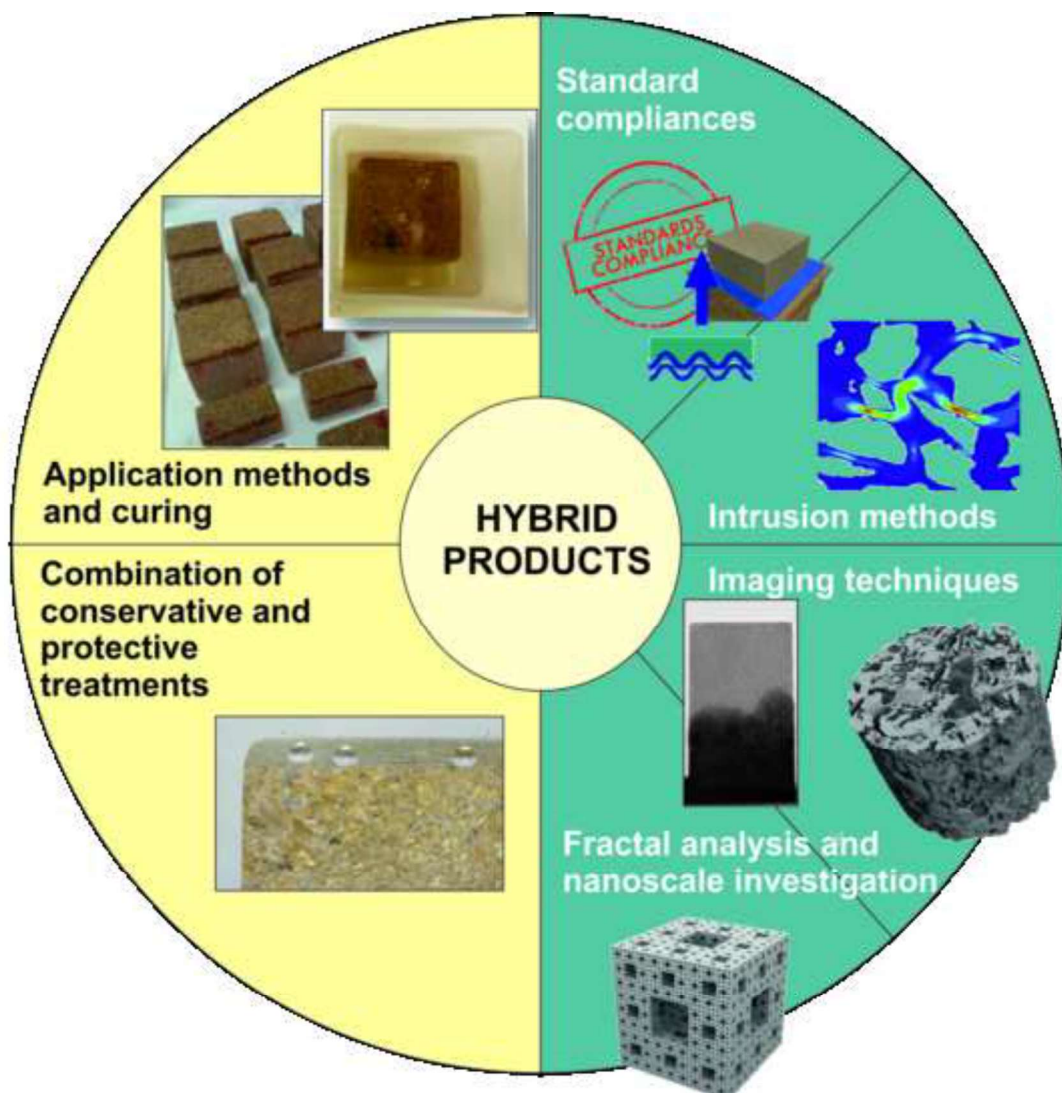


## \*Highlights

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- Efficiency of hybrid coatings were assessed on calcarenite substrate by using several techniques
- Advantages and limitations of classic and innovative methods were highlighted
- **Al-Si-based product led to changes not advisable for calcarenite substrates**
- **Polyamidoamine-based product is more suitable for porous calcarenite consolidation**
- **Merits and limitations of the hydrophobic coating used in combination with consolidants were explored**

**PROCEDURES ON CALCARENITE SUBSTRATE**



**ADVANCED MULTISCALE LABORATORY INVESTIGATION**

1 **Efficiency assessment of hybrid coatings for natural building stones: advanced and multi-**  
2 **scale laboratory investigation**

3  
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18  
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20  
21 **Abstract**

22 The efficiency of a hybrid patented consolidant (PAASi) and two commercially available hybrid coatings (a  
23 consolidant named AlSiX and a hydrophobic product named WS3) properly modified was assessed on a  
24 calcarenite substrate. Test routines based on standard recommendations were first applied to evaluate the  
25 performances of the consolidant and protective treatments, while the investigation of additional aspects such  
26 as penetration depth and interaction with the substrate was achieved by a multi-scale approach based on  
27 classic intrusion methods (mercury intrusion porosimetry) **and Drilling Resistance Measurement System**  
28 **(DRMS)**, combined with non-invasive imaging techniques (X-ray computed micro-tomography and neutron

29 radiography) and small angle neutron scattering (SANS). A distinct interaction of the products with the pore  
30 network of the stone was quantified in the range 0.007–200  $\mu\text{m}$ . Their effects on capillary water absorption  
31 were also visualized with neutron imaging. The suitability of the products on the selected substrate was  
32 discussed, highlighting also how the applied routine can support conservation material studies. **The results**  
33 **indicated that the Al-Si-based product led to unwanted effects. Alternative application methods and/or**  
34 **curing procedures have to be explored to overtake these undesirable changes. On the contrary, the**  
35 **polyamidoamine-based product seemed to be more suitable for calcarenite substrates conservation.**  
36 **The performances of the hydrophobic coating, when used in combination with consolidants, were**  
37 **strictly influenced by the pre-consolidation of the substrate.**

38

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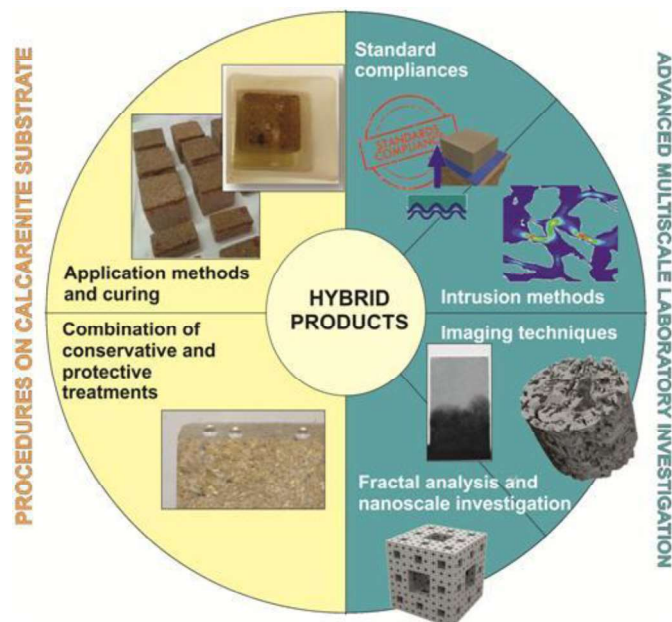
40 **Keywords:** consolidants; **hydrophobic products;** stones; hybrid coatings; nanoparticles; efficiency

41 **Highlights**

- 42 • Efficiency of hybrid coatings were assessed on calcarenite substrate by using several techniques
- 43 • Advantages and limitations of classic and innovative methods were highlighted
- 44 • **Al-Si-based product led to changes not advisable for calcarenite substrates**
- 45 • **Polyamidoamine-based product is more suitable for porous calcarenite consolidation**
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- 47 **explored**

48

49 **Graphical abstract**



50

51

52 **1. Introduction**

53 One of the main difficulties in conservation field is the choice of suitable consolidants and protective  
54 treatments for stones, able to preserve masonry, compatible with the stone substrate of interest, and without  
55 any detrimental effect on its aesthetical properties. Protective products must preserve stones in their state of  
56 aging and prevent further decay. This generally means applying a coating to the stone surface. Consolidation,  
57 on the other hand, aims at stabilizing a friable material, while allowing weathering to take place at a natural  
58 rate as a result of natural processes.

59 The requirements for consolidant products mainly consist in a good stability, compatibility with the substrate  
60 [1,2], and a suitable penetration depth. A good consolidant should primarily reduce the rate of decay of the  
61 stone surface and improve its mechanical properties. In the ideal case, the treated stone should mimic sound  
62 stone in as many characteristics as possible, especially in terms of porosity, permeability, thermal expansion,  
63 water absorption and desorption, and color.

64 **The main challenges in stone protection are related to the creation of a barrier against water**  
65 **penetration and the protection of the stone surface from pollutants and organic/inorganic particles**  
66 **deposition, while also ensuring the aesthetical compatibility with the substrate (i.e., color changes**  
67 **within acceptable ranges), the minimum alteration of the water vapor permeability and the**  
68 **reversibility of the treatment [3]. In this perspective, hydrophobic coatings [4], antifouling treatments**  
69 **[5] and self-cleaning nanoparticle-based protectives [6] are currently on the light of the research in**  
70 **stone preservation field [7].**

71 **Usually, tests based on standard recommendation procedures are applied** to evaluate the efficiency of  
72 consolidants or protective products, mainly aiming at verifying their harmlessness with respect to the aspect  
73 of stones and their physical properties [8]. However, up to now, in spite of the huge literature in the field, no  
74 standard procedures and/or univocal methods for assessing **the efficiency of consolidants and protective**  
75 **products** are proposed [9]. Going **beyond** the classic approaches, usually using microscopy, micro-drilling,  
76 and ultrasound velocity tests [10], imaging techniques could add relevant information, as demonstrated by  
77 the recent applications in archaeological, geological, and industrial fields [11,12]. **Indeed**, neutron and X-ray  
78 imaging **techniques** allow inspecting and **analyzing** numerous properties and processes, such as porosity,

79 water movement, degradation effects, amount and distribution of degradation products, or penetration depth  
80 of protective and consolidant products [13–19].

81 In the case of consolidants, penetration depth and bonding **to the** substrate are the two main aspects to  
82 investigate. Bonding ability greatly depends on both chemical composition of the product **used** (including  
83 solvent and concentration) and the stone surface [10]. Usually, products having a composition **similar to**  
84 **that of the** stone are preferred. **However**, this appears a non-exclusive requirement, **such** as in the case of  
85 silicate-based networks largely employed in marble and limestone consolidation [20–22].

