

Effect of planet ingestion on low-mass stars evolution: the case of 2MASS J08095427–4721419 star in the Gamma Velorum cluster

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ABSTRACT

We analysed the effects of planet ingestion on the characteristics of a pre-main-sequence star similar to the Gamma Velorum cluster member 2MASS J08095427–4721419 (#52). We discussed the effects of changing the age t_0 at which the accretion episode occurs, the mass of the ingested planet and its chemical composition. We showed that the mass of the ingested planet required to explain the current $[\text{Fe}/\text{H}]^{\#52}$ increases by decreasing the age t_0 and/or by decreasing the iron content of the accreted matter. We compared the predictions of a simplified accretion method – where only the variation of the surface chemical composition is considered – with that of a full accretion model that properly accounts for the modification of the stellar structure. We showed that the two approaches result in different convective envelope extension which can vary up to 10 per cent. We discussed the impact of the planet ingestion on a stellar model in the colour–magnitude diagram, showing that a maximum shift of about 0.06 dex in the colour and 0.07 dex in magnitude are expected and that such variations persist even much later the accretion episode. We also analysed the systematic bias in the stellar mass and age inferred by using a grid of standard non-accreting models to recover the characteristics of an accreting star. We found that standard non-accreting models can safely be adopted for mass estimate, as the bias is $\lesssim 6$ per cent, while much more caution should be used for age estimate where the differences can reach about 60 per cent.

Key words: planet–star interactions – stars: abundances – stars: chemically peculiar – stars: evolution – stars: formation – stars: pre-main sequence.

1 INTRODUCTION

Recently, Spina et al. (2014) found a chemically peculiar star, namely 2MASS J08095427–4721419 (hereafter #52), in the young Gamma Velorum cluster. This star is significantly metal richer ($[\text{Fe}/\text{H}]^{\#52} = +0.07 \pm 0.07$) than the cluster itself ($[\text{Fe}/\text{H}]^{\text{cl}} = -0.057 \pm 0.018$), showing also an overabundance of refractory elements (e.g. Mg, Al, Sc, Ti, V and Co), which are expected to condensate in a protoplanetary disc (Spina et al. 2015). Spina et al. (2014, 2015) suggested that those chemical abundance peculiarities might be ascribed to one or more episodes of planet engulfment, a scenario that has already been proposed to explain chemical anomalies found in iron-rich and/or lithium-rich hosting planets stars (see e.g. Gonzalez 1997; Laughlin & Adams 1997; Israelian et al. 2001; Montalbán & Rebolo 2002; Ashwell et al. 2005; Carlberg et al. 2010, and references therein).

Spina et al. (2014) estimated a mass of about $1.3 M_{\odot}$ for #52 relying on standard stellar models that do not take into account mass accretion episodes. At the age of the cluster, i.e. 10–20 Myr (Jeffries et al. 2014), a star of $1.3 M_{\odot}$ is in an advanced enough stage of the pre-main-sequence (MS) evolution to have already developed a sizeable radiative core and to have an external convective region thinner than a few per cent of the total mass.

The ingestion of a rocky planet on a star with these characteristics is thus able to produce significant surface chemical abundance anomalies as the metal-rich material is diluted in a thin convective envelope. Clearly, the extent of the anomalies depends on the planet characteristics – its mass and chemical composition – and on the mass of the stellar convective envelope.

Spina et al. (2014) assumed that the planet accretion episode does not affect the structure of the star and in particular the extension of its convective envelope. Within such a simplified assumption, the only effect of the planet ingestion is the modification of the surface chemical composition, which can be easily computed. Following this approach, they found that the ingestion of a rocky planet with mass in the range of 50–70 M_{\oplus} in the last 5 Myr would be enough to produce the observed high- $[\text{Fe}/\text{H}]^{\#52}$ value.

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The main aim of this paper is twofold: (1) to extend the analysis performed by Spina et al. (2014, 2015) by computing stellar models that consistently follow the accretion episode and (2) to quantify the resulting differences. Unfortunately, the details of the accretion are not known and cannot be directly obtained from the observations. As such, this work is intended to be a first investigation of the main effects of a single episode of planet ingestion on a star similar to #52. We focused on the impact on the results of the age at which the accretion begins and of the properties of the accreted planet, such as its mass and chemical composition. The only constraint imposed to the models is to reproduce the observed high-[Fe/H]^{#52} value after the accretion process.

The paper is structured as it follows. In Sections 2 and 3, we summarized the main characteristics of the computed stellar evolutionary models with and without accretion. In Sections 4 and 5, we analysed the impact of the accretion on the surface chemical composition ([Fe/H], total metallicity Z and heavy element abundances), discussing the differences between the full and the simplified accretion model. In Section 6, we analysed the effect of the planet ingestion on the theoretical predictions for the position of the star in the colour–magnitude diagram (CMD). In Section 7, we discussed the systematic error induced in recovering the properties of the star that ingested a planet (i.e. mass and age) with standard evolutionary tracks that do not take into account the accretion episode.

2 STELLAR MODELS

We computed the stellar models by means of the Pisa evolutionary code (PROSECCO; Tognelli et al. 2015; Tognelli, Prada Moroni & Degl’Innocenti 2015a) – an updated version of the FRANEC code (see e.g. Degl’Innocenti et al. 2008; Tognelli, Prada Moroni & Degl’Innocenti 2011; Dell’Omodarme et al. 2012) – adopting the same input physics/parameters and the thin-disc mass-accretion treatment described in Tognelli, Prada Moroni & Degl’Innocenti (2015b).

To compute stellar models to be compared against stars with an observed [Fe/H] value, proper values of the initial helium and metal abundances must be chosen. To do this, we used equations 1 and 2 given in Gennaro, Prada Moroni & Degl’Innocenti (2010) assuming the Asplund et al. (2009) solar-scaled metals distribution. The [Fe/H] values (hereafter [Fe/H]_{G07}) provided by Spina et al. (2014) for the Gamma Velorum cluster and #52 are referred to the Grevesse, Asplund & Sauval (2007) solar iron abundance, i.e. $\log \epsilon_{\text{Fe},\odot}^{\text{G07}} \equiv 12 + \log(N_{\text{Fe}}/N_{\text{H}})_{\odot} = 7.45$. Such a value is slightly different from the more recent Asplund et al. (2009) one ($\log \epsilon_{\text{Fe},\odot}^{\text{AS09}} = 7.50$) adopted in our stellar models. Thus, for consistency, we converted the [Fe/H]_{G07} into the [Fe/H]_{AS09} using the [Fe/H] definition, namely

$$[\text{Fe}/\text{H}] \equiv \log \left(\frac{N_{\text{Fe}}}{N_{\text{H}}} \right)_{*} - \log \epsilon_{\text{Fe},\odot} + 12. \quad (1)$$

In our case, applying equation (1) we obtained

$$\begin{aligned} [\text{Fe}/\text{H}]_{\text{AS09}} &= [\text{Fe}/\text{H}]_{\text{G07}} + \log \epsilon_{\text{Fe},\odot}^{\text{G07}} - \log \epsilon_{\text{Fe},\odot}^{\text{AS09}} \\ &= [\text{Fe}/\text{H}]_{\text{G07}} - 0.05. \end{aligned} \quad (2)$$

By adopting, respectively, [Fe/H]_{G07}^{cl} = −0.057 and [Fe/H]_{G07}^{#52} = +0.07 for the bulk of the cluster and for #52 (Spina et al. 2014), the conversion leads to [Fe/H]_{AS09}^{cl} = −0.107 and to [Fe/H]_{AS09}^{#52} = +0.02, which, in turn, translate into the following initial helium and metal contents, ($Y^{\text{ini}} = 0.269$, $Z^{\text{ini}} = 0.0102$)_{cl} and ($Y^{\text{ini}} = 0.275$, $Z^{\text{ini}} = 0.0135$)_{#52}.

To analyse the impact of the ingestion of a planet on stellar evolution, we first computed a grid of standard models (hereafter STD models, reference set) in the mass range [1.0, 1.4] M_{\odot} with a mass spacing of 0.01 M_{\odot} , evolved from the beginning of the Hayashi track – without any accretion episode – to the exhaustion of the central hydrogen. We selected this mass range as the mass we obtained for the #52 star is approximately 1.2 M_{\odot} (see Section 3.1).

Standard non-accreting models have been computed with the low-[Fe/H] value ($[\text{Fe}/\text{H}]_{\text{AS09}}^{\text{cl}} = -0.107$, $Y^{\text{ini}} = 0.269$ and $Z^{\text{ini}} = 0.0102$), representative of both the bulk of the cluster and of the initial chemical composition of #52, if the accretion hypothesis is fulfilled. A set of standard non-accreting models with the high-[Fe/H] value measured for #52 ($[\text{Fe}/\text{H}]_{\text{AS09}}^{\text{\#52}} = +0.02$, $Y^{\text{ini}} = 0.275$ and $Z^{\text{ini}} = 0.0135$) is also computed, to take into account the possibility that #52 was born with a chemical composition different from the cluster one and equal to that currently observed.

As a second step, we computed models with the low-[Fe/H] value that follow the accretion episode. The planet ingestion is supposed to occur in a single episode at a stellar age t_0 . To check the effect of changing the age at which the accretion episode occurs, we adopted three t_0 values, namely $t_0 = 10, 12$, and 15 Myr, where the last one approximately corresponds to the estimated age of the Gamma Velorum cluster. We did not investigate cases for $t_0 < 10$ Myr because, as we will show in Section 3.1, the mass of the planet required to reproduce the observed [Fe/H]_{AS09}^{#52} would reach unrealistic large values.

