

# Lighting up stars in chemical evolution models: the CMD of Sculptor

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Accepted 2016 May 11. Received 2016 May 11; in original form 2016 February 2

## ABSTRACT

We present a novel approach to draw the synthetic colour–magnitude diagram (CMD) of galaxies, which can provide – in principle – a deeper insight in the interpretation and understanding of current observations. In particular, we ‘light up’ the stars of chemical evolution models, according to their initial mass, metallicity and age, to eventually understand how the assumed underlying galaxy formation and evolution scenario affects the final configuration of the synthetic CMD. In this way, we obtain a new set of observational constraints for chemical evolution models beyond the usual photospheric chemical abundances. The strength of our method resides in the very fine grid of metallicities and ages of the assumed data base of stellar isochrones. In this work, we apply our photochemical model to reproduce the observed CMD of the Sculptor dSph and find that we can reproduce the main features of the observed CMD. The main discrepancies are found at fainter magnitudes in the main sequence turn-off and sub-giant branch, where the observed CMD extends towards bluer colours than the synthetic one; we suggest that this is a signature of metal-poor stellar populations in the data, which cannot be captured by our assumed one-zone chemical evolution model.

**Key words:** stars: abundances – Hertzsprung–Russell and colour–magnitude diagrams – galaxies: dwarf – Local Group – galaxies: stellar content.

## 1 INTRODUCTION

In this work, we present a novel approach to obtain a synthetic colour–magnitude diagram (CMD) of galaxies, starting from predictions of chemical evolution models. Our new *photochemical model* ‘lights up’ the stars of chemical evolution models, according to their initial mass, metallicity and age; in this way, we can obtain a new set of observational constraints for chemical evolution models beyond the usual photospheric chemical abundances. The method presented in this work can provide – in principle – a deeper insight in the interpretation of current observations, since we can understand how our hypothesis about galaxy formation and evolution can affect the final configuration of the CMD.

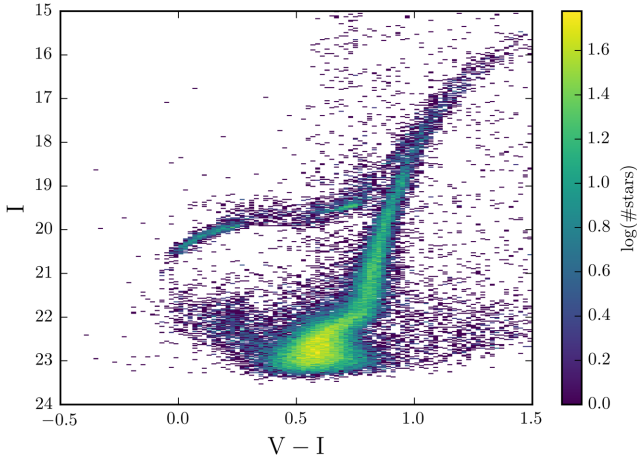
By solving a set of physically motivated differential equations, which take into account the main physical processes taking place and influencing the evolution of the galaxy interstellar medium (ISM), numerical codes of chemical evolution are able to provide the galaxy star formation history (SFH) and age–metallicity relation; the evolution of the galaxy stellar and gas mass, and the run of the

ISM chemical abundances with time. Building up a photochemical code consists then in coupling the output of chemical evolution models with a data base of stellar isochrones, currently available and computed with very high accuracy.

Most of the previous works in the literature recover the SFH of galaxies from the observed CMD by adopting sophisticated fitting techniques (e.g. Harris & Zaritsky 2001; Dolphin 2002; Aparicio & Gallart 2004; Tolstoy, Hill & Tosi 2009; Cignoni & Tosi 2010; Monelli et al. 2010; Hidalgo et al. 2011); in particular, they search for the suitable linear combination of simple stellar populations (SSPs) with different age and metallicity, which provides the best agreement with the observed photometric properties of the galaxy composite stellar population. As a byproduct, this ‘classical’ procedure can also predict an average galaxy age–metallicity relation. Nevertheless, no underlying approximate physical model is assumed in these works for the galaxy formation and evolution.

