs pressure obtained from simulation results of volumes and compressibility Eq. (13) (points with error bars) and from Eq. (12) using expressions derived from Eq. (16) (line green) and Eq. (17) (line blue).

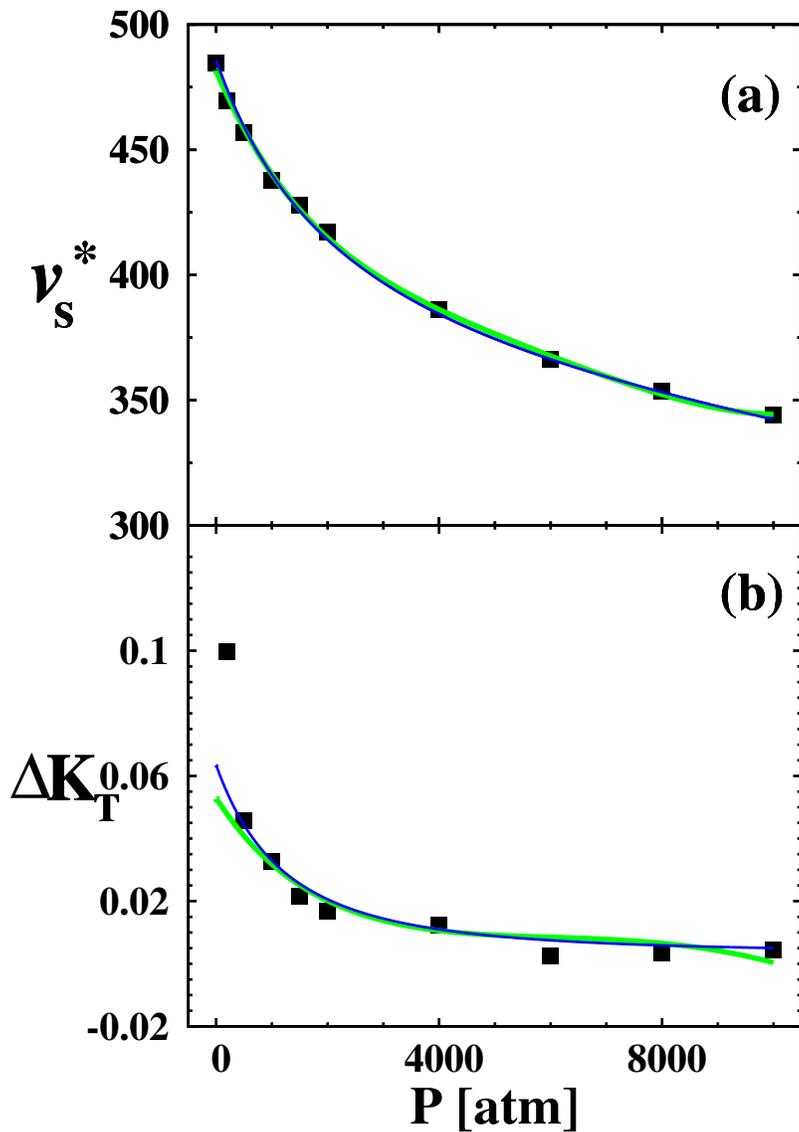


Figure 8: (a) Simulation results of  $v_s^*$  (cc/mol) computed by the direct method (points with error bars) for a cavity radius of 6.05 Å in TIP4P water plotted versus pressure. Lines represent results from fits of quantities related to average accessible volumes in pure water and in the solution with Eq. (16) (line green) and with Eq. (17) (line blue). (b) The negative pressure derivative of  $v_s^*$  (cc/(mol atm)) vs pressure obtained from simulation results of volumes and compressibility (Eq. (13)) (points with error bars) and from Eq. (12) using expressions derived from Eq. (16) (line green) and Eq. (17) (line blue).

418 *3.3.1. Fitting  $v_s^*$  against cavity radius at constant pressure*

419 At constant pressure, the radial dependence of  $\Delta V_{AIC}$ , and namely  $v_s^*$  can be  
 420 described by a very simple expression that is able to fit both, data at 1 atm and at  
 421 8000 atm, namely

$$v_s^* = C \left( \frac{4}{3} \pi \right) (a + b R)^3 \quad (14)$$

422 where  $C$  is a conversion factor from  $\text{\AA}^3$  to  $\text{cm}^3 \text{mol}^{-1}$ . Precisely, at 1 atm,  $a =$   
 423  $-0.98(6) \text{ \AA}$  and  $b = 1.12(2) \text{ \AA}$  were found in our previous work [48, 46] while,  
 424 at 8000 atm,  $a = -1.018(5) \text{ \AA}$  and  $b = 1.0274(1) \text{ \AA}$  were found for the results  
 425 presented in this work and shown in Table 1. However, Eq. (14) does not fulfill  
 426 the requirement of a constant adsorption at infinity [64], except in the case of  
 427  $b = 1$ . For this reason in previous works [45, 48, 46], by scaling to further larger  
 428 radii, a quadratic polynomial was adopted for  $n_s$  and consequently for  $\Delta V_{AIC}$ .  
 429 This model inserted in Eq. (7) gives

$$v_s^* = C \left( \frac{4\pi}{3} R^3 + a_2 R^2 + a_1 R + a_0 \right). \quad (15)$$