Since we are interested in the impact on the stellar evolution of a planet ingestion episode, with particular attention to the surface chemical composition, we analysed the effect of accreting matter with two different metal distributions. For simplicity, the accreted matter is assumed to be hydrogen- and helium-free, thus we adopted $Z^{\text{p}} = 1$ for the metal abundance of the ingested planet. In one case, we assumed the same metal mass fraction relative abundances of the star (i.e. the solar-like mixture by Asplund et al. 2009, hereafter AS09),¹ thus matter mainly composed by oxygen, carbon, neon and iron. In the following, we will refer to this case as the iron-poor distribution. In the other case, we adopted the same metal distribution of the Earth (Javoy et al. 2010, hereafter JK10), thus a material mainly constituted by iron, oxygen, silicon and magnesium (hereafter iron-rich case). This last case corresponds to accrete matter where the volatile elements are absent and where the condensation processes have occurred – as expected in the case of rocky planets – and hence compatible with the overabundance of refractory elements measured by Spina et al. (2015) in the spectra of #52.

The relative mass abundances of the metals $z_i^{\text{p}} \equiv X_i^{\text{p}}/Z^{\text{p}}$ for the two adopted distributions are listed in Table 1. It is important to notice that the iron content in the two mixtures is different, being the iron abundance in Earth-like one (JK10) about 3.4 times larger than that in the solar-like mixture (AS09). In the next sections, we will discuss the impact of such a difference on the models.

In the following, we will show the evolutionary tracks in the observed CMD. To convert the models from the theoretical ($\log T_{\text{eff}}$, $\log L/L_{\odot}$) to the observed ($B - V$, M_V) plane, we used the bolometric corrections computed from the synthetic spectra by Allard, Homeier & Freytag (2011) – for several $\log g$, $\log T_{\text{eff}}$ and [Fe/H] values – and applying the formalism described in Girardi

¹ Metal mass fraction relative abundance is the ratio between the mass fraction abundance of the i th metal X_i and the total metallicity Z . For a solar-like metal distribution (or mixture) $(X_i/Z)_{*} = (X_i/Z)_{\odot}$.

Table 1. Metals relative abundances \bar{z}_i^P used for the accreted matter^a.

Elem.	$\bar{z}_i^P \equiv X_i^P/Z^P$		Elem.	\bar{z}_i^P	
	AS09	JK10		AS09	JK10
C	0.176 99	0.0	Cl	0.000 61	0.0
N	0.051 85	0.0	Ar	0.005 49	0.0
O	0.429 02	0.310 96	K	0.000 22	0.0
Ne	0.094 03	0.0	Ca	0.004 80	0.008 63
Na	0.002 19	0.0	Ti	0.000 23	0.000 50
Mg	0.052 97	0.130 40	Cr	0.001 24	0.003 61
Al	0.004 16	0.008 63	Mn	0.000 81	0.0
Si	0.049 76	0.189 58	Fe	0.096 69	0.329 02
P	0.000 43	0.0	Ni	0.005 33	0.018 67
S	0.023 14	0.0			

Note. ^aThe \bar{z}_i^P mass abundances have been re-normalized to sum to unity.

et al. (2002). Since the surface [Fe/H] value of the accreting stellar models changes in time, the colour transformations have been performed using the actual surface [Fe/H] at each stellar age.

3 ACCRETION MODELS

To quantify the impact of a planet ingestion episode on stellar surface iron abundance, we followed two different approaches, one quite simplified but with the advantage of being easily implemented by means of the commonly available STD models and the other more accurate and realistic but computationally more demanding. In the former case, similarly to Spina et al. (2014), we assumed that the planet ingestion does not affect the evolution of the stellar structure, in particular, leaving unaltered the extension of the convective envelope with respect to that of standard non-accreting models. On the contrary, in the latter case, we actually followed the accretion process computing consistently the structure evolution of non-standard stellar models in presence of matter accretion. The differences between such approaches are discussed in the following sections.

3.1 Simplified accretion models

In this first type of models, following an approach similar to that of Spina et al. (2014), we assumed that the only effect of accretion is the change of the surface chemical abundances. In such a scenario, the final surface iron abundance can be easily computed assuming that the accreted metal-rich matter is completely mixed and diluted with that within the convective envelope of the STD model (i.e. non-accreting model). Clearly, for a given planet, the final surface abundance strongly depends on the dilution process efficiency, i.e. on the extension of the convective envelope, which in turn depends on the characteristics of the stellar model, i.e. mass, age and initial chemical composition.

Assuming that the matter of the ingested planet M_p is instantaneously and fully mixed with that contained in the convective envelope $\Delta M_{c.e.}$, the mass fraction abundance of the i th-element inside the convective envelope after the accretion process X_i^{new} is given by the following equation:

$$X_i^{\text{new}} = \frac{X_i \Delta M_{c.e.} + X_i^P M_p}{\Delta M_{c.e.} + M_p}, \quad (3)$$

where X_i and X_i^P are the i th-element mass fraction abundance of the matter inside the stellar convective envelope before the accretion and in the ingested planet, respectively. From equation (3), one

can immediately obtain the surface total metallicity Z^{new} after the accretion episode,

$$Z^{\text{new}} = \frac{Z \Delta M_{c.e.} + Z^P M_p}{\Delta M_{c.e.} + M_p} \quad (4)$$

and the corresponding [Fe/H] surface value,

$$[\text{Fe}/\text{H}]^{\text{new}} = \log \left(\frac{X_{\text{Fe}}^{\text{new}} m_{\text{H}}}{X_{\text{H}}^{\text{new}} m_{\text{Fe}}} \right) - \log \epsilon_{\text{Fe}, \odot} + 12, \quad (5)$$

where m_{H} and m_{Fe} are the hydrogen and iron atomic masses and $\log \epsilon_{\text{Fe}, \odot} = \log \epsilon_{\text{Fe}, \odot}^{\text{AS09}} = 7.50$ (AS09). By inverting equations (3) and (5), the mass of the ingested planet needed to obtain the requested $[\text{Fe}/\text{H}]^{\text{new}}$ can also be computed,

$$\frac{M_p}{\Delta M_{c.e.}} = \frac{X_{\text{H}} \times 10^{([\text{Fe}/\text{H}]^{\text{new}} + \beta) - X_{\text{Fe}}}}{X_{\text{Fe}}^P}, \quad (6)$$

where $\beta = \log \epsilon_{\text{Fe}, \odot}^{\text{AS09}} - 12 + \log m_{\text{Fe}}/m_{\text{H}}$.

It is evident from equations (3)–(5) that, once the stellar model has been fixed (i.e. mass and chemical composition), the variation of the stellar surface chemical abundances depends on $\Delta M_{c.e.}$ – which changes with the age and hence t_0 – on the ingested planet mass M_p and on its chemical composition X_i^P . This implies that the mass of the ingested planet required to reproduce the observed surface chemical anomalies (the high-[Fe/H] value) depends only on t_0 and on the planet chemical composition, in particular on X_{Fe}^P (see equation 6), once the stellar model has been fixed.

Concerning the characteristics of the star, we adopted an initial mass $M = 1.2 M_{\odot}$, as obtained to reproduce the position in the CMD of #52, i.e. $(B - V) = 0.65$ and $M_V = 3.95$ (Spina et al. 2014), with our own evolutionary tracks with the same metallicity of the cluster $[\text{Fe}/\text{H}]_{\text{AS09}}^{\text{cl}} = -0.107$ (i.e. $Y^{\text{ini}} = 0.269$, $Z^{\text{ini}} = 0.0102$) at an age of about 15 Myr (see Section 6), the mid-value of the cluster age range (10–20 Myr) estimated by Jeffries et al. (2014).

The mass of the ingested planet depends on the extension of the convective envelope of standard tracks, which, having fixed the stellar mass and initial chemical composition, is a function of the age of the star. Top panel of Fig. 1 shows the temporal evolution the convective envelope mass extension during the pre-MS for our reference model (i.e. $M = 1.2 M_{\odot}$ and $[\text{Fe}/\text{H}] = -0.107$). In the selected time interval, the convective envelope progressively reduces due to the radiative opacity decrease in the envelope. For this particular stellar mass and chemical composition, the surface convection vanishes at an age of about 17 Myr.

Bottom panel of Fig. 1 shows how the mass of the ingested planet changes, as a function of the age t_0 at which the accretion episode occurs. The computations have been performed for a star of $1.2 M_{\odot}$ which accretes matter with both the solar-like (AS09) and the Earth-like (JK10) heavy elements abundances. For a chosen planet chemical composition, the mass of the ingested planet necessary to account for the observed $[\text{Fe}/\text{H}]_{\text{AS09}}^{\#52}$ is proportional to the mass of the convective envelope $\Delta M_{c.e.}$ (see equation 6) which in turn varies with t_0 . The earlier is the accretion (i.e. the smaller is t_0) and the thicker is the convective envelope and, consequently, the greater is the dilution of the accreted matter with the pristine stellar one and the larger is the requested planet mass M_p . Notice that for $t_0 \gtrsim 17$ Myr, the convective envelope disappears and consequently the derived planet mass drops to zero.