86 When a new product **is tested** on a new substrate, the first question is related to **the artificial aging of stones**  
87 **to mimic the weathering of in situ conditions**. For limestones, salt weathering is a major cause of natural  
88 degradation. **However**, **since** salts are usually difficult to remove and could influence the consolidation test  
89 results [23], laboratory tests are also performed on unweathered stones. Another aspect regards the  
90 application method [24–26], where brushing is **sometime preferred because it ensures** a good product  
91 application and a relatively controlled equilibrium between penetration and solvent evaporation. **Of course**,  
92 **the testing of a new product requires preliminary tests aiming to identify the most suitable methods**  
93 **and procedures** [10,27].

94 Among the new products synthesized for conservation of cultural heritage materials, hybrid **formulations**  
95 **have recently been proposed for inorganic [28] and organic materials [29,30]**. The term hybrid refers  
96 **to a product usually developed by sol-gel processes [31] and characterized by both the robustness of an**  
97 **inorganic skeleton and the functional properties of an organic material [32]**. With regards to  
98 **consolidants, the current researches have mainly explored the potential of TEOS-modified products by**  
99 **using organic additives with the aim to overtake the limitations of negative long-term effects of**  
100 **tetraethoxysilane [33–36] and to improve performances of consolidants, including water repellent**  
101 **properties [37]**. Among hybrid formulations, silicon-based products are becoming more and more  
102 **popular, due to the good processability and the stability of Si—C bonds during the formation of a**  
103 **silica network, which allows the production of organic-modified inorganic networks in a single step**.  
104 **Soft-matter chemistry applications are also focused on designing hybrid coatings having mainly the**  
105 **scopes to improve repellency [38,39], performances [40] and durability of protective products against**  
106 **aging [41]**.

107 To evaluate the possible use of these new products for cultural heritage conservation, **and better**  
108 **understand how to tune hybrid formulations toward a better compatibility with highly porous and**  
109 **calcite-based stone substrates**, in this study, we tested a hybrid patented **product** (PAASi, [42]) and two  
110 commercially available hybrid coatings (a consolidant named AlSiX and a hydrophobic product named  
111 WS3) on a calcarenite substrate (named Sabucina Stone). **The synthesis of consolidants was designed to**  
112 **overtake possible limitations of such products. For the PAASi product, the amine would promote**  
113 **interaction with limestone substrate, while for the AlSiX product, the organic chains would contribute**  
114 **to limit shrinkage process during curing process.** The compositional and physical properties of **the** stone  
115 **selected** for consolidation tests, especially its high porosity, give also the opportunity to inspect the potential  
116 use of the products **on** highly porous materials, often difficult to consolidate [24]. To evaluate bonding and  
117 penetration ability of **the** products, consolidation tests were performed on **an** unweathered treated substrate,  
118 to avoid **the** difficulties related to **the** artificial weathering, such as **the** presence of salts and no proper  
119 desalinization. **Efficiency** and suitability of the products were firstly evaluated by monitoring absorption,  
120 desorption, color, **resistance to** artificial weathering, and pore structure changes. Thus, non-invasive  
121 investigations by using X-ray and neutron sources were performed to visualize products inside stones and the  
122 **possible** pore network modification. Finally, additional structural information on the employed products was  
123 obtained with small angle neutron scattering (SANS) technique.

124 **Consolidants** were applied by **immersion to have maximum penetration depth and fully impregnated**  
125 **specimens. In view of combining both consolidation and a protective application, hydrophobic coating**  
126 **was therefore applied by** brushing **the treated specimens. Finally**, for structural studies by SANS,  
127 **samples were treated by both brushing and** immersion, to evaluate the possible influence of the method in  
128 small scale structural changes **and penetration in nano-sized pores.**

129

## 130 **2. Materials and methods**

### 131 **2.1 Materials**

#### 132 *2.1.1 Natural building stone*

133 A coarse grained calcarenite, named Sabucina stone, employed in Sicilian monuments as building and  
134 replace material was selected for this study [43]. **The stone is a biosparite with grainstone/packstone**



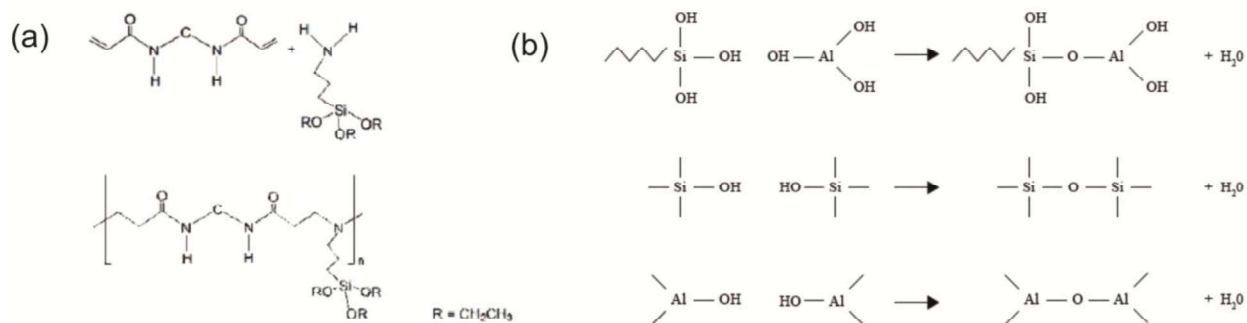
135 texture, mainly composed by calcium carbonate, along with small quantities of dolomite. It exhibits a  
 136 porosity of  $\sim 27\%$ , with a total pore volume of  $0.14 \text{ cm}^3 \text{ g}^{-1}$  and a modal pore radius of about  $8.5 \mu\text{m}$ .  
 137 Further details on the petrography, mineralogy, chemical composition, petrophysics, and porosimetry of  
 138 this lithotype are provided in Barone et al. [44].  
 139 For this study, 225 samples were obtained from a unique freshly quarried block sampled at Sabucina  
 140 Mountain (Caltanissetta, Sicily), varying in dimension and shape in accordance with the requirements of the  
 141 applied methods and recommendations (see Table 1).

142

### 143 2.1.2 Hybrid products

144 Two different hybrid inorganic-organic consolidants were synthesized and tested on Sabucina stones, namely  
 145 (i) a polyamidoamine-based product with siloxane functionality (PAASi), and (ii) a silicon alkoxide with  
 146 epoxy functional group and aluminum oxide (AlSiX). The schematic chemical structure of both products is  
 147 shown in Figure 1.

148



149

150 Figure 1. Pictorial sketch showing (a) the reaction producing PAASi and (b) the main reactions involved in the sol formation of  
 151 AlSiX.  
 152

153 The hybrid product PAASi is a patented wood protective material [42], modified for its application on stone  
 154 substrates. The product was synthesized by the Michael-type reaction, adding 3-aminopropyltriethoxysilane  
 155 (APTES) to N-N'methylenebisacrylamide (MBA). In detail, in a flask placed in a thermostatic bath at  $30^\circ\text{C}$ ,  
 156  $5 \times 10^{-2}$  mol of MBA were dissolved in 190 mL of deionized water and the solution was stirred for 20 min.  
 157 After complete solubilization of MBA in water,  $5 \times 10^{-2}$  mol of APTES, mixed in 10 mL of ethanol were  
 158 added. The obtained solution was vigorously stirred in the thermostatic bath at  $40^\circ\text{C}$  for 2 h. A 0.25 M sol

159 **was finally obtained.** The inorganic group inside the stone can polymerize in situ by hydrolysis and  
160 condensation reaction, forming a 3-D network.

161 The hybrid sol AlSiX is based on an Al-O-Si network functionalized with organic chains and epoxy groups,  
162 having the role of reducing the brittleness of the inorganic structure. The sol was synthesized by sol-gel  
163 process starting from a solution of aluminum and silicon alkoxides in propan-2-ol. The stoichiometric  
164 amount of water acidified with HCl was added to hydrolyze the precursors. The stirring was prolonged until  
165 a completely transparent sol was obtained. The sol was then diluted adding water (alcohol/water volumetric  
166 ratio = 1:2). The final concentrations of aluminum and silicon were 0.33 M and 0.66 M, respectively.

167 **For the treatment of the studied substrates, cubic samples of Sabucina stone ( $4 \times 4 \times 4 \text{ cm}^3$ ) were**  
168 **preliminary washed in distilled water and dried at  $60^\circ\text{C}$  to constant mass [45]. Samples were thus**  
169 **plunged into PAASi and AlSiX sols in sealed containers for 1 h and dried at  $60^\circ\text{C}$  to constant mass.**  
170 **Samples were cured 1 month at room temperature (RT) condition.**

171 **The average quantity of applied products was calculated as weight percent gain (WPG%):  $\text{WPG \%} =$**   
172  **$100 \cdot [(M_t - M_0)/M_0]$ , with  $M_0$ , the mass of dry sample before the product application, and  $M_t$ , the**  
173 **mass of dry sample after product application. The calculated quantities were  $1.9\% \pm 0.1 \text{ WPG\%}$  for**  
174 **AlSiX and  $1.4\% \pm 0.3 \text{ WPG\%}$  for PAASi.**

175

### 176 *2.1.3 Hydrophobic coating*

177 A colloidal silica with fluorinated groups named WS3 was tested as coating on Sabucina stones treated with  
178 PAASi and AlSiX, to verify its hydrophobic efficiency and suitability on treated calcarenite substrates.

179 The treatment was prepared by mixing -O-Si-O-Si( $R_f$ )-O- siloxane chains (with  $R_f$ , the fluorinated groups)  
180 and colloidal silica: the fluorinated groups provide the hydrophobic functions, while the colloidal  
181 nanoparticles enhance the water repellency by creating a suitable surface texture. The silica nanoparticles  
182 size was about 10 nm, whereas the resulting siloxane aggregates were micrometric in size.

183 **For this study, WS3 was applied by brushing on cubic samples after the application of PAASi and**  
184 **AlSiX. The average quantity of product applied was  $0.7 \pm 0.1 \text{ g m}^{-2}$ , calculated as the difference**  
185 **between the weight of dry specimens after and before the treatment (dry matter).**

186

187 **2.2 Characterization methods**

188 **2.2.1 Physical and mechanical tests**

189 A protocol based on standard NORMAL and UNI EN tests was applied in order to verify the compatibility  
190 of the studied products and their suitability on calcarenite substrates. In detail, comparative colorimetric,  
191 physical (water absorption, drying and salt crystallization resistance), and mechanical (**microdrilling**  
192 **resistance**) tests were performed on untreated and treated samples.