In this paper, the first of a series of future works, we focus on reproducing the CMD of the Sculptor dwarf spheroidal galaxy (dSph). In particular, we investigate whether the best chemical evolution model for Sculptor – reproducing the galaxy stellar metallicity distribution function (MDF) – is able to predict a synthetic CMD which agrees with the observed one.

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**Figure 1.** In this Figure, we show the observed CMD of the Sculptor dSph (de Boer et al. 2011). The data set is shown as 2D histogram, with the bin size in both the  $x$ - and  $y$ -dimensions being 0.02 dex; the colour coding in the figure corresponds to the number of stars within each grid element. We consider in our analysis only clean isolated stellar detections and the Sculptor member stars with an elliptical radius  $r_{\text{ell}} \leq 0.6$  deg.

This work is organized as follows: in Section 2 we summarize the main properties of the Sculptor dSph and describe the observed set of data used in this work for the comparison with our models; in Section 3 we present the main characteristics of our photochemical model and the methods we employ to fairly compare the synthetic with the observed CMD; in Section 4 we show our results, and in Section 5 we draw some conclusions.

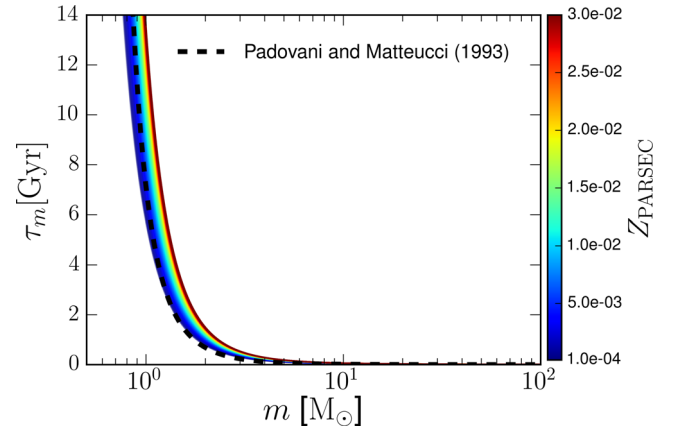
## 2 THE OBSERVED DATA SET

The Sculptor dwarf galaxy was discovered by Shapley (1938). Although it might appear simple at first glance, from the study of the kinematical, chemical and spatial distribution of its stellar populations, Tolstoy et al. (2004) were able to disentangle in this galaxy an inner, kinematically ‘cold’, metal-rich stellar population from an outer ‘hot’ metal-poor one, later on confirmed by Battaglia et al. (2008) and Walker & Peñarrubia (2011). Other studies based on photometric data sets also were able to identify (or confirm) the existence of stellar populations distinct in metallicity (Majewski et al. 1999), age and spatial distribution (de Boer et al. 2011, 2012).

McConnachie (2012) reported for Sculptor an average  $V$ -band surface brightness  $\mu_V = 23.5 \pm 0.5$  mag arcsec $^{-2}$ , an half-light radius  $r_h = 283 \pm 45$  pc, and an absolute  $V$ -band magnitude  $M_V = -11.1 \pm 0.5$  mag. We make use of the distance modulus  $\mu = 19.62 \pm 0.04$  mag derived by Martínez-Vázquez et al. (2015).

The observed CMD is taken from de Boer et al. (2011, see Fig. 1), which were able to resolve stars down to the oldest main sequence turn-off (MSTO) of the Sculptor dSph, by taking advantage of the deep wide-field photometry of CTIO/MOSAIC. In order to avoid a non-negligible contamination of foreground MW disc field stars, we consider only stars along the line of sight to the Sculptor dSph with elliptical radius  $r_{\text{ell}} \leq 0.6$  deg and corresponding to clean isolated detections; the percentage of stars with these characteristics in the de Boer et al. (2011) catalogue is about 92 per cent of the entire sample. We find that, for  $r_{\text{ell}} > 0.6$  deg, the noisy pattern introduced by foreground stars becomes larger than the ‘signal’ of the Sculptor CMD one wants to recover (see also fig. 5 in de Boer et al. 2011).