For the selected stellar mass, we explored three values of t_0 , namely 10, 12 and 15 Myr, the last approximatively corresponding to the cluster age. With this choice, in the case of the solar-like mixture (AS09), we obtained from equation (6) the following approximated values of the mass of the ingested planet, $M_p = 180$

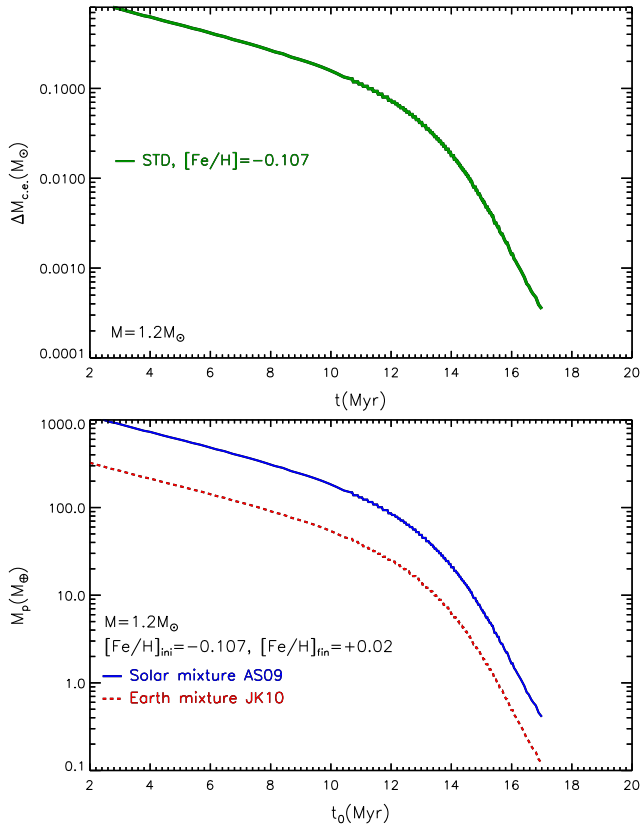


Figure 1. Top panel: temporal evolution of the convective envelope mass extension for the STD model with $M = 1.2 M_{\odot}$ and $[\text{Fe}/\text{H}] = -0.107$. Bottom panel: ingested planet mass as a function of the age t_0 at which the ingestion occurs, for the solar-like (AS09, solid blue line) and for the Earth-like heavy elements mixture (JK10, dashed red line).

Table 2. Mass values of the ingested planet for the three selected ages t_0 , obtained using equation (6) and the iron-poor and iron-rich mixture.

$t_0 =$	10 Myr	12 Myr	15 Myr
Iron-poor mixture: (AS09) Solar-like mixture			
$M_p (M_{\oplus})$	180	90	7
Iron-rich mixture: (JK10) Earth-like mixture			
$M_p (M_{\oplus})$	53	26	2

($t_0 = 10$ Myr), 90 (12 Myr) and $7 M_{\oplus}$ (15 Myr). For the same t_0 values, M_p reduces to $M_p = 53$ (10 Myr), 26 (12 Myr) and $2 M_{\oplus}$ (15 Myr), if the Earth-like mixture is adopted. The obtained M_p values are summarized in Table 2.

We emphasize that the mass of the ingested planet – at a given age t_0 and planet composition – is fixed by the constraint $[\text{Fe}/\text{H}]^{\text{new}} = [\text{Fe}/\text{H}]^{\#52}$. Moreover, we also assumed that the initial mass of the accreting stellar model is fixed to $1.2 M_{\odot}$. Thus, from equation (6) the ingested planet mass M_p depends only on (1) the age t_0 (through $\Delta M_{\text{c.e.}}$) and (2) on the iron content of the accreted planet, i.e. X_{Fe}^{p} .

If the chemical composition of the planet is fixed then the right-hand side of equation (6) is constant and independent of t_0 . This implies that the ratio $M_p/\Delta M_{\text{c.e.}}$ has to be constant, too. A change of the age t_0 at which the accretion occurs directly translates into a change of the convective envelope extension $\Delta M_{\text{c.e.}}$, and the mass of the ingested planet M_p must change accordingly, to keep the

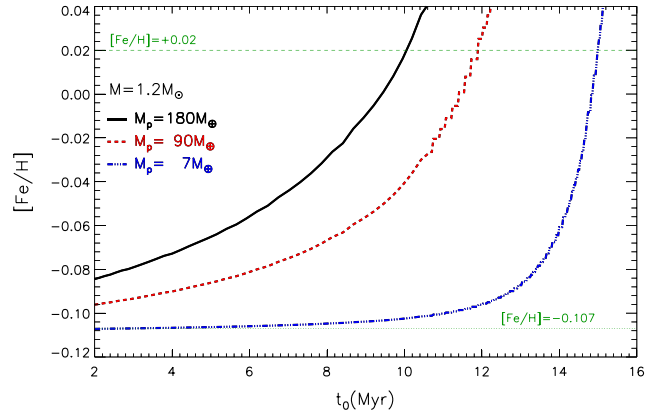


Figure 2. Surface $[\text{Fe}/\text{H}]$ value as a function of t_0 . Results for the three values of accreted mass $M_p = 7, 90$ and $180 M_{\oplus}$ with the solar-like AS09 metal distributions are shown.

$M_p/\Delta M_{\text{c.e.}}$ ratio constant. In particular if t_0 increases, $\Delta M_{\text{c.e.}}$ decreases and M_p must decrease too. This case corresponds to move along one of the rows of Table 2 (from left to right).

On the other hand, at a fixed age t_0 – fixed $\Delta M_{\text{c.e.}}$ – the change of the planet chemical composition (i.e. X_{Fe}^{p}) modifies the right-hand side of equation (6) and the ratio $M_p/\Delta M_{\text{c.e.}}$ must change consequently. The use of the Earth-like mixture – with an iron content about 3.4 times larger than that in the solar mixture – leads to a reduction of the $M_p/\Delta M_{\text{c.e.}}$ ratio and, consequently, to a decrease of the ingested planet mass – being $\Delta M_{\text{c.e.}}$ fixed. This case corresponds to move along one of the columns of Table 2.

Fig. 2 shows how the final surface $[\text{Fe}/\text{H}]$ changes as a function of the age t_0 at which the planet ingestion occurs in a star of $1.2 M_{\odot}$ and initial $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]_{\text{AS09}}^{\text{cl}}$. The figure shows the results obtained using equation (5) with the three different values of the ingested planet, namely $M_p = 7$ ($t_0 = 15$ Myr), 90 (12 Myr) and $180 M_{\oplus}$ (10 Myr), adopting the AS09 solar mixture for the planet.

For a given M_p , there is a specific value \bar{t}_0 at which the planet must be ingested to produce the observed $[\text{Fe}/\text{H}]_{\text{AS09}}^{\#52}$. If the accretion begins earlier than \bar{t}_0 , i.e. $t_0 < \bar{t}_0$, then the amount of metal-rich material supplied to the star is not enough to produce the requested surface $[\text{Fe}/\text{H}]_{\text{AS09}}^{\#52}$, as it is diluted in a thicker convective envelope. On the other hand, if the accretion starts later than \bar{t}_0 , i.e. $t_0 > \bar{t}_0$, then the resulting $[\text{Fe}/\text{H}]$ is larger than the requested value as the accreted material is diluted in a thinner convective envelope. Consequently, having fixed the mass M_p , the final surface $[\text{Fe}/\text{H}]$ strongly depends on the age t_0 at which the accretion occurs.

The results presented in Fig. 2 are unchanged if the Earth-like mixture (JK10) is adopted in place of the solar-like one (AS09). The reason is that in both the cases, the mass of the ingested planet is chosen in order to contain the same total iron content and to obtain exactly the same final $[\text{Fe}/\text{H}]$.

In the discussion above, we assumed that the stellar mass is fixed. This is a good assumption in our case because we focused on the analysis of a particular star (#52) for which we have an estimate of both the age and the mass by fitting its CMD location by means of our stellar tracks. However, it is worth to check the dependence of the presented results (i.e. mass of ingested planet) on the adopted stellar mass.

Fig. 3 shows the derived ingested planet mass as a function of the stellar mass at a fixed t_0 , in the mass range $[1.0, 1.4] M_{\odot}$. As in the previous cases, we imposed to reproduce the surface $[\text{Fe}/\text{H}]_{\text{AS09}}^{\#52}$ starting from the initial $[\text{Fe}/\text{H}]$ of the cluster. We performed the

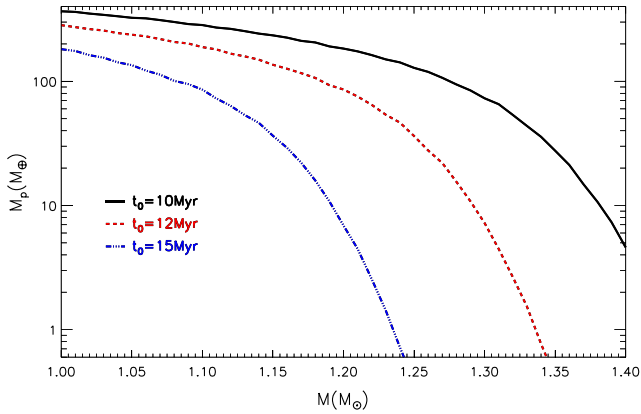


Figure 3. Ingested planet mass M_p as a function of the stellar mass for the simplified accretion model with $[\text{Fe}/\text{H}] = -0.107$, for $t_0 = 10, 12$ and 15 Myr and the solar-like (AS09) heavy elements mixture in the accreted matter.

analysis for the same three values of the age at which the accretion occurs used in the previous discussion, namely $t_0 = 10, 12$ and 15 Myr.

As expected, at a fixed t_0 , the value of M_p changes with the stellar mass. We recall that the mass of the ingested planet derived in the simplified accretion model is proportional to the mass inside the convective envelope and, as well known, the larger is the stellar mass the smaller is the convective envelope at the same evolutionary stage during the pre-MS. Moreover, the evolutionary time-scale of a star decreases by increasing its mass. Hence, for a fixed t_0 , the convective envelope gets thinner and thinner (until it eventually disappears) as the mass increases, causing the rapid decrease of the derived M_p . Fig. 3 also shows that the decrease of M_p versus the stellar mass is amplified at increasing t_0 . Thus, for a given t_0 , the value of the derived ingested planet mass might significantly change by varying the mass of the star that is supposed to accrete.

If the Earth-like metal distribution is adopted in the ingested planet, the results are similar with the only difference that the mass of the planet is smaller by a factor $X_{\text{Fe}}(\text{JK10})/X_{\text{Fe}}(\text{AS09}) \approx 3.4$.

3.2 Full accretion models

The simplified procedure described in the previous section and already adopted by Spina et al. (2014), although straightforward to be implemented, is not fully consistent, as the accretion of metal-rich material necessarily modifies the stellar structure and evolution after the planet ingestion. The ingestion of metal-rich material and the consequent increase in the radiative opacity leads to a deeper convective envelope and a lower effective temperature. Spina et al. (2014) did not show the effect of properly treating the accretion process during the stellar evolution on the position of the track in the CMD and, consequently, on the inferred age and mass of the star.