193 **Firstly, to evaluate the hydrophobic characteristics of the coating, contact angle measurements were**  
194 **performed on samples after the application of WS3 according to UNI 11207:2007 [46].**

195 Color difference between treated and untreated samples ( $\Delta E^*$ ) was evaluated according to UNI EN  
196 15886:2010 [47]. The absorption coefficient by capillarity AC ( $\text{g cm}^{-2} \text{s}^{-0.5}$ ) was evaluated according to the  
197 UNI EN 15801:2010 recommendation [48] on three cubic samples for each treatment (with edges of 4 cm)  
198 by applying the following time intervals: 5 min, 10 min, 20 min, 30 min, 60 min, 4 h, 6 h and 24 h, [...], 7  
199 days). Water absorption by total immersion was evaluated following the NORMAL 7/81 recommendation  
200 [49], that allows calculating the imbibition coefficient CI (%). **This** test was performed on fifteen samples  
201 for each treatment (time intervals: 5 min, 10 min, 20 min, 30 min, 60 min, 4 h, 6 h and 24 h, [...], 72 h). **The**  
202 **drying index DI was determined following the NORMAL 29/88 recommendation [50].** Saturated  
203 samples from the previous NORMAL 7/81 were used for this test. The resistance to aging by soluble salts  
204 was determined according to the UNI EN 12370:2001 test [51], performed on 15 cubic samples for each  
205 treatment ( $4 \times 4 \times 4 \text{ cm}^3$ ).

206 **Following the UNI EN 15803:2010 norms [52], the water vapor permeability tests were performed on**  
207 **treated and untreated stone samples  $4 \times 4 \times 1 \text{ cm}^3$ , mounted on of PVC containers, partly filled with**  
208 **water; the sealed containers kept in a climatic chamber (R.H. 25% and  $T = 25 \pm 0.5^\circ\text{C}$ ), were weighted**  
209 **every 24 h until the mass change per unit time were constant (i.e. constant value of vapor flow through**  
210 **the stone). The effect of the treatments on the water vapor permeability was quantified by  $RVP\% =$**   
211  **$\frac{m_{uv} - m_{tv}}{m_{uv}} \cdot 100$ , called reduction of vapor permeability, with  $m_{uv}$  = mass of water vapor penetrating**  
212 **untreated stone and  $m_{tv}$  = mass of water vapor penetrating treated stone, measured in the steady state**  
213 **[53].**

214

215 **Microdrilling resistance was determined by drilling resistance measurement system (DRMS) [54] on**  
216 **consolidated specimens cured several months. For this study, 3 mm diameter Widia drill bit was used,**  
217 **with a rotation speed of 800 rpm and a penetration rate of 10 mm min<sup>-1</sup>. For each treated specimen**  
218 **and for a reference untreated one, four holes were drilled over 5 mm in depth from the surface. The**  
219 **average force as a function of depth was reported.**

220

#### 221 *2.2.2 Mercury intrusion porosimetry (MIP)*

222 Mercury intrusion porosimetry (MIP) measurements were performed by using a Thermoquest Pascal system  
223 (coupled 240 and 140 units) to explore a pore radii range from 0.0074 to 116 μm. Average data were  
224 assessed on measurements performed on three small specimens similar in dimension and shape (**cubes of ~1**  
225 **cm<sup>3</sup>) sampled at the surface of cubic samples coated with AlSiX and PAASi.** Data were processed by  
226 using the SOL.I.D (Solver of Intrusion Data) software.

227

#### 228 *2.2.3 X-ray computed micro-tomography (μCT)*

229 μCT scans were performed at the Centre for X-ray Tomography (UGCT, Ghent University, Belgium) [55].  
230 Cylindrical samples with a diameter of 7 mm were scanned before and after the treatment with AlSiX and  
231 PAASi **at the stone surface.** An overall of 1201 projections were acquired **over an angle of 360°** with a  
232 **source-detector distance** of 1165 mm and a **source-object distance** of 22 mm, resulting in a voxel size of  
233 7.5 μm. **A voltage of 120 kV, a power of 10 W, and a tube current of 83 μA** were imposed. **Additionally,**  
234 **a beam hardening effect was reduced** by using an Al-filter (1 mm). Only objects with a minimum of 3  
235 voxels were retained in reconstruction analysis. Because the consolidation products tend to have attenuations  
236 for X-rays similar to those of the minerals of the stone samples, Ag<sup>+</sup> ions (from AgNO<sub>3</sub>) were added to the  
237 studied products as tracer. Before the application on Sabucina stones, AgNO<sub>3</sub> was directly dissolved in the  
238 sols by vigorous stirring (molar ratio PAASi monomer/Ag<sup>+</sup> = 2500:1 and Si(AlSiX)/Ag<sup>+</sup> = 2500:1). μCT  
239 data were reconstructed with the Octopus Reconstruction software [56], while 3-D visualization and  
240 quantification were obtained by using VGStudio MAX (Volume Graphics) and Octopus Analysis (former  
241 Morpho+) [57], respectively. Only objects of a minimum of 3 voxels were retained in the analysis.

242

#### 243 2.2.4 Neutron radiography

244 Neutron images were acquired on 15 samples ( $2 \times 2 \times 4 \text{ cm}^3$ ) of the studied stone with either consolidant or  
245 water repellent products, with the aim of (i) visualizing the penetration depth of the selected products after  
246 polymerization and (ii) monitoring the water absorption process by capillarity, to evaluate the possible  
247 modification of the physical properties of the stones. Neutron **radiographs** were acquired at **the** IMAGINE  
248 beamline of the Laboratoire Léon Brillouin (LLB, Saclay, France), using a neutron flux of  $2 \times 10^7$   
249 neutrons  $\text{s}^{-1} \text{ cm}^{-2}$  (cold neutrons with wavelength in the range 3–20 Å), a  $L/D$  ratio of 400 and a sCMOS  
250 camera (Andor) coupled with a lithium scintillator of 100  $\mu\text{m}$  thickness. **This set-up** allowed a spatial  
251 resolution of about 250  $\mu\text{m}$ .

252 Dark field and open beam images were firstly acquired for further corrections. Samples were scanned in an  
253 aluminum container and a reference image in dry state was acquired. To monitor capillary uptake, water was  
254 manually added by filling the container with 3 mm of water. After the addition, scans were acquired every 40  
255 s until saturation **with an exposure time of 40 s**. The duration of the **whole** experiment was about 20 min.

256 Image analysis was performed by using **the** ImageJ software [58] on **radiographs** corrected and normalized  
257 by dark field and open beam images. Water content distribution was quantified according to Kim et al. [59].  
258 Moreover, **the** sorptivity parameter ( $B$ ) was experimentally determined from the radiographs, according to  
259 Philip [60].

260

#### 261 2.2.5 Small angle neutron scattering (SANS)

262 Small angle neutron scattering measurements were performed on the PAXY instrument (cold neutron guide  
263 G2) at the ORPHEE reactor of the Laboratoire Léon Brillouin (LLB, Saclay, France). Neutrons **were**  
264 monochromatized by a mechanical selector and collimated by two slits 5 m far apart. Scattered neutrons  
265 **were** collected by a 2-D  $\text{BF}_3$  detector consisting in  $128 \times 128$  cells, **each** of them measuring  $5 \times 5 \text{ mm}^2$ . Two  
266 different set-ups were used to explore different  $Q$  ranges: for large  $Q$  (from  $3.2 \times 10^{-2}$  to  $0.28 \text{ \AA}^{-1}$ ), **the**  
267 **wavelength**  $\lambda = 6 \text{ \AA}$  and **the sample-detector distance** = 1 m, **whereas** for small  $Q$  (from  $4 \times 10^{-3}$  to  $3.6 \times$   
268  $10^{-2} \text{ \AA}^{-1}$ ),  $\lambda = 8.5 \text{ \AA}$  and **the sample-detector distance** = 5 m.

269 In order to minimize multiple scattering effects, measurements were performed on thin sections of treated  
270 stone, with thickness  $< 1 \text{ mm}$ . Slices were treated with AlSiX and PAASi by different **application** methods,

271 i.e., by brushing and by immersion under vacuum to investigate the possible variation in pore surface-air  
272 interface due to the product deposition. No appreciable neutron activation of the samples was found after the  
273 experiment.

274 The two-dimensional intensity distributions were corrected for the background and **normalized** by  
275 measuring the incident beam intensity, transmission, and sample thickness. One-dimensional data were  
276 obtained by integrating the normalized two-dimensional intensities with respect to the azimuthal angle. At  
277 large  $Q$ , the constant asymptotic incoherent scattering of the hydrogen atoms present in the samples was  
278 subtracted. The coherent scattering  $I(Q)$  is expressed in  $\text{cm}^{-1}$  and corresponds to a differential coherent cross-  
279 section per unit volume of the samples. Starting from the  $I(Q)$  distributions, roughness of the pores surface in  
280 terms of surface fractal dimension  $D_s$  [61], were obtained for untreated and treated samples according to the  
281 following equation:

$$I(Q) \propto Q^{-(6-D_s)}$$

282

### 283 **3. Results and Discussion**

#### 284 **3.1 Physical and mechanical tests**

##### 285 **3.1.1 Static contact angle**

286 **The test confirmed the hydrophobic behavior of the WS3 product, with an average measured contact**  
287 **angle of  $130^\circ \pm 2^\circ$ .**

288

##### 289 **3.1.2 Colorimetric tests**

290 In **Table 2**, the total color difference  $\Delta E^*$  between treated and untreated stone samples, calculated on the  
291 basis of the measured colorimetric parameters  $a^*$ ,  $b^*$ , and  $L^*$  are reported (approximated to the integer).