The observed stellar MDF is taken from Romano & Starkenburg (2013), which combined the Kirby et al. (2009, 2010) spectroscopic



**Figure 2.** In this figure, we show how the stellar lifetimes we have derived from the PARSEC stellar evolutionary tracks vary as functions of the stellar mass and metallicity. The dashed black curve corresponds to the stellar lifetimes of Padovani & Matteucci (1993).

sample (with Sculptor stars belonging to the inner 0.2 deg of elliptical radius) with the data set provided by the Dwarf galaxies Abundances and Radial velocities Team (DART, covering a much larger radial extent and making use of the calcium triplet equivalent width to infer the Fe abundances; see Battaglia et al. 2008; Starkenburg et al. 2010), in order to have an MDF which were representative of the global Sculptor stellar populations. By looking at Romano & Starkenburg (2013, their figure A1), the low-metallicity portion of their MDF is almost solely determined by the DART sample, with the Kirby et al. (2009, 2010) MDF mainly contributing towards larger [Fe/H] abundances.

## 3 MODEL, ASSUMPTIONS AND METHODS

### 3.1 Database of stellar isochrones and stellar lifetimes

We make use of the PARSEC stellar isochrones (Bressan et al. 2012; Tang et al. 2014; Chen et al. 2015), as computed for the following grid of stellar ages and metallicities, by assuming a Reimers mass loss with efficiency  $\eta = 0.2$ .

(i) The step in metallicity in our isochrone data base is  $\Delta Z = 1.0 \times 10^{-4}$ , from a minimum metallicity  $Z_{\text{min}} = 1.0 \times 10^{-4}$  to a maximum metallicity  $Z_{\text{max}} = 3.0 \times 10^{-2}$ .

(ii) The step in age between two adjacent isochrones is  $\Delta \log(t/\text{yr}) = 0.01$ , from a minimum age  $\log(t_{\text{min}}/\text{yr}) = 6.5$  to a maximum age  $\log(t_{\text{max}}/\text{yr}) = 10.12$ .

For self-consistency, we assume in our model the same stellar lifetimes as the ones which can be derived from the PARSEC data base; in particular, we fit the stellar lifetimes with the following function:

$$\tau_m(Z) = A(Z) \times \exp[B(Z)m^{-C(Z)}], \quad (1)$$

where  $A(Z)$ ,  $B(Z)$  and  $C(Z)$  are the fitting parameters, provided with the corresponding  $1\sigma$  errors in the supplementary material, as functions of the metallicity  $Z$ . In Fig. 2 we compare our derived stellar lifetimes with the ones of Padovani & Matteucci (1993), which do not depend on metallicity and are extensively used in chemical evolution models.

### 3.2 Modelling the chemical evolution of Sculptor

The numerical code of chemical evolution is the same as the one adopted in Vincenzo et al. (2014, 2015) – where we address the reader for details – for the study of the classical and ultra-faint dSph galaxies. We make use of an updated version, by assuming the stellar yield compilation of Romano et al. (2010, their model 15) and the stellar lifetimes derived from the PARSEC isochrones.

We assume the galaxy to assemble by accreting pristine gas from an external reservoir, until an infall mass – given by  $M_{\text{inf}}$  – is accumulated at  $t_G = 14$  Gyr. The infall rate is assumed to follow a decaying exponential law, with typical time-scale  $\tau_{\text{inf}}$ . We assume for the star formation rate the Schmidt–Kennicutt law, namely  $\text{SFR}(t) = \nu M_{\text{gas}}(t)$ , where  $\nu$  is the so-called star formation efficiency (SFE) and  $M_{\text{gas}}$  is the galaxy gas mass. The run of the intensity of the SFR with time is crucially regulated by the various physical processes acting on  $M_{\text{gas}}$ , namely inflows and outflows of gas, returned matter from dying stars and Supernovae, astration due to the star formation activity itself.