To analyse such an effect, we computed a second class of models by consistently following the accretion episode in stellar evolution calculation (hereafter ACC models). In this case, the star is evolved at constant mass with the initial $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]_{\text{AS09}}^{\text{cl}} = -0.107$ from the beginning of the Hayashi track to the age t_0 , when the planet ingestion occurs. Then, the mass is accreted, using exactly the same values of t_0 , M_p and chemical compositions quoted in Section 3.1, with the accretion process consistently followed during the stellar evolution.

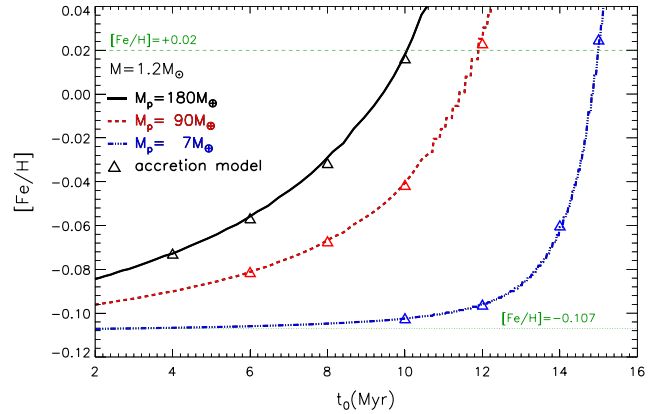


Figure 4. The same as in Fig. 2 with overlotted the $[\text{Fe}/\text{H}]$ values obtained from the full accretion models after the accretion episode (empty triangles).

To do this, we adopted the same accretion formalism described in Tognelli et al. (2015b). The accretion is supposed to interest only a very small area of the star so that the most of the stellar surface is freely radiating the energy, allowing us to adopt the same boundary conditions (i.e. atmosphere models) used for the computation of non-accreting models. The mass is accreted only in the convective envelope where it is instantaneously mixed with the stellar matter contained in it. The accretion of matter modifies the whole stellar structure evolution because of the change of the total mass (gravitational energy) and of the chemical composition within the convective envelope. We discuss the results in the next sections.

4 SURFACE $[\text{Fe}/\text{H}]$ AND GLOBAL METALLICITY EVOLUTION

In the simplified models described in Section 3.1, the surface iron abundance evolution of a planet-ingesting star is a simple step function, with $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]_{\text{low}}$ for $t < t_0$ and $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]_{\text{high}}$ for $t \geq t_0$. However, as mentioned in Section 3.2, the surface iron abundance evolution occurring in fully accretion models computation is more complex as the planet ingestion modifies also the stellar structure evolution.

Fig. 4 shows the surface $[\text{Fe}/\text{H}]$ after the accretion episode obtained using the full accretion model, computed for different values of t_0 . We performed the analysis using the three M_p used in the simplified accretion case, namely 7, 90 and $180 M_{\oplus}$ (AS09 solar mixture). The results of the full accretion model is compared to the predictions of the simplified one with the same M_p . As already discussed, for a given M_p there is only one specific value of the accretion age \bar{t}_0 that produces the requested final $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]^{\#52}$. We computed the surface $[\text{Fe}/\text{H}]$ for full accreting models at three $t_0 < \bar{t}_0$ and at $t_0 = \bar{t}_0$. Figure shows that the surface $[\text{Fe}/\text{H}]$ after the planet ingestion obtained using the simplified accretion model fully agrees with that predicted by the detailed accretion one. Slight differences are present only in the case of large planets accretion, $M_p \gtrsim 90 M_{\oplus}$. In this case, the detailed calculations show a tendency of producing a lower $[\text{Fe}/\text{H}]$ after the accretion episode, although the difference is always smaller than 0.01 dex.

To better analyse such a difference, we focused on the planet ingestion at $t_0 = \bar{t}_0$, i.e. the age needed to produce the requested $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]^{\#52}$. Top panel of Fig. 5 shows the surface $[\text{Fe}/\text{H}]$ for models that fully account for the accretion process (ACC models). We adopted exactly the same values of the accretion age t_0 and of the mass of the ingested planet M_p used in the simplified models

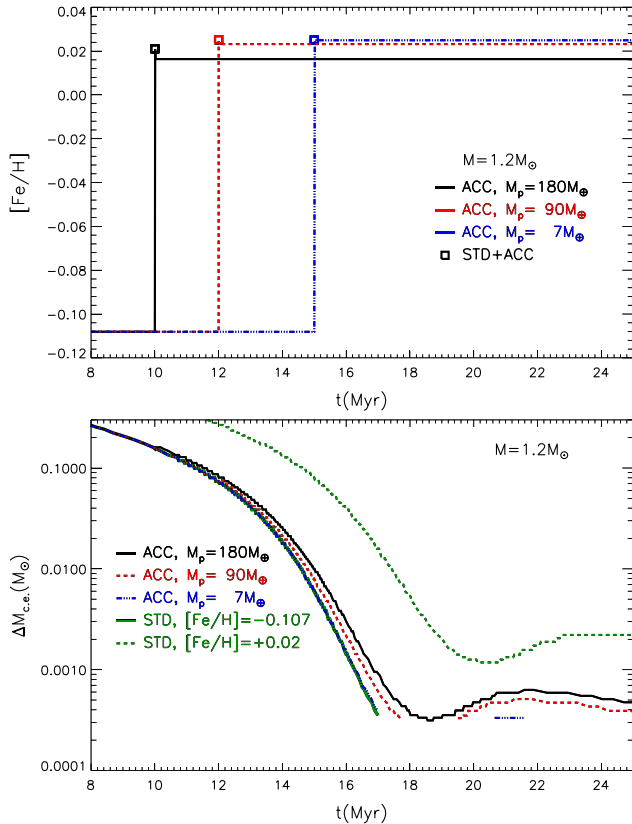


Figure 5. Top panel: surface $[\text{Fe}/\text{H}]$ value as a function of the stellar age for accreting models for the three values of the ingested planet mass ($M_p = 7, 90$ and $180 M_\oplus$) with the solar-like AS09 metal distributions and three t_0 values, namely $t_0 = 10$ ($180 M_\oplus$), 12 ($90 M_\oplus$) and 15 Myr ($7 M_\oplus$). The empty squares correspond to the $[\text{Fe}/\text{H}]$ obtained from the simplified accretion models discussed in Section 3.1 for the same M_p and t_0 . Bottom panel: temporal evolution of the mass inside the convective envelope ($\Delta M_{\text{c.e.}}$) for the same models shown in the top panel. Standard non-accreting models with $[\text{Fe}/\text{H}] = -0.107$ and $[\text{Fe}/\text{H}] = +0.02$ are shown too (green lines).

for the solar heavy element mixture (AS09), namely $M_p/M_\oplus = 180$ (10 Myr), 90 (12 Myr) and 7 (15 Myr). For comparison, in the figure we overplotted the $[\text{Fe}/\text{H}]$ values obtained by the simplified accretion model at the same age t_0 and for the same M_p .

The surface iron abundance evolution (top panel) is the same as the simplified models for $t < t_0$, since before the planet ingestion the star evolves as a standard pre-MS model without accretion, and consequently $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]_{\text{low}}$. On the other hand, for $t = t_0$, when the planet ingestion occurs, $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]_{\text{high}}$. For $t > t_0$ the accreting models show a quick – even if modest – decrease of the surface $[\text{Fe}/\text{H}]$, which is more pronounced for large M_p . Such a behaviour is a peculiarity of the models that actually follow the accretion process. It is the result of the quick increase of the opacity in the external convective region – caused by the accretion of metal-rich material – which makes the bottom of the convective envelope to sink inwards, thus reaching regions with the pristine chemical composition. Consequently, the accreted metal-rich material is further diluted leading to the observed modest decrease in the surface $[\text{Fe}/\text{H}]$, with differences that grow by increasing the ingested planet mass. However, the maximum extent of such differences is small, being less than 0.01 dex, and consequently negligible if compared to the uncertainty on abundance determinations. To be noted that, after the accretion and after the quick drop of $[\text{Fe}/\text{H}]$, the surface

abundances remain constant because the convective envelope never extends deep enough to reach regions not interested by the accretion and no further dilution occurs.

Bottom panel of Fig. 5 shows the temporal evolution of the mass contained inside the convective envelope for the same accreting (ACC) models shown in the top panel. For comparison, we also plotted the STDmodel with the low and high initial $[\text{Fe}/\text{H}]$, i.e. $[\text{Fe}/\text{H}]_{\text{AS09}}^{\text{cl.}} = -0.107$ and $[\text{Fe}/\text{H}]_{\text{AS09}}^{\#52} = +0.02$. As well known, the more metallic is the structure the thicker is the external convective envelope at the same evolutionary stage.

The differences between the accreting and standard sets of models get larger and larger by increasing the mass of the ingested planet. The model that actually follows the accretion process with the lowest value of M_p (i.e. $M_p = 7 M_\oplus$) shows an extension of the convective envelope almost indistinguishable from that of the low- $[\text{Fe}/\text{H}]$ standard one. On the other hand, by increasing M_p the convective envelope gets – after the planet ingestion – progressively thicker and thicker with respect to the standard low- $[\text{Fe}/\text{H}]$ model. Just after the accretion, the mass extension of the convective envelope can change of about 10 per cent if a $180 M_\oplus$ planet is accreted and of about 6–4 per cent for a 90 and $7 M_\oplus$ planet. The differences between the extension of the convective envelope in standard and accretion models increase at larger ages.