292 **As reported in the literature [62], a conservative treatment should not lead to a total color change greater**  
293 **than 5. The AlSiX product clearly led to strong chromatic changes, especially when used in association**  
294 **with the hydrophobic coating. This could be related to the presence of aluminum bonded with the**  
295 **silica network. Conversely, the application of PAASi had acceptable chromatic changes, even if the**  
296 **presence of hydrophobic coating led to higher  $\Delta E^*$ .**

297

298 *3.1.3 Comparative water absorption-desorption and accelerated aging test*

299 The average capillary absorption curves assessed on three samples for each treatment (*i.e.*, untreated, PAASi,  
300 PAASi + WS3, AlSiX, AlSiX + WS3) are shown in Figure 2a, and the absorption coefficients AC, evaluated  
301 as the slope of the line fitted to the evolution of  $Q_t$  as function of  $t^{0.5}$  in the first 30 min are reported in Table  
302 **3**. The samples treated with PAASi showed slightly lower capillary absorption **as** compared to the untreated  
303 stones, with a low increase of the absorption coefficient in the first 30 min of the test. In samples treated with  
304 AlSiX, the capillary absorption decreased **as** compared to the untreated stones, especially during the first 30  
305 min of **water** absorption. Finally, the presence of the hydrophobic coating WS3 led to a reduction of the  
306 water absorption by capillarity, with a decrease of AC from  $0.03 \text{ g cm}^{-2} \text{ s}^{-0.5}$  to  $0.01 \text{ g cm}^{-2} \text{ s}^{-0.5}$ . The amount  
307 of water absorbed by capillarity at the transition from the first to the second stage of the capillary absorption  
308 curves (*i.e.*, after 4 h) can be used to evaluate the changes in porosity accessible to water before and after the  
309 treatments [63]. On the basis of the obtained data, it is possible to estimate the following effective porosity:  
310 ~21% in untreated stone, ~19% and ~14% in samples treated with PAASi and AlSiX, respectively. A more  
311 important decrease (up to ~13%) can be observed for samples coated also with the hydrophobic **product**  
312 WS3. These results indicate that the two consolidants reduced the effective porosity **of** about 2% (PAASi)  
313 and 7% (AlSiX). Of course, in the case of samples treated also with hydrophobic product, the calculated  
314 porosity has to be carefully considered, as its drastic reduction is plausibly attributable to the coating **at** the  
315 **stone** surface.

316 For the total immersion test, the average curves calculated on 15 samples for each treatment are reported in  
317 Figure 2b. The **imbibition coefficient** CI after 72 h (Table **3**) highlights a slight decrease (of about 1%) of  
318 the water imbibition for samples treated with both consolidants, whether associated or not with WS3. This  
319 indicates that the total porosity **was** not strongly modified by the treatments, while more relevant  
320 modifications occurred in **the** pore structure arrangement, **mainly affecting** capillary water absorption. **To**  
321 **summarize, treated samples have a lower absorption of water by capillarity and total immersion,**  
322 **proving the deposition of the products in pores and/or pore throats.**

323 The use of both consolidants and hydrophobic treatment also influenced the drying properties of the studied  
324 stone, as suggested by the increase of the dry index DI for samples treated with consolidants and coated or  
325 not with WS3 (Figure 2c and **Table 3**). The treatments modified the overall drying rate of Sabucina stone,

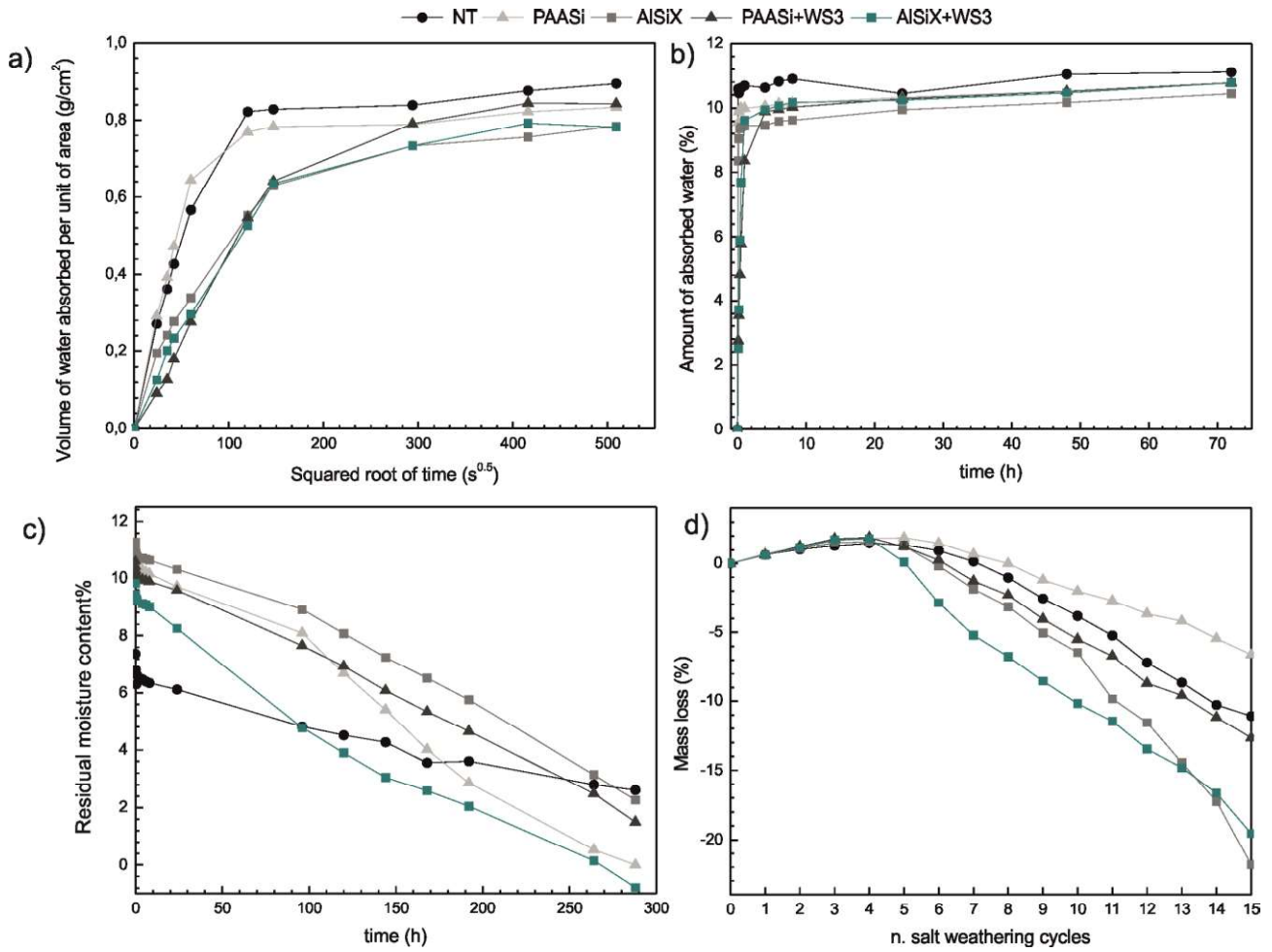
326 affecting particularly the second phase of the drying process, which is strongly governed by vapor diffusion.  
327 **Indeed**, the critical moisture content **was** higher for **the** treated samples, in **agreement** with the observed  
328 decrease in the capillary coefficient.

329 **The results on the reduction of the vapor permeability *RVP*%, calculated after a 14 days test are**  
330 **reported in Figure 3. The stone samples treated with ALSiX and PAASi consolidants show %RPV**  
331 **values in the range 4-10%, below the acceptable threshold of 20% [64]. On the contrary, for the**  
332 **combined use of consolidants and hydrophobic treatment, the reduction of vapor permeability is**  
333 **significantly higher (40-45%); actually, it is not unusual that hydrophobic films determine strong**  
334 **water permeability reduction when used onto porous substrates [65].**

335 As regards aging tests (Figure 2d), PAASi **seemed** to improve the resistance to salt crystallization, with a  
336 decrease of the mass loss after 15 cycles (**Table 3**), from -11.1% (untreated samples) to -6.6%. It is  
337 noteworthy that the presence of WS3 slightly **increased** the mass loss, from -11.1% to -12.7%. For ALSiX,  
338 even if the product resulted in lower absorption **properties**, it was responsible for a slight decrease of the  
339 durability of the studied material: an increase of the mass loss after 15 cycles was observed for treatments  
340 with ALSiX and ALSiX + WS3. It is possible to assume that the reduced capillary transport might **have**  
341 **caused** a faster shift towards phase 2 in drying at higher moisture content (and thus lower salt  
342 concentrations), so that supersaturation **was** reached with a drying front within the stone, **leading to an**  
343 **increase in** mass loss.

344





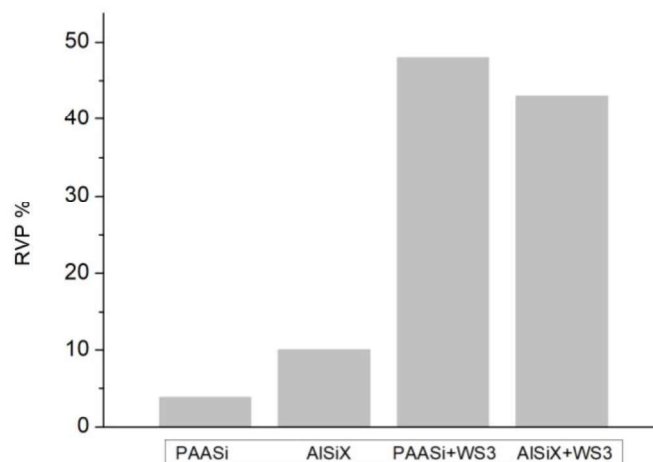
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Figure 2. Water absorption by (a) capillarity and (b) total immersion, (c) drying and (d) durability tests performed on untreated stones (NT) and stones treated with both consolidants (PAASi and AISiX) and hydrophobic (WS3) products.



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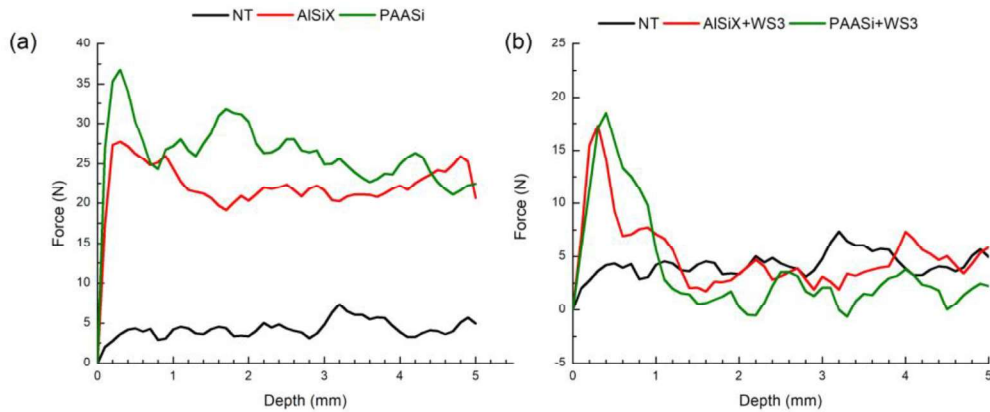
351

Figure 3. Reduction of vapor permeability RVP% for different treatments.