430 It can be emphasized that a constant value of adsorption at the accessible dividing  
 431 surface in the limit of an infinite radius is consistent with convergence of the con-  
 432 tact value of  $g(r)$  to  $P/(\rho K_B T)$  in the same limit. Both convergence requirements  
 433 are fulfilled also by Eq. (14) when, for  $b = 1$ , it reduces to a particular case of Eq.  
 434 (15). Adsorption from simulation results at 8000 atm (Fig. 3) appears to converge  
 435 fast to a positive constant value. Both equations here discussed fit well the data,  
 436 but lead to very different extrapolations outside the range (see also Fig. S2 in SD).  
 437 With  $b = 1$ , Eq. (14) reduces to the expression [42] that has been used for the ”  
 438 cavity volume” deduced using SPT from experimental excess volumes of solutes

439 in water [65]. In order to obtain the so called "border thickness" parameter [65,  
440 44],  $R$  is written as the sum of two radii, i.e.  $R = r_c + r_w$ , for a chosen value  
441 of  $r_w$  ( 1.38 Å), whose pressure dependence was neglected. At 8000 atm, the  
442 optimal value of parameter  $a$  is -0.876 Å that corresponds to a "border thickness"  
443 of 0.505 Å. The performance of the fitting is not as good as that obtained when  
444 also parameter  $b$  is optimized. This is still more evident at 1 atm, for which the  
445 "border thickness" falls in the range between 0.72 and 1.38 Å, when fitting data  
446 in different ranges of  $R$ . Simulation results interpreted with this model clearly  
447 indicate that this parameter increases with the size of the cavity, at atmospheric  
448 pressure. Similar results have been obtained from the "cavity volume" extracted  
449 from experimental excess volumes of various small solutes and some globular  
450 proteins [65, 38, 66].

451 However, according to Chalikian and coworkers [66], the "border thickness" should  
452 reach a plateau of 1 Å for solutes with van der Waals radii of  $\sim 7$  Å ( $R \sim 8.4$  Å),  
453 in contrast with the larger value obtained from simulations of cavities in TIP4P  
454 water [15]. Graziano [44] argued that systematic errors in the simulations of the  
455 largest cavities [15] can explain such disagreement with SPT interpretation of ex-  
456 perimental data. Even if errors in simulations cannot be ruled out [15, 59, 45, 46],  
457 this view does not appear well founded for the following reasons: (1) the compar-  
458 ison between simulation results and those extracted from experimental data is not  
459 consistent; (2) the lack of experimental data on larger spherical solutes; (3) the  
460 "border thickness" is defined within an empirical scheme. Moreover, the overes-  
461 timated compressibility of TIP4P has been indicated as a possible source of errors  
462 in simulations, even though, one should prove that the box containing the cavity

463 is much more affected by this problem than the box of pure water. At the same  
 464 time, one should explain why excess volumes from SPT were found qualitatively  
 465 similar when using instead of experimental values, those of the TIP4P water [15].  
 466 Very recently, simulation results on repulsive spherical solutes in water at 1 atm  
 467 have confirmed that the "border thickness" increases with the solute size, and that  
 468 this is consistent with dewetting [67]. However, a smaller increase has been ob-  
 469 served when also attractive solute-water interactions have been coupled. Values  
 470 from simulation results of hydrated non-polar molecular solutes obtained by Cha-  
 471 likian and coworkers [66] have been found in between. In these cases, according  
 472 to Ashbaugh et al. [67], a larger "border thickness" does not indicate dewetting,  
 473 but is related to the assumed spherical shape when calculating the van der Waals  
 474 volume of these solutes.

### 475 3.3.2. Fitting $v_s^*$ against pressure at fixed cavity radius

476 Simple models for  $v_s^*(P)$  can follow from the two expressions proposed in a pre-  
 477 vious work [35] to fit the inverse of number density. Both have been found able  
 478 to give at the same time a good description of TIP4P water and experimental data.  
 479 One is linear in constant parameters,  $t_0, t_1, t_2, t_3$  and  $t_4$ ,

$$\frac{1}{\rho(P)} = t_0 + t_1 P + t_2 P^2 \ln(P/P_0) + t_3 P^{2.5} + t_4 P^3 \quad (16)$$

480 where  $P_0$  is the unity used for pressure, here 1 atm, while the other can be seen as  
 481 a modified Tait expression,

$$\frac{1}{\rho(P)} = \frac{1}{\rho_0} + \frac{(ab - c) \ln(bP + 1) + bcP}{b^2} \quad (17)$$