The different evolution of the convective envelope in presence of accretion can be explained by considering two aspects. First, the accretion of the metal-rich material with the AS09 mixture produces a relevant increase of the iron content (i.e. the $[\text{Fe}/\text{H}]$ value) but also of the total metallicity Z^{new} in the envelope (see e.g. equation 4) to about $Z^{\text{new}} \approx 0.0135$ – 0.0138 (i.e. increased by about 30–35 per cent). These values have to be compared with those of both the low- $[\text{Fe}/\text{H}]$ ($Z^{\text{mi}} = 0.0102$) and the high- $[\text{Fe}/\text{H}]$ (i.e. $Z^{\text{mi}} = 0.0135$) models. It is evident that the resulting surface Z^{new} of the AS09 models is essentially the same of the high- $[\text{Fe}/\text{H}]$ metallicity standard ones. Secondly, if the accretion begins earlier (smaller t_0 and larger M_p) the star has a thicker convective envelope and the modification of the chemical composition due to the accretion of metal-rich material occurs on a larger fraction of the star. Consequently, as t_0 decreases, the accreting model gets progressively more similar to the standard one with the high- $[\text{Fe}/\text{H}]$ value in the whole structure. On the contrary, if the accretion begins later (larger t_0 and smaller M_p) when the convective envelope is thinner, a larger part of the star has a chemical composition equal to that of the STD models with low- $[\text{Fe}/\text{H}]$, while the enhanced metals abundance is confined to the outer region. As such, the accreting model is expected to be much closer to the standard low- $[\text{Fe}/\text{H}]$ one.

We want to emphasize that the final metallicity Z^{new} in the convective envelope – after the planet ingestion – does not depend neither on t_0 nor on M_p , once the chemical composition of the planet has been fixed, as a consequence of the constraint $[\text{Fe}/\text{H}]^{\text{new}} = [\text{Fe}/\text{H}]^{\#52}$ imposed to compute M_p . This can be easily seen using equation (4). Noticing that $M_p/\Delta M_{\text{c.e.}} \approx 10^{-3}$ – 10^{-4} at t_0 , one obtains

$$Z^{\text{new}} \approx Z + Z^{\text{p}} \frac{M_p}{\Delta M_{\text{c.e.}}} \quad (7)$$

As discussed in Section 3.1, having fixed X_{Fe}^{p} the ratio $M_p/\Delta M_{\text{c.e.}}$ is fixed and Z^{new} is independent of M_p and t_0 .

Notice that, close to the zero-age main sequence (ZAMS) – i.e. for $t \gtrsim 20$ Myr – the convective envelope of accreting models with $M_p \gtrsim 90 M_\oplus$ shows an oscillation similar to that of STD models with the high- $[\text{Fe}/\text{H}]$, which leads to a slight increases of $\Delta M_{\text{c.e.}}$. However, this temporarily oscillation does not affect the surface chemical composition, as the maximum depth reached by the

surface convection during the oscillation is much smaller than that reached by the surface convection at the moment of the accretion. Consequently, the convective mixing is occurring in a region of homogeneous chemical composition, already mixed during the previous evolution after the accretion.

In order to study the impact of the chemical composition of the ingested planet on the final stellar surface elements abundance, we performed the same analysis discussed above but using the Earth-like mixture (JK10) for the accreted material. In this case, the mass abundance of iron X_{Fe}^{p} is about 3.4 times larger than that in the solar-like one. However, we recall that for a given accretion age t_0 , the total mass of the ingested planet is fixed by the constraint that the final $[\text{Fe}/\text{H}]$ must match the observed $[\text{Fe}/\text{H}]_{\text{AS09}}^{\#52}$. This, as shown in Section 3.1, results in an ingested planet mass M_{p} smaller than that obtained for the solar-like mixture.

The surface $[\text{Fe}/\text{H}]$ evolution in the case of solar-like or Earth-like heavy element mixture is similar, as the total mass of accreted iron is forced to be the same. On the other hand, this is not true for the final metallicity Z^{new} in the convective envelope. The smaller planet mass M_{p} required in the case of the Earth-like mixture with respect to that of the solar-like one at the same age t_0 – i.e. at the same $\Delta M_{\text{c.e.}}$ – causes a smaller increase of the surface metallicity Z^{new} . This can be easily understood by looking at equation (7), as the metallicity variation is proportional to the mass of the ingested planet M_{p} . The use of the Earth-like mixture (JK10) in the accreted matter leads to models with a maximum total metallicity in the envelope of about $Z^{\text{new}} = 0.0112$ (i.e. increased by about 10 per cent), a value which is very close to that used for the computation of the standard low- $[\text{Fe}/\text{H}]$ models, namely $Z^{\text{ini}} = 0.0102$, and much lower than that of the high- $[\text{Fe}/\text{H}]$ ones ($Z^{\text{ini}} = 0.0135$). Thus, even if the iron content in the envelope is significantly increased ($[\text{Fe}/\text{H}] \approx +0.02$), the total metallicity Z^{new} is only marginally affected by the accretion. As a consequence, such models show an evolution of $\Delta M_{\text{c.e.}}$ very similar to that of the standard low- $[\text{Fe}/\text{H}]$ ones, with a maximum variation of $\Delta M_{\text{c.e.}}$ of about 4 per cent when a $53 M_{\oplus}$ planet is ingested.

From this discussion, it emerges a first important result. The adoption of an iron-poor or iron-rich mixture for the accreted matter has the effect of producing two limiting sets of models: one with an high-metallicity Z^{new} similar to that of the high- $[\text{Fe}/\text{H}]$ STD models (iron-poor AS09 mixture), and the other with a low metallicity more similar to that of the low- $[\text{Fe}/\text{H}]$ ones (iron-rich JK10 mixture, rocky planet).

5 SURFACE HEAVY ELEMENT ABUNDANCES

Another point to discuss is the predicted surface elements abundances after the accretion episode. To this regard, Spina et al. (2015) measured the abundances of several elements (Na, Mg, Al, Si, Ca, Sc, Ti, V, Cr, Mn, Fe, Co, Ni Cu) in both the peculiar star #52 and in another cluster star, namely #45, representative of the mean cluster composition. They provided the differences of the surface abundances between these two stars, i.e.

$$\Delta A_i \equiv \log(N_i/N_{\text{H}})_{\#52} - \log(N_i/N_{\text{H}})_{\#45}. \quad (8)$$

The variation of the surface elements abundance depends on the characteristics of the accretion episode, in particular on the chemical composition of the accreted matter. Thus, it is worth to compare the predicted ΔA_i obtained in our computations with those measured by Spina et al. (2015).

Fig. 6 shows the comparison between the predicted and observed ΔA_i for a subsample of elements available both in our models and

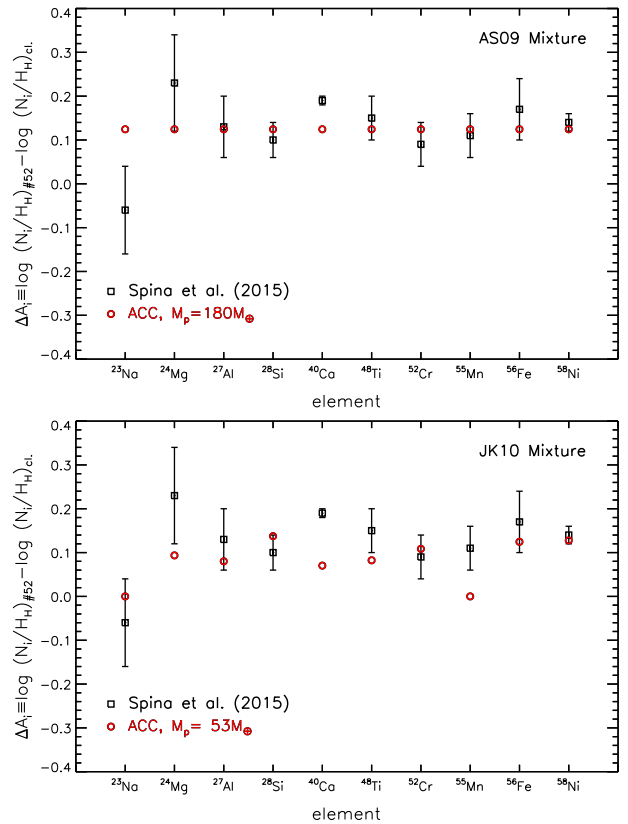


Figure 6. Observed (black squares) and predicted (red circles) surface abundance differences ΔA_i between the peculiar star #52 and the mean cluster values for the labelled elements. Top panel: predictions of full accretion models obtained using the solar-like AS09 mixture in the accreted matter. Bottom panel: the same as top panel but for models with the Earth-like JK10 mixture in the accreted matter.

in Spina et al. (2015). The upper panel shows the case for the solar-like mixture and the bottom panel the Earth-like one. Notice that, the final surface abundances are independent of M_{p} if the ingested planet mass is tuned to obtain the same $[\text{Fe}/\text{H}]$ after the accretion episode.

In the case of the solar-like mixture, the results of the accretion models agrees quite well with the values measured by Spina et al. (2014), within the observational uncertainties, with the exception of Na (overestimated in our models) and Ca (underestimated in our models). Nevertheless, the adoption of a solar-like mixture seems to be a good approximation, at least within the current uncertainties, of the metals distribution in the accreted matter. Since the heavy element mixture used in the star and in the accreted matter is the same, the accretion produces an abundance enhancement of all the elements by the same factor.

The situation is different if the Earth-like mixture is used for the planet. In this case, the enhancement factor is different for each element. If the Earth-like mixture is adopted, the agreement with the observed and predicted ΔA_i pattern gets slightly worse, in particular for Mg, Ti and Mn. For all these elements we underestimated the abundance, although in almost all the cases we are still compatible within 2σ .

We performed the same analysis using the simplified accretion scheme that, as expected, produces abundance very close (with differences lower than 0.01 dex) to the full accretion one.