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### 3.1.4 Drilling resistance

Fig. 4 shows the drilling resistance graphs obtained by drilling resistance measurements on untreated and treated specimens cured in laboratory during several months.



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Figure 4. Drilling resistance on Sabucina stones treated with (a) consolidants (AISiX and PAASi) and (b) consolidants in combination with hydrophobic product (WS3).

361 The curve describing the behavior of the untreated stone (black line) highlights a natural variation in  
362 strength, probably related to the texture of the stone. Overall, the drilling resistance of the stone was  
363 quite low (about 4–6 N).

364 The two consolidants promoted both an increase in strength, well pronounced in the first 1–2 mm. In  
365 combination with the hydrophobic product, the strengthening effect was strictly limited to the first  
366 millimeter. Potentially, this behavior could be ascribed to the different long-term curing dynamic, *i.e.*,  
367 influence of the hydrophobic layer on moisture transfer during polymerization.

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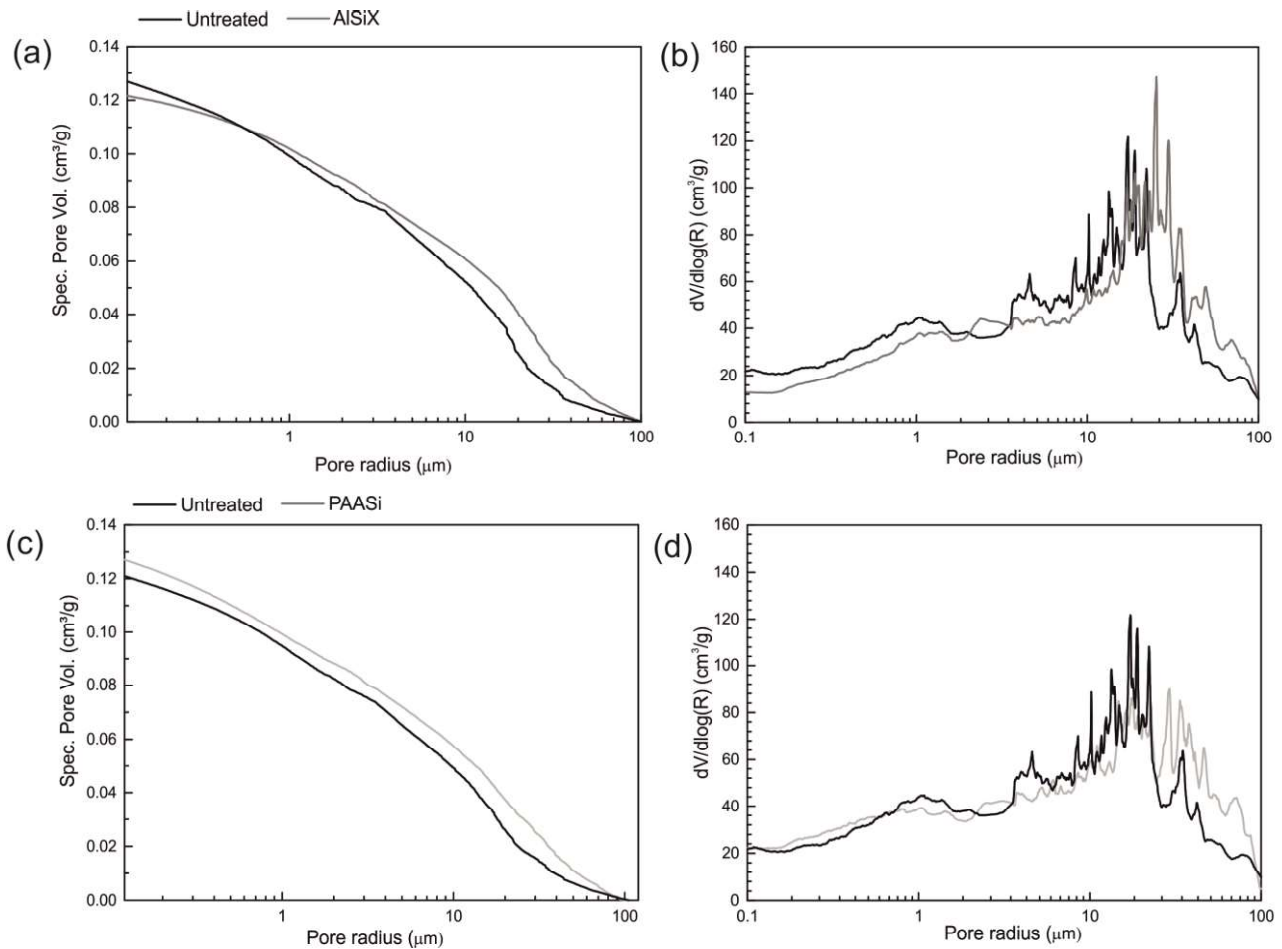
### 3.2 MIP

370 Table 4 reports pore structure parameters obtained on untreated samples and samples treated with AISiX and  
371 PAASi. In agreement with the results of the absorption tests, products did not greatly modify the total  
372 porosity, but mainly affected the pore structure arrangement of the stone. For AISiX, a strong shift of the  
373 average pore radius and of the median and modal pore sizes can be observed, from 0.14  $\mu\text{m}$  to 0.22  $\mu\text{m}$ , from  
374 8.56  $\mu\text{m}$  to 12.55  $\mu\text{m}$ , and from 2.25  $\mu\text{m}$  to 4.21  $\mu\text{m}$ , respectively. The ranges of these variations are

375 adequately expressed by the cumulative volume intrusion and pore size distribution curves (Figure 5a),  
376 **suggesting the impregnation of pore larger than 5  $\mu\text{m}$ .**

377 For the PAASi treatment, the small differences in the porosimetric parameters could only be related to the  
378 already attested variability of the stone, **even if some variations can be observed in the cumulative**  
379 **volume intruded and pore size distribution curves (Figure 5b).**

380



381

382 *Figure 5. Pore size distributions represented as (a, c) cumulative or (b, d) differential pore volumes, measured on untreated samples*  
383 *(black) and samples treated with (a, b) AlSiX and (c, d) PAASi consolidants (gray).*

384

### 385 3.3 $\mu\text{CT}$

386 In order to better visualize the distribution of the studied consolidants inside the pore space of the stone,  
387 scans were performed on small cylindrical samples before and after the application of the products.  $\mu\text{CT}$   
388 scans were obtained by subtracting measurements collected on untreated and treated samples. The untreated  
389 stone had a resolved porosity of about 11.7% (with open and closed porosity values of 10.1% and 1.6%,

390 respectively), and pore distribution described by equivalent diameter (ED) and maximum opening (MO)  
391 ranging from 7.5  $\mu\text{m}$  to 967.5  $\mu\text{m}$  and from 7.5  $\mu\text{m}$  to 372.5  $\mu\text{m}$ , respectively (see also [66]).

392 After the application of the AISiX product, the resolved porosity **of the whole sample** decreased by 2%.

393 From an inspection of ED and MO distributions (Figure 6a and b), it is possible to conclude that AISiX

394 impregnated pores exhibiting ED values from 7.5 to 500  $\mu\text{m}$  and pores with MO values between 7.5 and 150

395  $\mu\text{m}$ . Pores having ED > 500  $\mu\text{m}$  and MO > 150  $\mu\text{m}$  were not affected by the treatment. The 3-D image

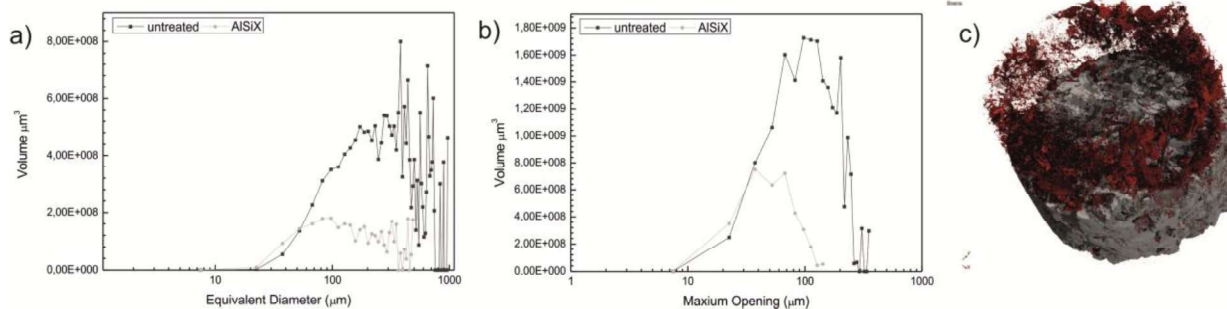
396 reconstructions presented in Figure 5c allow visualizing the distribution of AISiX into the pore network of

397 the stone (in red). Of course, due to the voxel resolution, only pores with ED > 7.5  $\mu\text{m}$  can be considered.

398 **Therefore**, it is possible that pores with ED < 7.5  $\mu\text{m}$  also contain consolidant.