482 where the constant parameters are  $\rho_0$ ,  $a$ ,  $b$  and  $c$ . These expressions can be used  
 483 for pure water and for the corrected number density in the system containing the  
 484 cavity, i.e. to fit  $\langle V \rangle / N_w$  and  $(\langle V \rangle - V_0) / N_w$  respectively,  $N_w$  being the  
 485 number of waters in the box of simulations . Thus, the same functional form  
 486 can describe accessible volumes from which  $v_s^*$  can be obtained, as well as its  
 487 pressure derivative at a fixed cavity radius. Furthermore, because of the linearity  
 488 with respect to parameters, Eq. (16) can also be used to fit this quantity directly.  
 489 In Fig. (7) and Fig. (8), results from the heuristic expressions above are shown for  
 490 contact radii of 2.85 and 6.05 Å respectively. Overall, their performance can be  
 491 judged relatively and reasonably good, given the large range of pressure consid-  
 492 ered. In particular for the smaller cavity, Eq. (16) performs better than Eq. (17),  
 493 as already observed for pure water when interactions are described by the TIP4P  
 494 model potential [35]. Slopes of the curves qualitatively differ (Fig. 7) within the  
 495 limit of low pressure. In this range simulation results of excess volumes appear  
 496 scattered even if with values which are close to one another approximately within  
 497 statistical uncertainties. This could indicate the possible existence of a maximum  
 498 for  $v_s^*$ , as predicted by Eq. (16) ( $P = \simeq 225 \text{ atm}$ ). For methane in TIP4P, at the  
 499 same temperature, a similar trend was observed when pressure is raised, with a  
 500 clear decreasing of the excess volume only for pressures greater than 1000 *atm*.  
 501 However,  $\Delta K_T$  computed from simulation results of compressibility and average  
 502 volumes seem to indicate that  $v_s^*$  generally decreases except for between 6000  
 503 and 8000 *atm*. On the contrary, for the larger cavity, in Fig.8, the decreasing of  
 504 this quantity appears very clearly in all the range of pressure, and both heuristic  
 505 expressions predict slopes which are consistent with simulation results from Eq.

506 (13). Nonetheless, it is evident that curves can differ for relatively small quantities,  
507 which are generally within statistical uncertainties on  $v_s^*$ , but slopes can be quite  
508 different. This is in line with the general problems expected when computing  
509 derivatives.

#### 510 **4. CONCLUSIONS**

511 In this work, NPT MC simulation results of excess volumes computed by the  
512 direct method are presented for hard-sphere cavities in TIP4P water. Two main  
513 effects of increasing pressure at 298 K are investigated. The first depicts a very  
514 different behaviour of the non-ideal correlation contribution,  $\Delta V_{AIC}$ , when scal-  
515 ing the cavity radius at a constant high pressure in comparison with 1 atm. The  
516 effect is well interpreted in terms of KB integrals that involve deviations from 1  
517 of the cavity-solvent rdf. These can be positive or negative, so determining lo-  
518 cally a negative or a positive contribution to excess volume. At a constant high  
519 pressure, well defined hydration shells are maintained even when the cavity can  
520 host a solute larger than a fullerene molecule. Hence, examining adsorption at the  
521 cavity surface, it seems reasonable to assume a rapid convergence of this quantity  
522 to a positive value. On the contrary, at atmospheric pressure, negative adsorption  
523 was extrapolated for a very large cavity radius. On the basis of such a different  
524 behaviour, adsorption is expected to invert its sign at an intermediate value of  
525 pressure. In order to further investigate this point, a systematic study is necessary.  
526 This implies a large number of quite expensive simulations, or alternatively, ex-  
527 cess volumes can be obtained from Eq. (12), which is convenient when simple  
528 models are used to compute the excess chemical potential. On the other hand, the

529 sign of adsorption at the cavity surface extrapolated for an infinite radius can be  
530 relevant for their parameterization.

531 The second effect is observed at a fixed cavity radius and mainly consists in the  
532 decreasing of excess volumes with increasing pressure in a wide range (1-10000  
533 atm) along the isotherm. This is shown in two cases, for cavities that can host  
534 spherical solutes approximately as large as a water molecule and slightly larger  
535 than a fullerene molecule, respectively. However, for the smaller cavity, simula-  
536 tion results seem to indicate the possibility of a change of slope sign. Fitting the  
537 excess volume versus pressure with expressions previously tested on density of  
538 pure water enables estimation of its pressure derivative. This can be compared  
539 with the value obtained from simulation results of compressibility. Discrepancies  
540 can be relatively significant in the case of the smaller cavity. Nevertheless, the  
541 comparison shows acceptable consistency if one considers the general problem of  
542 computing derivatives with good accuracy.

#### 543 **Supplementary Data**

544 Fig. (S1) and Fig. (S2).

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