These comparisons show that the accretion models are compatible with the observed ΔA_i pattern using both the solar-like and

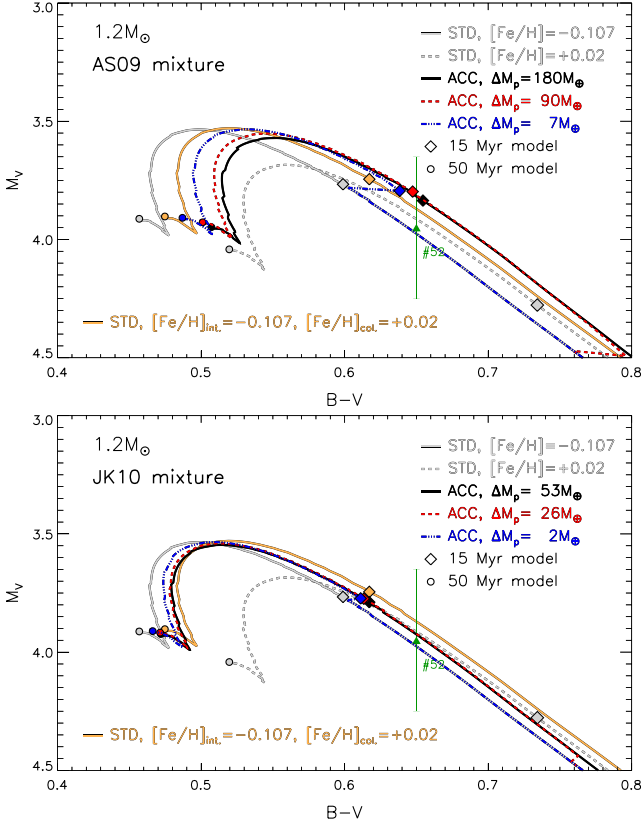


Figure 7. CMD with the standard low-[Fe/H] (STD, $[\text{Fe}/\text{H}] = -0.107$, grey solid line), standard high-[Fe/H] (STD, $[\text{Fe}/\text{H}] = +0.02$, grey dashed line), and accreting evolutionary tracks (ACC, coloured lines). The ACC tracks are computed for the three labelled M_p . The standard evolutionary track computed for $[\text{Fe}/\text{H}] = -0.107$ and converted into the CMD using a surface $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]^{\#52} = +0.02$ is also shown. The models corresponding to an age of 15 Myr (filled diamonds) and 50 Myr (filled circles) are shown too, together with the position of #52. Top panel: models computed assuming the AS09 solar-like heavy elements distribution in the accreted matter. Bottom panel: the same as in top panel, but for the (JK10) Earth-like metals distribution.

Earth-like mixture in the accreted matter. More accurate surface abundances are needed to better constrain the chemical composition of the ingested planet. We remark that our aim is not to reproduce exactly the observed abundances but rather to investigate the effect of adopting different values of the not well constrained parameters, such as the planet mass and its chemical composition, that significantly affect the stellar models after the planet ingestion.

6 EFFECT ON THE CMD

We showed that the ingestion of a planet affects not only the surface chemical abundance of a star but also the structure evolution. Thus, the planet engulfment is expected to produce effects also on the track morphology/position in the CMD, mainly because of (1) the variation of the luminosity and effective temperature caused by the accretion process and (2) the metallicity change in the atmosphere. The first effect can be obtained only by means of the full accretion model, while the second can be evaluated using the simplified approach.

Fig. 7 shows the evolutionary tracks of $M = 1.2 M_{\odot}$ in the $(B - V, M_V)$ plane. The STD models with the two extreme $[\text{Fe}/\text{H}]$ values, namely $[\text{Fe}/\text{H}]_{\text{AS09}}^{\text{cl}} = -0.107$ and $[\text{Fe}/\text{H}]_{\text{AS09}}^{\#52} = +0.02$, and

Table 3. Main characteristics of the 15 and 50 Myr standard and accreting models shown in Fig. 7.

Type	M_p (M_{\oplus})	Age = 15 Myr			Mixture
		$B - V$	M_V	$[\text{Fe}/\text{H}]$	
STD	0	0.5989	3.77	-0.107	–
STD	0	0.7343	4.28	+0.020	–
ACC ^a	7	0.6384	3.79	+0.025	AS09
ACC ^a	90	0.6474	3.80	+0.023	AS09
ACC ^a	180	0.6546	3.84	+0.016	AS09
ACC ^b	2	0.6112	3.77	+0.025	JK10
ACC ^b	26	0.6134	3.77	+0.024	JK10
ACC ^b	53	0.6172	3.79	+0.017	JK10
STD+ACC ^c	0	0.6172	3.74	+0.020	–
Type	M_p (M_{\oplus})	Age = 50 Myr			Mixture
		$B - V$	M_V	$[\text{Fe}/\text{H}]$	
STD	0	0.4569	3.91	-0.107	–
STD	0	0.5196	4.04	+0.020	–
ACC ^a	7	0.4870	3.91	+0.025	AS09
ACC ^a	90	0.5011	3.93	+0.023	AS09
ACC ^a	180	0.5072	3.95	+0.016	AS09
ACC ^b	2	0.4663	3.91	+0.025	JK10
ACC ^b	26	0.4714	3.92	+0.024	JK10
ACC ^b	53	0.4720	3.92	+0.017	JK10
STD+ACC ^c	0	0.4747	3.90	+0.020	–

Notes. ^aAccretion of matter with the AS09 mixture.

^bAccretion of matter with the JK10 mixture.

^cStandard low-[Fe/H] track with high-[Fe/H] colours.

the accreting models computed adopting the three quoted planet masses M_p for the solar-like (AS09, top panel) and the Earth-like mixtures (JK10, bottom panel) in the accreted matter are shown. We overplotted a standard track computed with the mean cluster $[\text{Fe}/\text{H}]$ (in the interior), but converted into the colour–magnitude plane using a the #52 surface $[\text{Fe}/\text{H}] = +0.02$. This model corresponds to take into account only the effect of varying the chemical composition in the stellar atmosphere (i.e. simplified accretion model). For all the evolutionary sequences, we also marked the position in the CMD of the models at the age $t = 15$ Myr (approximately the age of the Gamma Velorum cluster) and $t = 50$ Myr (on the MS). The main characteristics of the 15 and 50 Myr models are listed in Table 3. In figure, we also overplotted the observational data for #52 corrected for the reddening and distance modulus given in Spina et al. (2014). Notice that at the age of the cluster (15 Myr), the location of the STD model computed adopting the initial low-[Fe/H] = -0.107 is about 0.05 mag bluer (in colour) and 0.1–0.2 mag brighter than the data. However, if an age of 14 Myr is adopted, the low-[Fe/H] model matches the observed position of #52 quite well.²

The standard track with the initial high-[Fe/H] is the coolest and fainter while that with the initial low-[Fe/H] is the hottest and brighter. The non-standard ones computed taking into account the accretion episode are located in between. The inclusion of the accretion affects the position of the track in the CMD, depending on the evolutionary phase, mass M_p and the chemical composition of the ingested planet. As already stated, the main effect of the accretion is to increase the $[\text{Fe}/\text{H}]$ and the metallicity inside the convective envelope leaving unchanged the metallicity in the stellar core. Such

² If the $1.2 M_{\odot}$ model with the high-[Fe/H] = +0.02 is adopted, the best age is slightly larger, about 16.5 Myr, but still compatible with the cluster age.

an increase of the metal content causes a shift of the track towards lower effective temperatures altering only marginally the total luminosity and the temporal evolution, which are more sensitive to the core metallicity. In addition, the accreting models get redder and redder as M_p increases (see Table 3), as a consequence of the progressively larger Z in a larger fraction of the star. However, such a metallicity variation produces an effect that might be not clearly visible in all the evolutionary phases. As an example, the three accreting models are almost coincident during the Henyey phase of the pre-MS evolution.³ During this phase, the shift induced by the accretion is almost parallel to the evolutionary track. On the other hand, the separation gets more and more visible as the star approaches the ZAMS. This fact clearly shows that the effect of a planet ingestion on the structure of the star is not limited to the period just after the accretion itself, but it is still present much later, i.e. near the MS. In other words, the planet ingestion leaves footprints that can be observed even long after the accretion. We only mention that, for ages larger than about 50–100 Myr (i.e. on the MS), the metals overabundance in the convective envelope can be erased by non-standard turbulent mixing (thermohaline mixing, see e.g. Vauclair 2004) and the surface chemical anomalies might significantly reduce (see e.g. Garaud 2011; Théado & Vauclair 2012).

The largest differences between the standard low-[Fe/H] and the accreting models occur when it is ingested a planet of $180 M_\oplus$ with the solar-like heavy elements mixture (AS09, top panel), because of the relatively large increase of the surface metallicity Z (about 30 per cent) with respect to the initial one. Referring to the 15 Myr model location in the CMD, we obtained a significant reduction of the effective temperature of the accreting model of about 120 K, which corresponds to a track redder of about 0.05 mag than the standard low-[Fe/H] one. Similar variations are obtained for the 50 Myr model (see Table 3). Notice that at the age of 15 Myr all the three accretion models match quite well the observed position of #52 in the CMD.

In the case of an Earth-like planet ingestion (JK10, bottom panel), the maximum variation of the surface metallicity Z is much smaller (about 10 per cent) and the accreting tracks are very close to the low-[Fe/H] standard ones, even when the higher value of the ingested planet mass is considered (i.e. $53 M_\oplus$). We obtained an accreting track cooler than about 40 K and redder of about 0.01–0.02 mag than the low-[Fe/H] standard one for both the age of 15 and 50 Myr (see Table 3). In this case, the 15 Myr accretion models are slightly hotter and brighter than #52 in the CMD. However, such models match the data if an age of 14 Myr is adopted.