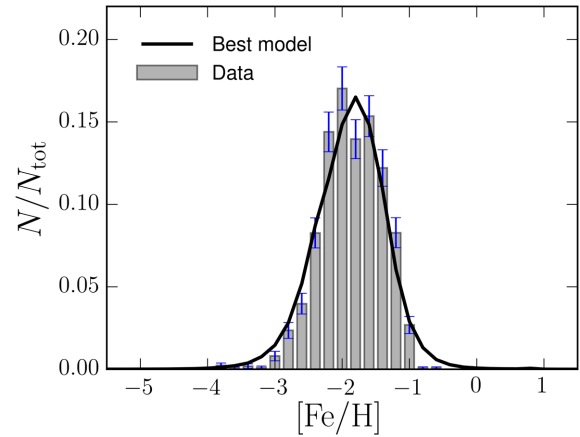
A fundamental role in the evolution of dSphs is played by the galactic outflows, which are predicted to occur very soon in these galaxies because of their shallow potential well; the intensity of the outflow rate is assumed to be directly proportional to the SFR. On the one hand, if the efficiency for the gas removal is high (typically  $\lambda_{\text{wind}} \approx 10 \text{ Gyr}^{-1}$ ), then the galaxy gas mass suddenly decreases and hence the SFR rapidly drops to zero; on the other hand, if the galactic wind has a relatively lower efficiency (typically  $\lambda_{\text{wind}} \approx 1 \text{ Gyr}^{-1}$ ), then the decrease in the SFR is smoother and it drops to zero on longer typical time-scales.

#### 3.2.1 The assumed best model

We have explored the parameter space, by running a large number of chemical evolution models. The best parameters for Sculptor are found by minimizing the  $\chi^2$  figure of merit, with the best model being the one reproducing the shape of the observed stellar MDF, which represents the most reliable observational constraint to any slight variation of the free parameters. We vary the SFE in the range  $\nu = 0.03\text{--}0.2 \text{ Gyr}^{-1}$ , the wind efficiency in the range  $\lambda_{\text{wind}} = 2.0\text{--}10 \text{ Gyr}^{-1}$ , and the infall time-scale in the range  $\tau_{\text{inf}} = 0.1\text{--}0.5 \text{ Gyr}$ . In order to allow our photochemical model to be more flexible when comparing its predictions with data, we make the further approximation of assuming the galactic wind to be always active over the whole galaxy lifetime; since all the galaxy physical properties in our chemical evolution model are normalized with respect to the infall mass, this assumption causes the predicted stellar MDF not to be influenced by the variation of the infall mass. In this simplified formulation of the galactic wind, all the galaxy physical properties (such as the SFR, stellar mass, gas mass, and so on) simply scale with the infall mass and our results can be easily readjusted for a different assumption of the cutoff in the elliptical radius of Sculptor stars (here we consider only stars with  $r_{\text{ell}} \leq 0.6$  deg). We find that the best chemical evolution model is characterized by the following parameters:

- (i) star formation efficiency  $\nu = 0.04 \text{ Gyr}^{-1}$ ;
- (ii) wind efficiency  $\lambda_{\text{wind}} = 3.0 \text{ Gyr}^{-1}$ ;
- (iii) infall time-scale  $\tau_{\text{inf}} = 0.3 \text{ Gyr}$ .