399

400



401 **Figure 6.** Pore volume as function of (a) the equivalent diameter and (b) maximum opening for AISiX treatment (step intervals 2  
402 voxels, i.e., 15  $\mu\text{m}$ ). (c) 3-D visualization of the bulk material (gray) and distribution of AISiX (red). The sample diameter is  
403 approximately 7 mm.  
404

405 Before PAASi application, the resolved porosity of the untreated samples was about 12.3% (with open and

406 closed porosity values of 10.8% and 1.5%, respectively), and the pore network was characterized by pores

407 ranging from 7.5  $\mu\text{m}$  to 1220  $\mu\text{m}$  in ED and **from** 7.5  $\mu\text{m}$  to 400  $\mu\text{m}$  in MO. A reduction of 0.8% of the

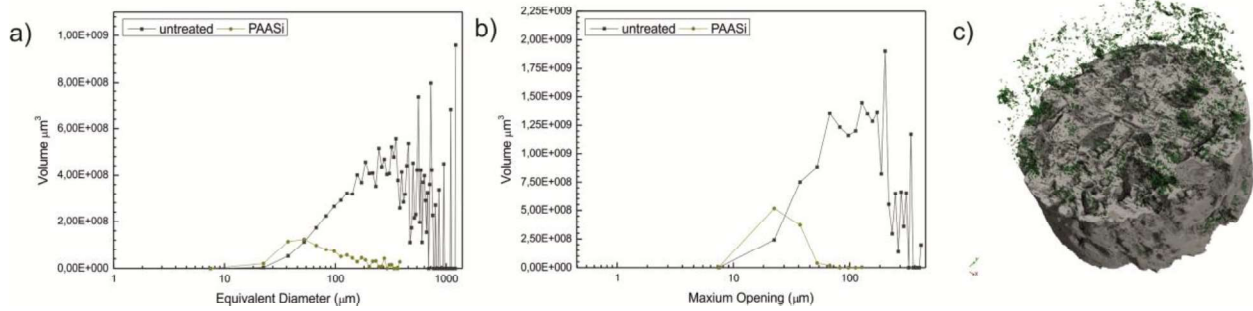
408 resolved porosity **of the whole sample** was observed after **PAASi** application, suggesting a very poor

409 impregnation ability of PAASi. This behavior was confirmed by the ED and MO distributions relative to

410 pores filled by the consolidant (Figure 7a and b), indicating that only a limited range of pores (i.e., ED ~40–

411 300  $\mu\text{m}$  and MO < ~70  $\mu\text{m}$ ) was involved. This low impregnation ability is also visible in the 3-D

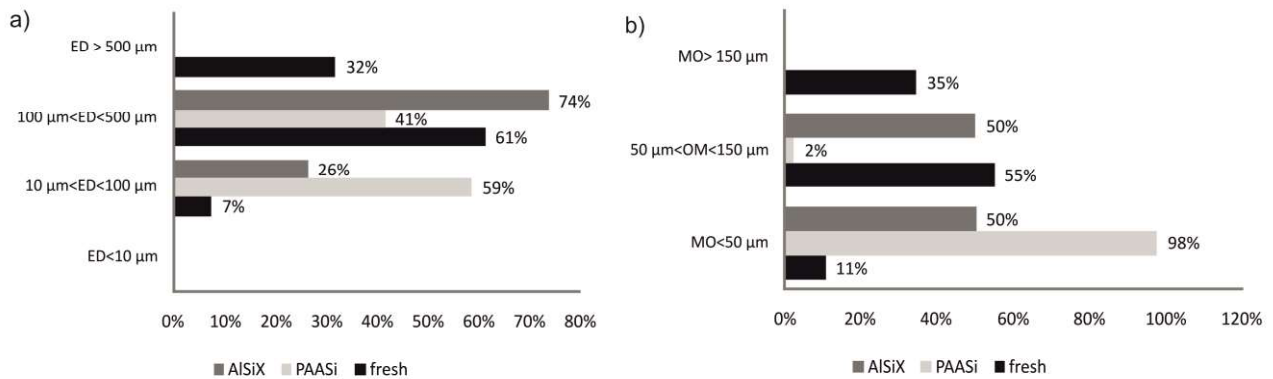
412 representation (Figure 7c).



413

414 **Figure 7.** Pore volume as function of (a) the equivalent diameter and (b) maximum opening for PAASi treatment (step intervals 2  
 415 voxels, i.e., 15  $\mu\text{m}$ ). (c) 3-D visualization of the bulk material (gray) and distribution of PAASi (green). The sample diameter is  
 416 approximately 7 mm.  
 417

418 By comparing the behavior of the two different studied products (Figure 8), it is possible to conclude that in  
 419 the case of PAASi, the product mainly impregnated pores with ED in the range from 50 to 100  $\mu\text{m}$  and MO  
 420 in the range from 7.5 to 50  $\mu\text{m}$ , whereas in the case of AISiX, the product involved larger pore ranges (ED  
 421 between 100 and 500  $\mu\text{m}$ , MO between 50 and 150  $\mu\text{m}$ ). It indicates a different interaction of the products  
 422 with the pore network of the stone, with PAASi penetrating into finer pores than AISiX.



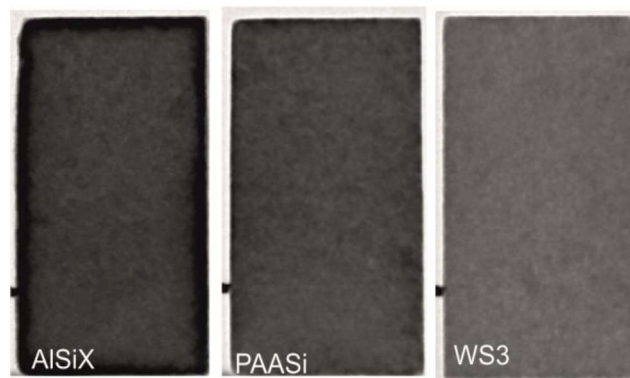
423

424 **Figure 8.** Comparison of (a) the equivalent diameter (ED) and (b) maximum opening (MO) classes impregnated with consolidants  
 425 (AISiX and PAASi).  
 426

### 427 3.4 Neutron radiography

428 Neutron radiographs acquired for treated Sabucina stone samples are shown in Figure 9. In the sample  
 429 treated with AISiX, the radiograph shows the presence of product inside the sample, resulting in an increased  
 430 attenuation of the neutron beam close to the sample edges. The product may be homogeneously  
 431 distributed up to a penetration depth of 2–3 mm, in agreement with microdrilling results. A lower  
 432 amount of product may reach 5 mm depth. Such a behavior can also be observed in the case of the  
 433 combined use of AISiX and water repellent WS3.

434 In the case of samples treated with PAASi, the presence of consolidant is hard to detect in the radiographs,  
435 **due to a low interaction between the neutron beam and the product.** Similar observations can be made  
436 for the combination PAASi + WS3. **Nevertheless, information about the penetration depth are available**  
437 **from drilling resistance, attesting a relevant increase in strength up to a depth of a few millimeters.**  
438 The water repellent product cannot be distinguished, because its thickness may be too small for a good  
439 contrast between untreated and treated areas. Of course, it has to be taken into account that the two products  
440 consist in chemical components differently detectable by neutrons, so that PAASi has credibly a lower  
441 attenuation coefficient than AISiX.



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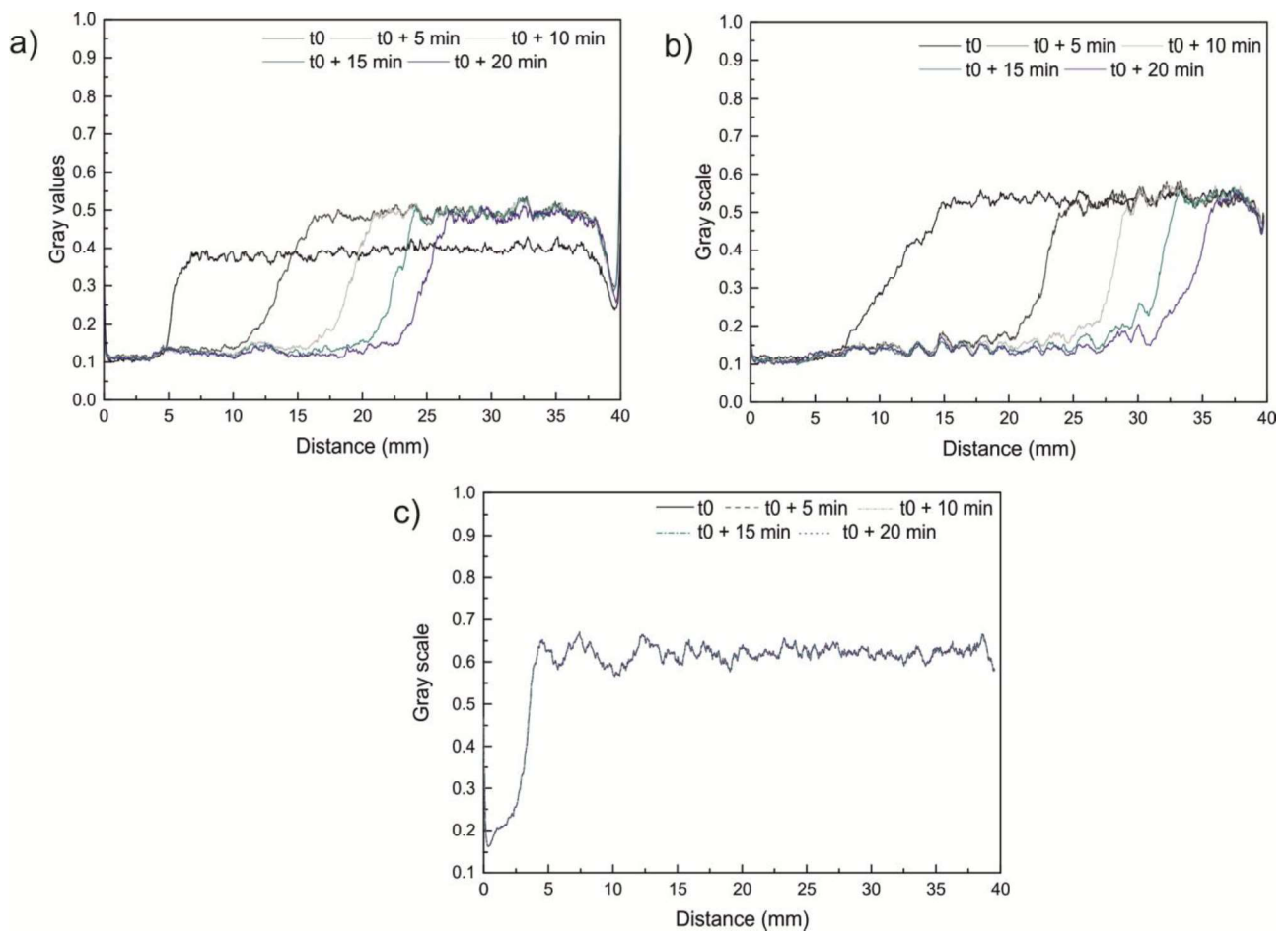
443 *Figure 9. Neutron radiographs of samples treated with consolidant (AISiX and PAASi) and water repellent (WS3) products.*

444

445 Water movement by capillarity was monitored over time through neutron radiography. Radiographs were  
446 acquired at 5, 10, 15, and 20 min after the addition of water at the bottom of the samples, for a reference  
447 untreated sample and for samples representative of different treatments. The 2-D distribution of water and  
448 the wetting front advancement can be easily visualized. In **Figure 10**, the profiles of intensity values at  
449 selected time steps obtained from the central vertical column of pixels in the normalized transmission images  
450 are reported. The wetting front position **was** determined as the inflection point of the profile, indicating the  
451 transition between low intensity values (saturation) and higher intensity values (dry conditions).