We also analysed the effect on the CMD position of a standard track with the initial [Fe/H] of the cluster, converted into magnitude and colours using a surface $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]^{\#52} = +0.02$. This case corresponds to the simplified accretion scheme, where we assumed that the accretion modifies only the surface chemical composition of the star in a very thin layer so that the structure (mainly T_{eff} and luminosity) is unaltered. The adoption of a higher [Fe/H] in the atmospheric models leads to an almost rigid translation of the track in the CMD, with a shift of +0.02 mag in colour and less than -0.01 mag in magnitude, without changing the temporal evolution (because no structural change occurs). Such a variation has to be compared with that achieved in the case of full accretion models, where the variation of T_{eff} and luminosity is consistently ac-

counted for. Referring to top panel of Fig. 7 (solar-like mixture), the simplified accretion track is systematically bluer (from 0.01 to 0.04 mag depending on M_p) and can reach a maximum difference in magnitude of about 0.1 mag with respect to the full accretion one. On the other hand, the simplified accretion model is much closer to those obtained using the Earth-like mixture (bottom panel). In this case, full and simplified accretion tracks differs in the CMD by less than 0.01 mag in colour and 0.05 mag in magnitude.

In summary, although the differences between simplified and full accretion models are present also in the CMD, they are quite small when compared to the current observational uncertainties.

7 IMPACT ON THE INFERRED STELLAR PROPERTIES

Since important stellar quantities such as mass and age are often inferred by comparing theoretical models and observations, the shift in the CMD location of the evolutionary tracks that takes into account the accretion process with respect to the standard ones directly translates into differences in the inferred stellar quantities. In other words, the values of the stellar mass and age (or the mass value of the ingested planet) obtained by means of STD models might be quite different from those based on models which explicitly take into account the accretion process.

Given such a situation, it is worth to estimate the maximum error in the stellar mass and the age estimated by adopting standard tracks to recover an artificial star generated using accreting ones. We performed this test because usually specific accreting models are not available and the main properties of chemically peculiar stars are derived by means of non-accreting stellar evolutionary grids.

First, we sampled synthetic stars with the age of 15 Myr (about the age of Gamma Velorum cluster) and 50 Myr (about the beginning of the MS) from the accreting evolutionary tracks that show the largest deviation from the standard one. We choose the track of $1.2 M_\odot$ which follows the ingestion of an $M_p = 180 M_\oplus$ planet at an age $t_0 = 10$ Myr with the solar-like heavy element mixture. We also used the $1.2 M_\odot$ accreting track that ingested an Earth-like planet of $53 M_\oplus$ at $t_0 = 10$ Myr. We performed the analysis for both the mixtures because of the significant impact of the chemical composition of the ingested planet in the location of the models in the CMD, as shown in Section 6.

As a second step, we used the standard grid of models with both the low- and high-[Fe/H] to recover the data. To get a good mass resolution, the standard grid has been interpolated at a mass step of $0.001 M_\odot$, and each evolutionary track at a time step of 10^4 yr. The recovery has been performed using a maximum Likelihood technique. We adopted a formalism similar to that described in Gennaro, Prada Moroni & Tognelli (2012) to compute the Likelihood (defined in their equation 3), the best-fitting value (the *mode*) and the confidence interval obtained by rejecting the 16 per cent of the total area under the distribution function from the left and the right tail.

Being interested only to quantify the systematic errors in the inferred age and mass of a star that ingested a planet by using available standard non-accreting models in the recovery procedure, we adopted a very small uncertainty in the synthetic data in the ($B - V$, M_V) plane, namely $\sigma_V = \sigma_B = 0.0005$.

Fig. 8 shows the synthetic star in the CMD at an age of 15 and 50 Myr (filled red circle and blue triangle, respectively), extracted from the model of $1.2 M_\odot$ which follows the accretion of a planet of $M_p = 180 M_\oplus$ and a solar metal distribution (AS09 mixture). A partial grid of standard tracks used for the recovery with $[\text{Fe}/\text{H}]_{\text{AS09}}$

³ The Henyey track corresponds to that part of the pre-MS evolution from the formation of a sizeable radiative core to the maximum in luminosity before the ZAMS, when the star moves towards higher effective temperatures.

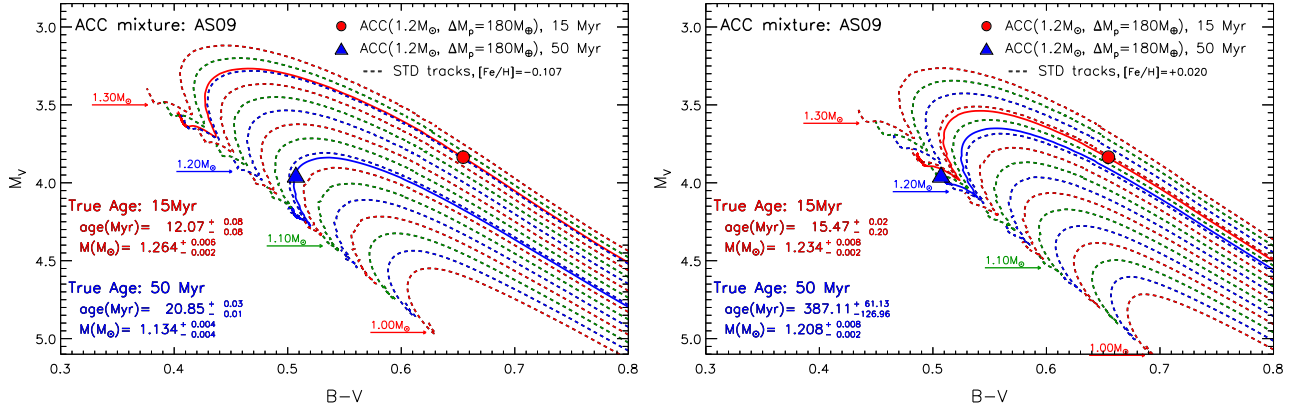


Figure 8. CMD with the standard evolutionary tracks used for the recovery (dashed lines). The 15 (filled red circle) and 50 Myr models (filled blue triangle) obtained from the $1.2 M_\odot$ accreting model with the AS09 solar-like mixture and $M_p = 180 M_\oplus$ are shown. The best-fitting tracks for the 15 (solid red line) and 50 Myr model (solid blue line) are shown too. Left-hand panel: STD models with $[\text{Fe}/\text{H}] = -0.107$. Right-hand panel: STD models with $[\text{Fe}/\text{H}] = +0.020$.

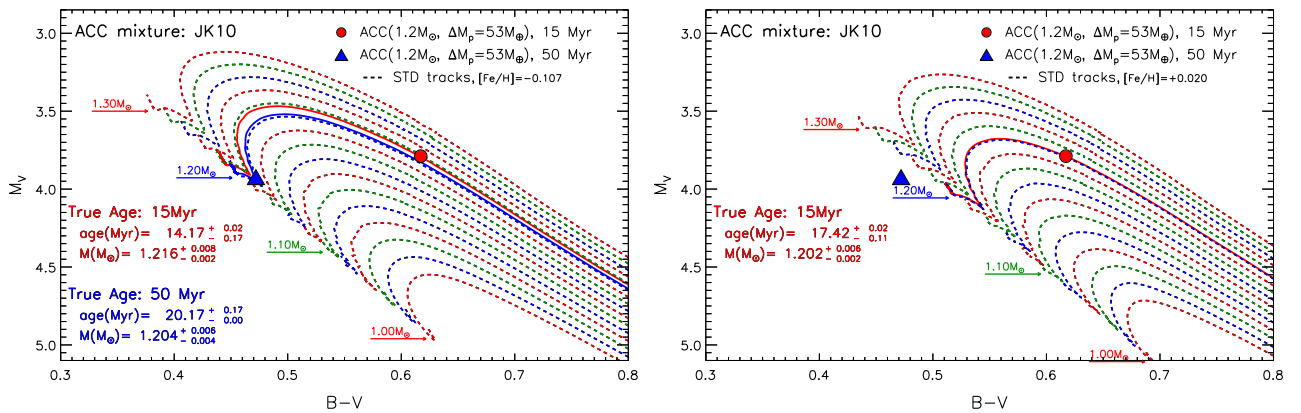


Figure 9. The same as in Fig. 8 but for models with the JK10 Earth-like mixture in the accreted matter and $M_p = 53 M_\oplus$.

$= -0.107$ (left-hand panel) and $[\text{Fe}/\text{H}]_{\text{AS09}} = +0.020$ (right-hand panel) is also shown.

The inferred age and mass of the best-fitting model depends on the $[\text{Fe}/\text{H}]$ value of the grid. Using the standard grid with $[\text{Fe}/\text{H}]_{\text{AS09}} = -0.107$ (left-hand panel), the recovery procedure yields a best estimate of the mass of $1.26 M_\odot$ and age of 12 Myr, while the synthetic star has a true mass of $1.2 M_\odot$ and an age of 15 Myr. Thus, the inferred mass is overestimated by about 5 per cent and the age is underestimated by about 20 per cent. Notice that both the mass and age estimates are not compatible – within their confidence interval – with the true ones. The discrepancies between the true and the recovered mass and age increases for the synthetic star at a true age of 50 Myr. In this case, the inferred mass and age are underestimated, by about 6 and 58 per cent, respectively, with a best-fitting mass of $1.13 M_\odot$ and an age of about 21 Myr.

If the $[\text{Fe}/\text{H}]_{\text{AS09}} = +0.020$ standard grid is used in the recovery procedure (right-hand panel), the differences between the true and the estimated values slightly reduce in the case of the artificial star of 15 Myr. The best-fitting mass is about 3 per cent larger ($1.23 M_\odot$) than the true one, and the best-fitting age overestimated by about 3 per cent. The situation is different in the case of the simulated star at a true age of 50 Myr. Although the inferred stellar mass is overestimated by less than 1 per cent ($M = 1.21 M_\odot$) the best-fitting age is badly recovered and drastically overestimated ($t = 388$ Myr). Such an occurrence can be easily understood by remembering that metal richer tracks are cooler and fainter than metal-poorer ones. Hence, the CMD location of the

simulated star with a true age of 50 Myr is confused with metal-rich models in a much more advanced phase on the MS. As well known, this phase is much slower than the pre-MS one and a large variation of the age only marginally affects the luminosity and colour of the star. As a consequence, the age estimate becomes less precise, i.e. the marginalized age distribution gets progressively broader and broader moving towards the MS, thus causing a broadening of the confidence interval too. Moreover, for the same reason, during the MS phase the models with large ages are denser along the evolutionary track. Thus, their contribution in defining the age distribution is the strongest and this leads to prefer a large best-fitting age (see also the discussion in Gennaro et al. 2012).