We assume at the beginning a reference infall mass  $M_{\text{inf,ref}} = 1.0 \times 10^8 M_{\odot}$ , as in Vincenzo et al. (2014), for which we predict a present-day total stellar mass  $M_{\star,\text{ref}} = 8.27 \times 10^5 M_{\odot}$ . The infall mass of the best model is then obtained by rescaling



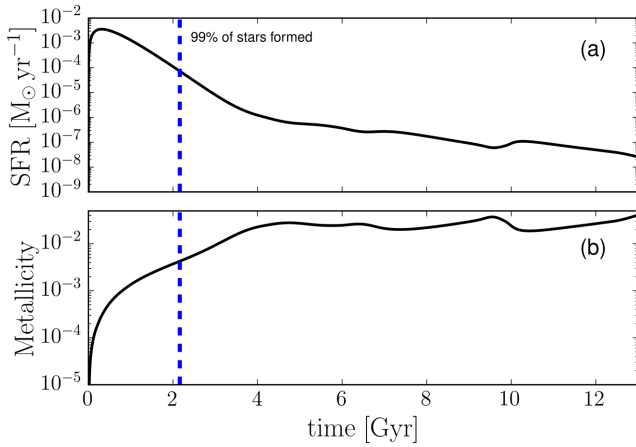
**Figure 3.** In this figure, we compare the observed Sculptor stellar MDF (Romano & Starkenburg 2013, grey histogram with blue error bars) with the predictions of our best Sculptor chemical evolution model, having star formation efficiency  $\nu = 0.04 \text{ Gyr}^{-1}$ , wind efficiency  $\lambda_{\text{wind}} = 3.0 \text{ Gyr}^{-1}$ , infall mass  $M_{\text{inf}} = 2.31 \times 10^8 M_{\odot}$ , and infall time-scale  $\tau_{\text{inf}} = 0.3 \text{ Gyr}$ . The predicted MDF is convolved with a Gaussian function with  $\sigma = 0.2$ .

our results for the reference model so as to have the same number of stars in the synthetic and observed CMD. We find for our best model an infall mass  $M_{\text{inf,best}} = 2.31 \times 10^8 M_{\odot}$ , giving rise to a present-day total stellar mass  $M_{\star,\text{best}} = 1.91 \times 10^6 M_{\odot}$ , larger than the value  $M_{\star} = (1.2 \pm 0.6) \times 10^6 M_{\odot}$  estimated by de Boer et al. (2012), but of the same order of magnitude.

According to the fitting formula of Faucher-Giguère, Kereš & Ma (2011), which is assumed in many recent works to mimic a cosmologically motivated infall in galaxy formation and evolution models, dwarf galaxies with  $M_{\text{halo}} = 10^8 M_{\odot}$  must have accreted almost 63 per cent of their cumulative infall mass (which turns out to be  $M_{\text{inf}} \approx 1.4 \times 10^8 M_{\odot}$ ) in the first  $\sim 1.5$  Gyr of their evolution, namely from redshift  $z = 6$  to redshift  $z \sim 4$ , a larger time-scale than the one found by our best model ( $\tau_{\text{inf}} = 0.3 \text{ Gyr}$ ). Nevertheless, we remark on the fact that the Faucher-Giguère et al. (2011) fitting formula is strictly valid only in the redshift range  $0 < z < 6$ , namely only after the reionization epoch; therefore, a comparison with the gas mass assembly history of our model is not straightforward.

In Fig. 3 the predicted stellar MDF of the best model (convolved with a Gaussian function with  $\sigma = 0.2$  dex) is compared with the observed one (Romano & Starkenburg 2013). The assumed very low SFE causes the MDF to be peaked at low  $[\text{Fe}/\text{H}]$  abundances. The width of the MDF is mostly determined by the wind efficiency; in particular, the lower the  $\lambda_{\text{wind}}$  parameter, the wider is the bulk of the galaxy star formation activity and hence also the MDF.

In Fig. 4(a) we show the predicted SFH of our best model, while in Fig. 4(b) we show the corresponding age–metallicity relation. In summary, the length of the bulk of the galaxy star formation activity can be regulated in our model by suitably varying the main parameters determining the star formation and outflow intensity and the galaxy gas accretion rate; these parameters are the SFE, which determines the intensity of the SFR and the rate of thermal energy injection by Supernovae, the wind efficiency, which determines the slope with which the SFR drops to zero, and the infall time-scale, which crucially determines the evolution with time of the galaxy potential well.