452 The wetting front positions were related to time and the sorptivity parameters ( $B$ ) were determined by using  
453 linear regressions. The **wetting front** migrating inside the treated samples was slightly slowed down by the  
454 presence of the products (Table 5), even if during the first minutes of contact with water, a faster  
455 advancement of the wetting front position was observed.

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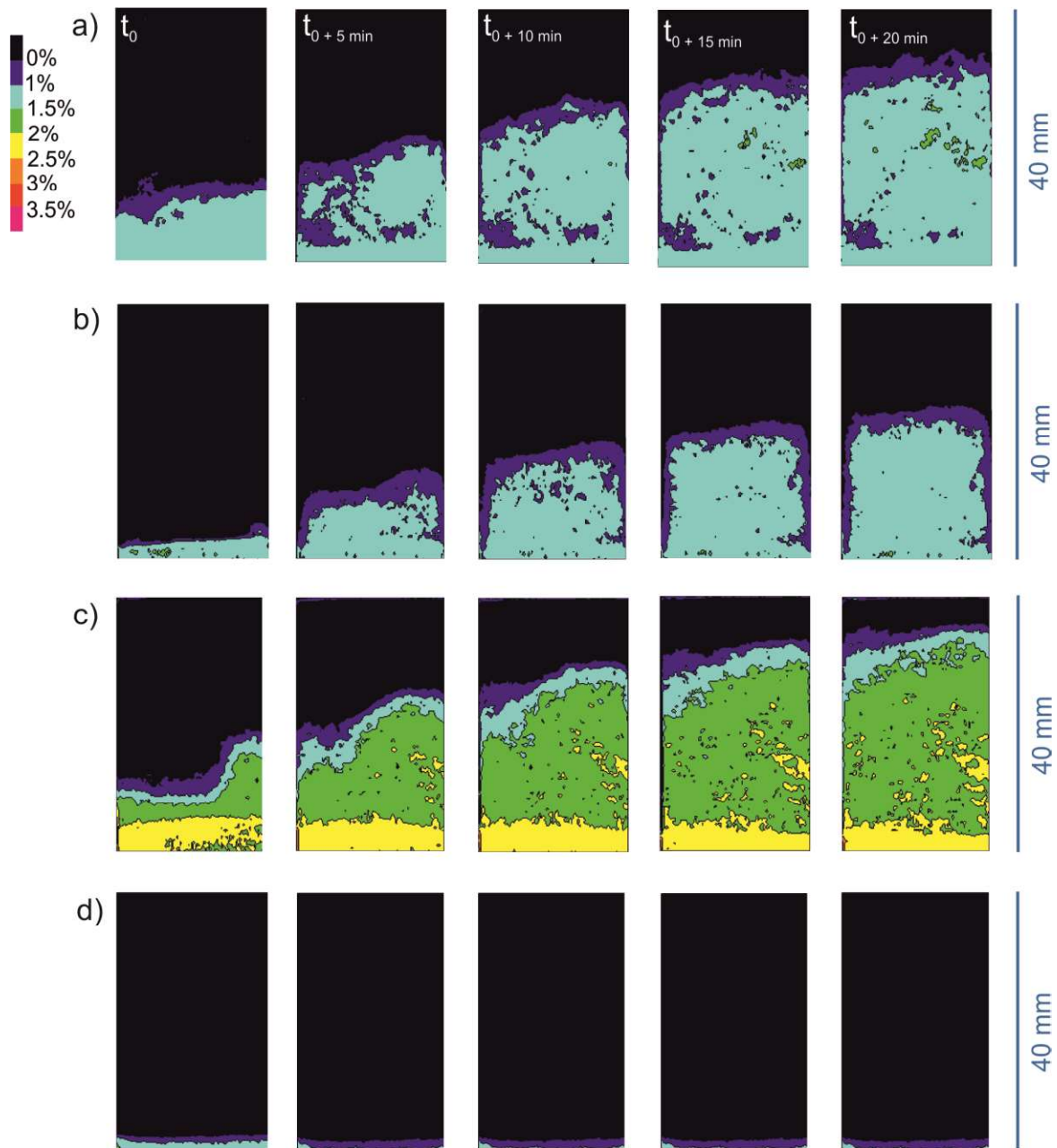


457

458 **Figure 10.** Profiles of intensity values of samples treated with (a) AlSiX and (b) PAASi consolidants, and (c) hydrophobic product  
 459 WS 3 at selected time steps during capillary water uptake. The 0 reference distance is the bottom of the samples.  
 460

461 In order to quantify the water distribution and to better understand the water absorption process in treated  
 462 samples, the thickness of water crossed by the neutron beam as a function of time was estimated. Examples  
 463 of contour plots of the water content distribution (WC%) estimated from the neutron radiographs at 5, 10, 15,  
 464 and 20 min after the addition of water are shown in **Figure 11**. In the case of the AlSiX treatment, WC% was  
 465 lower than in the untreated samples (always < 2%). Water penetrated preferentially through areas not  
 466 impregnated by the consolidant, as can be seen by the lower WC% close to the lateral edges. On the  
 467 contrary, for the PAASi treatment, an increase of the water absorbed was observed (WC% > 2.5–3%).  
 468 Finally, the performances of hydrophobic treatments (used both alone and in combination with consolidant)  
 469 are clearly evidenced: the contour plots show that no water invaded the samples during the first minutes of  
 470 contact with water. The layer visible at the bottom of the radiographs has to be related to the set-up reservoir.  
 471 **Overall, these results are in agreement with the porosity and pore network changes evaluated by**  
 472 **capillary absorption, even if the results obtained for the PAASi treatment could appear in**

473 contradiction with gravimetric test (*i.e.*, a reduction of the water absorbed by capillarity of about 2%  
 474 and an increase of WC% observed with neutron radiography), However, an accurate inspection of  
 475 water capillary absorption curves (Figure 2) can simply explain these observations. Indeed, during the  
 476 first minutes of contact with water, samples treated with PAASi absorbed more water than untreated  
 477 ones, even if a reduction of the total amount of water was observed at longer time steps.  
 478



479 **Figure 11.** Evolution of the water content during capillary water uptake for (a) untreated samples and samples treated with (b)  $AlSiX$   
 480 and (c) PAASi consolidants, and (d) hydrophobic product WS3.  
 481



482 **3.5 SANS**

483 The Q dependence of the coherent neutron scattered intensity of each untreated and treated sample,  $I(Q)$ , is  
484 depicted in **Figure 12**. As it was expected for these samples with a high porosity,  $I(Q)$  is dominated by the  
485 high contrast between pores and solid matter. Because the majority of pores is larger than the inverse of the  
486 minimum Q value of the experimental window ( $1/Q_{\min}$  is of the order of 25 nm), all the scattered intensity is  
487 due to the interfaces between solid matter and air in the pores.

488 The linear dependence of  $\log(I(Q))$  vs.  $\log Q$  is consistent with the fractal formalism that associates  
489 roughness to a fractal surface dimension  $D_s$ . SANS data **were** fitted by the addition of a power law and a  
490 constant:

$$I(Q) = C \cdot Q^{-\alpha} + const$$

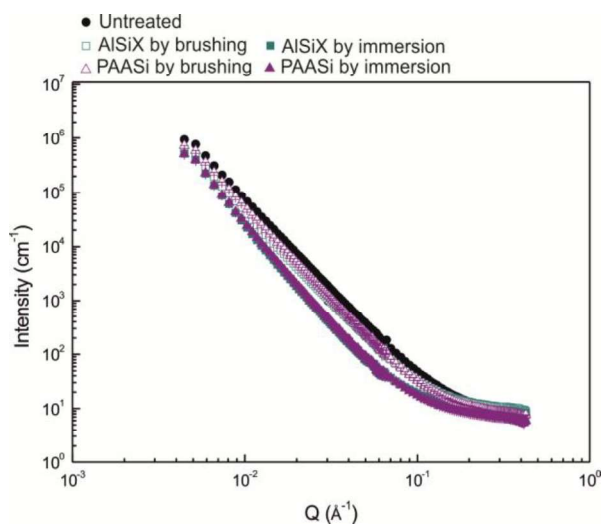
491 with  $\alpha$  ranging from  $-3$  to  $-4$ . The additive constant is due to the incoherent scattering essentially of  
492 hydrogen atoms present in the sample either through the chemical composition of additives or because of  
493 hydration water.

494 Within this simple model, a clear cut interface is associated to the exponent  $\alpha = 4$ , and  $C$  gives the total area  
495 of the interface (Porod's law). The scattering due to a rough surface interface can also be described by a  
496 power law of the same type:  $\alpha = 6 - D_s$ , with  $2 < D_s < 3$ . Obviously, a clear cut surface corresponds to  $D_s = 2$   
497 while the limit  $D_s = 3$  corresponds to a mathematically defined interface filling totally the volume.

498 By analogy, one can associate the roughness to  $D_s$ . The larger is  $D_s$  and higher is the roughness of the  
499 interface. In the matter in question, scattering curves collected on both untreated and treated samples are well  
500 described by fractal interfaces. Indeed, a surface fractal law fits the curves in the whole investigated Q range  
501 ( $Q_{\min} = 0.0044$ ,  $Q_{\max} = 0.42$ ) with a slope of the different  $I(Q)$  ranging from  $-3$  to  $-4$ , with variations related  
502 to the presence of the products on the pore surfaces.

503 Essentially, two different slopes are clearly observed, corresponding to values of  $D_s$  of the order of either  
504 2.4–2.5 or 2.8 (Table 6). Certainly, the first describes smoother interfaces, **whereas** the cases where  $D_s$  is of  
505 the order of 2.8 correspond to a higher roughness of the interfaces.