We repeated the same analysis for the other two artificial stars of $1.2 M_\odot$ and true age of 15 and 50 Myr, but extracted from the models which follows the ingestion of an Earth-like planet of $53 M_\oplus$, as shown in Fig. 9.

By adopting the standard grid with $[\text{Fe}/\text{H}]_{\text{AS09}} = -0.107$ (left-hand panel), the recovery yields – for the model with the true age of 15 Myr – a best estimate mass of $1.22 M_\odot$ (overestimated by about 1 per cent) and age of 14 Myr (underestimated by about 6 per cent). For the synthetic star of a true age of 50 Myr, the estimated mass is well recovered (overestimated by less than 1 per cent), while the age estimate is much worse, yielding about 20 Myr (underestimated by about 60 per cent). If the high- $[\text{Fe}/\text{H}]$ grid is used to infer the best mass and age (right-hand panel), then the artificial star with a true age of 15 Myr is still recovered quite well, especially the mass which is overestimated by less than 1 per cent, and with an age of 17 Myr

(overestimated by 16 per cent). The situation is different if the high-[Fe/H] grid is used to recover the synthetic star of 50 Myr. From the figure, it is clearly visible that the simulated data is much bluer than the high-[Fe/H] STD models and, consequently, the simulated star at 50 Myr is not recovered at all.

The analysis we performed clearly shows that the systematic bias in the mass and age estimates induced by using STD models which do not take into account the accretion strongly depends on the chemical composition of the ingested planet. Unfortunately, generally no indication about this quantity is available, as observation provides only the actual cluster low-[Fe/H] (assumed to be equal to the initial one) and the high-[Fe/H] (after the accretion) of the chemically peculiar star.

Nevertheless, the presented simulations also show that it is possible to obtain two limiting cases corresponding to accrete matter with two different heavy elements mixtures, namely the solar-like (AS09, low-iron content) and the Earth-like (JK10, high-iron content). The results described above show that in these two limiting cases, the standard tracks with the high- and the low-[Fe/H] grid of STD models provide a best-fitting mass not very different from the true one for both the 15 and 50 Myr synthetic stars. On the other hand, the age estimates are worst in particular for stars near the ZAMS.

Given such a situation, since no a priori information about the chemical composition and mass of the ingested planet is available, the best choice is to use, simultaneously, both the low- and high-[Fe/H] standard tracks to constrain the most plausible range of the mass and age of the peculiar star.

8 CONCLUSIONS

We analysed the effect of a single episode of planet ingestion on the evolution of a pre-MS star, to explain the peculiar surface chemical abundance observed in 2MASS J08095427–4721419 (#52) belonging to the Gamma Velorum cluster. Contrarily to previous investigations, we computed pre-MS models that, for the first time, consistently take into account the accretion effects, i.e. the change of both the stellar structure and the chemical composition. The results of our computations have been compared with those achieved by adopting a simplified accretion method that considers only the effect of the accretion on the surface chemical abundances without any modification of the stellar structure.

The impact of a planet ingestion on the evolution of a star depends on both the characteristics of the star and of the planet. Concerning the star, we analysed the evolution of a model with $M = 1.2 M_{\odot}$ with an initial [Fe/H] equal to that of the cluster (i.e. $[\text{Fe}/\text{H}]_{\text{AS09}}^{\text{cl}} = -0.107$). This particular value of the stellar mass has been obtained to reproduce the #52 position in the CMD at an age of about 15 Myr (i.e. the mid-age value of the Gamma Velorum cluster). Since the surface iron-abundance enhancement caused by the planet ingestion strongly depends on the convective envelope extension – which in turn depends on the age – we focused on three values of the age t_0 at which the accretion event is supposed to occur, namely $t_0 = 10, 12$ and 15 Myr (about the Gamma Velorum cluster age).

We tuned the ingested planet mass to reproduce the observed $[\text{Fe}/\text{H}]^{\#52}$ value (i.e. $[\text{Fe}/\text{H}]_{\text{AS09}}^{\#52} = +0.02$) of the stellar metallicity after the accretion process. For the planet chemical composition, we analysed the adoption of two different heavy elements distributions, namely a solar-like (AS09, low-iron content) and an Earth-like one (JK10, high-iron content).

We showed that the earlier is the accretion episode (i.e. the smaller is t_0), the more extended is the convective envelope, and thus the

more diluted is the ingested metal-rich material with the pristine stellar one. Consequently, the mass of the accreted planet required to reproduce the observed $[\text{Fe}/\text{H}]^{\#52}$ value increases as t_0 decreases. We also showed that, at a fixed age t_0 , the mass of the ingested planet necessary to account for the observed chemical peculiarities decreases by increasing the iron content in the planet. Indeed, we showed that the needed mass of a planet with the Earth-like chemical composition is smaller than that of a planet with a solar-like one. For a solar-like mixture, we derived a planet mass M_p of 180, 90 and 7 M_{\oplus} for an accretion age t_0 of, respectively, 10, 12 and 15 Myr. The values of M_p reduces to 53, 26 and 2 M_{\oplus} if an Earth-like mixture is adopted.

The ingestion of metal-rich material affects the stellar structure – after the accretion episode – and in particular the extension of the convective envelope with respect to that of standard pre-MS track without accretion. We showed that the mass inside the convective envelope just after the accretion can vary up to 10 per cent when the solar-like mixture and the largest value of the ingested planet (i.e. $M_p = 180M_{\oplus}$) are used. Such differences reduces to 4–6 per cent by adopting lower M_p values. If the Earth-like mixture is used in the accreted matter then the maximum variation reaches about 4 per cent.

The change in the extension of the convective envelope has an impact also on the surface [Fe/H] value after the planet ingestion. Full accretion models predict a surface [Fe/H] value slightly lower than that obtained in the case of a more simplified accretion, differences that increase by increasing the ingested planet mass. However, the maximum extent of such a difference is always lower than about 0.01 dex, thus negligible if compared to the common observational uncertainty on abundance determination.

We quantified the impact of the accretion on the surface chemical composition. First, we analysed the total metallicity Z^{new} after the planet ingestion. We identified two limiting situation. In the first case, which corresponds to accrete matter with a low-iron content (i.e. solar-like mixture for the planet), the surface metallicity Z^{new} is significantly increased and more similar to that attained by STD models with the initial peculiar star $[\text{Fe}/\text{H}]^{\#52}$ (i.e. a maximum metallicity Z increase of about 30 per cent). In the second case, which corresponds to accrete a planet with an high-iron content (Earth-like mixture), the surface metallicity is only marginally enhanced and more similar to that attained by standard non-accreting models with the initial cluster $[\text{Fe}/\text{H}]^{\text{cl}}$ (a maximum metallicity Z increased of about 10 per cent). We also analysed the effect of the accretion on the surface abundances of some elements which have been measured by Spina et al. (2015) in the peculiar star #52. We showed that both the enrichment patterns we obtained using the solar-like and the Earth-like mixture for the accreted planet are in agreement with that observed by Spina et al. (2015). To better constrain the most suitable mixture for the accreted matter, more precise measurements are needed.

We analysed the impact of the planet ingestion on the tracks in the CMD. Depending on the characteristics of the ingested planet, the accretion leads to slightly cooler and fainter models caused by the increase of the metallicity (i.e. radiative opacity) in the external layers. The most visible effects in the CMD occurs when a planet of $M_p = 180 M_{\oplus}$ and the solar-like mixture is ingested by the star, due to large metallicity enhancement in the external envelope. In this case, variations of about 0.06 mag in colour and about 0.07 mag in magnitude can be achieved. The differences get smaller by reducing the ingested planet mass or by adopting the Earth-like mixture in the accreted matter. The effects of the planet ingestion on the stellar structure and in the CMD are still

present long after the accretion, even at the beginning of the MS evolution.

As generally accreting models consistent with the observed peculiar stars are not available, we investigated the systematic bias in the inferred age and mass due to the use of standard non-accreting pre-MS tracks to recover the characteristics of a synthetic star generated using an accreting model. The synthetic star had been obtained fixing the mass to $1.2 M_{\odot}$ and selecting two ages, namely 15 Myr (about the estimated age of the Gamma Velorum cluster) and 50 Myr (about the beginning of the MS). We adopted the accreting model that attains the largest deviation from the standard one (at the same age and mass) for both the solar-like ($M_p = 180 M_{\oplus}$) and Earth-like planet ($M_p = 53 M_{\oplus}$) chemical composition. We performed the recovery using both the low- and high-[Fe/H] standard non-accreting models.

As a general result, while the stellar mass estimate is not severely biased by the adoption of non-accreting stellar models, with a maximum difference between the recovered and the true mass of about 6 per cent, the stellar age is badly recovered, especially for synthetic data near the ZAMS, with a maximum uncertainty of 60 per cent. The use of STD models computed for an initial [Fe/H] equal to that of the peculiar star (i.e. $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]^{\#52}$) provides a quite good estimate of the stellar mass when the ingested planet has a low-iron content (i.e. solar-like mixture). On the other hand, the accretion of an iron-rich planet (Earth-like mixture) is better reproduced by standard track with the pristine initial metallicity (i.e. $[\text{Fe}/\text{H}] = [\text{Fe}/\text{H}]^{\text{cl}}$).

Thus, standard tracks with both the low- and high-[Fe/H] values can be used to constrain the inferred properties of such chemically peculiar objects when the details of the accretion are not known.

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