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507

508 *Figure 12. Scattered SANS intensity for untreated sample and samples treated with consolidants (AISiX and PAASi) by brushing or*  
 509 *by immersion.*

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Thus, starting from a rough surface described by a fractal dimension of 2.8 in the untreated stone, the application of the products by immersion clearly penetrated pores, **leading to** a smoothing of the pore surfaces. In contrast, a test with application of the products by brushing **did not lead to** relevant changes in the small pore-air interfaces, **and therefore did not greatly affect** the structural features of the substrate. **To summarize, SANS data clearly indicated that taking advantage from their nanosize, the tested products were able to penetrate also pores with a diameter of the order of the inverse of the investigated Q range. Products may occupy the pore surface as a smooth layer of particles. However, differences in surface roughness were only detected when products were applied by immersion, suggesting that this method is preferable because it ensures higher bonding of the product to the pore surface and the complete penetration of consolidants into nano-sized pores.**

**It has to be noticed that the roughness changes at the pore-air interfaces shown by the D, variations can also help to explain the modification of the drying rate due to the presence of products. In this direction, since nanoparticles were mainly located on pore surfaces and not inside the pores, they affected the second stage of the drying rate controlled by vapor diffusion at air-particle interface.**

526

#### 527 4. Conclusions

528 **In this study, a hybrid patented product constituted by polyamidoamine with siloxane functionality, named**  
 529 **PAASi, and a hybrid sol based on an Al-Si network functionalized with organic chains, named AISiX, were**

530 tested as consolidants on a calcarenite substrate (named Sabucina stone), alone or associated with the  
531 hydrophobic coating WS3 (based on colloidal silica with fluorinated groups). This study aimed at  
532 evaluating the compatibility of the studied hybrid products with porous calcareous stones and  
533 highlighting the merits of multi-scale laboratory investigation procedure.

534 The results showed that the Al-Si-based product is not advisable in material conservation of  
535 calcarenites because it led to unacceptable changes. On the contrary, calcarenite substrates could be  
536 treated with a polyamidoamine-based product, even if it showed a lower ability to reduce water  
537 absorption **assuring however acceptable vapor permeability reduction**. Some negative aspects and  
538 unwanted effects, such as chromatic changes or long-term preservation performances, could be  
539 overtaken by exploring alternative application methods and/or curing procedure. Generally, it is  
540 possible to argue that treatment by immersion is preferable, because it ensures a complete penetration  
541 of consolidants into nano-sized pores, not obtained by brushing. However, the application method  
542 could be improved, e.g., by washing the surface, wiping excess product after immersion, testing longer  
543 immersion procedures, and/or different curing time. Finally, as regards the combined consolidation  
544 and protective application, it has to be carefully evaluated by considering the influence of the  
545 hydrophobic coating in the kinetics of drying and in supersaturation equilibria when moisture can go  
546 through the hydrophobic barrier (e.g., after the partial removal of product due to weathering and/or  
547 the possible discontinuous coating on the substrate), **as suggested also by the dramatic reduction of the**  
548 **water vapor permeability**. Of course, additional studies will be welcomed in order to explore the possible  
549 ability of this class of hybrid coatings to preserve different kind of substrates, especially low porous  
550 ones, for which consolidation appears particularly critical.

551 Going to evaluate the potential of integrating multi-scale methods in consolidation tests, water  
552 absorption, mercury intrusion porosimetry, and  $\mu$ CT methods **offered** together an overview on the changes  
553 in pore structure of the studied stone in the range 0.007–200  $\mu$ m after the application of consolidant  
554 products. They provided consistent results, even if some discrepancies due to the intrinsic differences among  
555 the applied methods have to be considered [67]. **Thus**, the applied approach, and especially the use of  
556 imaging and small angle scattering methods allowed to better understand interactions between new products  
557 and substrates, supplying quantitative data about pore ranges in which consolidants interact with stone, and

558 adequately supporting the interpretation of material behavior especially against water. In this direction, the  
559 possibility to incorporate standard routines and/or substitute destructive testing with non-destructive ones  
560 seems to be a valid alternative to evaluate efficiency and monitor behavior of stones treated with consolidant  
561 products.

562

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565 **tests.**

566

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761 **Tables**

762

763 **Table 1.** Summary of the number, shape, and dimension of the analyzed samples.

Test or experiment	Number of sample	Shape	Dimension	Product location	Standard recommendation
Microscopic analysis	5	Thin section	standard	Around the sample	
Colorimetric test	15 (3 per treatment)	Cubes	4x4x4 cm <sup>3</sup>	Top of the sample	UNI EN 15886:2010
Static contact angle	4	Cubes	4x4x4 cm <sup>3</sup>	Top of the sample	UNI 11207:2007
Capillary water absorption	15 (3 per treatment)	Cubes	4x4x4 cm <sup>3</sup>	Around the sample	UNI EN 15801:2010
Total immersion	75 (15 per treatment)	Cubes	4x4x4 cm <sup>3</sup>	Around the sample	NORMAL 7/81
Resistance to salt crystallization	75 (15 per treatment)	Cubes	4x4x4 cm <sup>3</sup>	Around the sample	UNI EN 12370:2001
DRMS	5 (1 per treatment, 4 holes)	Cubes	7x7x7 cm <sup>3</sup>	Around the sample	
MIP analysis	9 (3 per treatment)	Cubes	1 cm <sup>3</sup>	Top of the sample	
X-ray micro-tomography	2 (1 per treatment)	Cylinder	7 mm in diameter	Top of the sample	
Neutron radiography	15 (3 per treatment)	Parallelepiped	2x2x4 cm <sup>3</sup>	Around the sample	
SANS	5 (1 per treatment)	Thin slices	< 1 mm thick	Around the sample	

764

765 **Table 2.** Average color difference  $\Delta E^*$  of untreated samples and samples treated with both consolidants  
 766 (PAASi and AlSiX) and hydrophobic (WS3) products.

Samples	$L^*$	$a^*$	$b^*$	$\Delta E^*$ ( $n = 3$ )
Untreated	66	5	21	
PAASi	63	7	25	<b>5</b>
PAASi + WS3	63	6	24	<b>4</b>
AlSiX	56	8	29	<b>13</b>
AlSiX + WS3	52	12	30	<b>18</b>

767

768 **Table 3.** Physical properties ( $\pm$  standard deviation) of untreated samples and samples treated with both  
 769 consolidants (PAASi and AlSiX) and hydrophobic (WS3) products. AC is the absorption coefficient, CI is  
 770 the imbibition coefficient, DI is the drying index, and  $\Delta M$  is the mass variation after salt crystallization test.

Samples	AC ( $\text{g cm}^{-2} \text{t}^{-0.5}$ ) <sup>1</sup> ( <i>n</i> = 3)	CI (%) <sup>2</sup> ( <i>n</i> = 15)	DI (%) <sup>3</sup> ( <i>n</i> = 15)	$\Delta M$ (%) <sup>4</sup> ( <i>n</i> = 15)
Untreated	0.03 $\pm$ 0.01	11.5 $\pm$ 1.2	0.4	-11.1
PAASi	0.04 $\pm$ 0.01	10.8 $\pm$ 0.8	0.7	-6.6
PAASi + WS3	0.02 $\pm$ 0.01	11.1 $\pm$ 2.0	0.7	-12.7
AlSiX	0.02 $\pm$ 0.01	10.4 $\pm$ 0.4	0.7	-21.8
AlSiX + WS3	0.01 $\pm$ 0.01	10.8 $\pm$ 0.5	0.5	-19.5

<sup>1</sup>UNI EN 15801:2010; <sup>2</sup>NORMAL 7/81; <sup>3</sup>NORMAL 29/88; <sup>4</sup>UNI EN 12370:2001

771

772 **Table 4.** Average parameters ( $\pm$  standard deviation) derived from mercury intrusion porosimetry on  
 773 untreated samples and samples treated with consolidants (AlSiX and PAASi).

Parameters	Untreated ( <i>n</i> = 3)	PAASi ( <i>n</i> = 3)	AlSiX ( <i>n</i> = 3)
Total intruded volume ( $\text{cm}^3 \text{g}$ )	0.14 $\pm$ 0.01	0.14 $\pm$ 0.02	0.13 $\pm$ 0.01
Bulk density ( $\text{g cm}^{-3}$ )	1.98 $\pm$ 0.05	1.95 $\pm$ 0.10	1.98 $\pm$ 0.05
Apparent density ( $\text{g cm}^{-3}$ )	2.71 $\pm$ 0.06	2.67 $\pm$ 0.06	2.65 $\pm$ 0.02
Porosity (%)	26.86 $\pm$ 0.94	27.07 $\pm$ 3.09	25.44 $\pm$ 1.75
Total surface area ( $\text{m}^2 \text{g}$ )	1.89 $\pm$ 0.20	1.75 $\pm$ 0.22	1.17 $\pm$ 0.22
Average pore radius ( $\mu\text{m}$ )	0.14 $\pm$ 0.01	0.16 $\pm$ 0.04	0.22 $\pm$ 0.02
Modal pore radius ( $\mu\text{m}$ )	8.56 $\pm$ 30.9	14.22 $\pm$ 5.07	12.55 $\pm$ 2.50
Median pore radius ( $\mu\text{m}$ )	2.25 $\pm$ 0.12	2.90 $\pm$ 1.30	4.21 $\pm$ 0.45

774

775 **Table 5.** Sorptivity parameter *B* ( $\pm$  standard deviation) calculated for untreated samples and samples treated  
 776 with consolidant (AlSiX and PAASi) and hydrophobic (WS3) products.

Samples	Sorptivity parameter <i>B</i> ( $\text{mm s}^{-0.5}$ ) ( <i>n</i> = 3)
Untreated	0.69 $\pm$ 0.01
PAASi	0.59 $\pm$ 0.01
PAASi + WS3	0.00 $\pm$ 0.00
AlSiX	0.56 $\pm$ 0.01
AlSiX + WS3	0.00 $\pm$ 0.00

777

778 **Table 6.** Calculated fractal dimension from  $\alpha$  exponent for untreated sample and samples treated with  
779 consolidants (AlSiX and PAASi) by brushing or by immersion.

Samples	$C$ ( $\text{cm}^{-1}$ )	$\alpha$	$D_s$
Untreated	$8.5 \pm 0.1$	$-3.1545 \pm 0.0003$	2.8
PAASi by brushing	$6.3 \pm 0.1$	$-3.2239 \pm 0.0004$	2.8
AlSiX by brushing	$9.7 \pm 0.1$	$-3.2396 \pm 0.0004$	2.8
PAASi by immersion	$6.6 \pm 0.1$	$-3.5356 \pm 0.0006$	2.5
AlSiX by immersion	$9.1 \pm 0.1$	$-3.5935 \pm 0.0006$	2.4

780

**Method Details (MethodsX)**

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