**Figure 4.** In this figure, we show the predicted SFH (top panel) and age–metallicity relation (bottom panel) as predicted by our best chemical evolution model for Sculptor. Our best model for Sculptor predicts that  $\sim 99$  per cent of the stars observable at the present time are formed within the first 2.16 Gyr of the galaxy evolution; this time corresponds to the vertical dashed blue line in the figures. Furthermore, the number of stars with initial metallicity  $Z < 1.0 \times 10^{-4}$  is roughly  $\sim 5.72$  per cent of the total number of stars alive at the present time.

### 3.3 The photochemical model

The stepwise structure of the photochemical model is the following.

(i) We sample the galaxy SFH, as predicted by our best chemical evolution model for Sculptor, to randomly extract an age for the formation of a given star.

(ii) We sample the assumed initial mass function (IMF) to randomly assign a mass to the star. In this work we assume the Salpeter (1955) IMF for simplicity.

(iii) We use the age–metallicity relation of our best Sculptor chemical evolution model to find the initial metallicity of the star.

(iv) Given the age, mass and metallicity of the star, we check whether the star is alive or not at the present time, by assuming the metallicity dependent stellar lifetimes we have derived from the PARSEC stellar evolutionary tracks (see Section 3.1).

(v) If the star can be observed at the present time, we store the photometric properties of the synthetic star, to later draw it in the synthetic CMD.

On the one hand, the strength of our method resides in the very fine grid of the assumed isochrone data base; moreover, in our approach, we start from the predictions of chemical evolution models, assuming *ab initio* an underlying galaxy formation and evolution scenario, which is physically motivated. On the other hand, the main shortcoming of our model is due to the fact that the lowest available metallicity in the PARSEC data base is  $Z_{\min} = 1.0 \times 10^{-4}$ . We assume that all the stars with  $Z < Z_{\min}$  have the same photometric properties as the stars with  $Z = Z_{\min}$ . This fact can introduce a systematic error. By looking at Fig. 4(a) and (b), according to our best model, the galaxy spends its first 122 Myr at metallicity  $Z < 1.0 \times 10^{-4}$ ; the number of stars with initial metallicity  $Z < 1.0 \times 10^{-4}$  is roughly  $\sim 5.72$  per cent of the total number of stars alive at the present time.

#### 3.3.1 Methods

To get a fair comparison with the observed CMD, we convolve the synthetic CMD with the distribution of the observed photometric

errors, by assuming that the latter are Gaussian. In particular, we first divide the observed CMD in a uniform grid and, for each grid element  $ij$ , we compute the average  $V$ - and  $I$ -band observed photometric errors,  $\bar{\sigma}_{ij}(V, I)$ , which we adopt as the standard deviations of the photometric noise in the  $ij$ th grid element. Hence, for any given  $k$ th synthetic star residing in the  $ij$ th grid element, we add the following noise to its predicted  $V$ - and  $I$ -band magnitudes:  $\bar{\sigma}_k(V, I) = r_k \times \bar{\sigma}_{ij}(V, I)$ , where  $r_k$  is a random number, drawn according to the standard normal distribution. In this way, the model ‘spreads out’ according to the errors in the data and we can fairly compare the synthetic with the observed CMD.

The synthetic CMD corrected for the photometric noise is then convolved with the results of the artificial star test performed by de Boer et al. (2011). In particular, by following a standard procedure, de Boer et al. (2011) inserted in the observed images a large catalogue of artificial stars; after reducing and analysing the altered images, they could compute the fraction of artificial stars recovered in the data as a function of their input magnitude and colour. We use the results of their test to compute the recovered fraction in each grid element, so as to throw out from the synthetic CMD the remaining lost fraction. By means of this type of analysis, one can apply to the synthetic CMD the same completeness profile as is present in the data. After correcting the synthetic CMD for the incompleteness, the number of synthetic stars strongly reduces, becoming  $N_{\text{tot,syn}} \approx 40636$ .

## 4 RESULTS

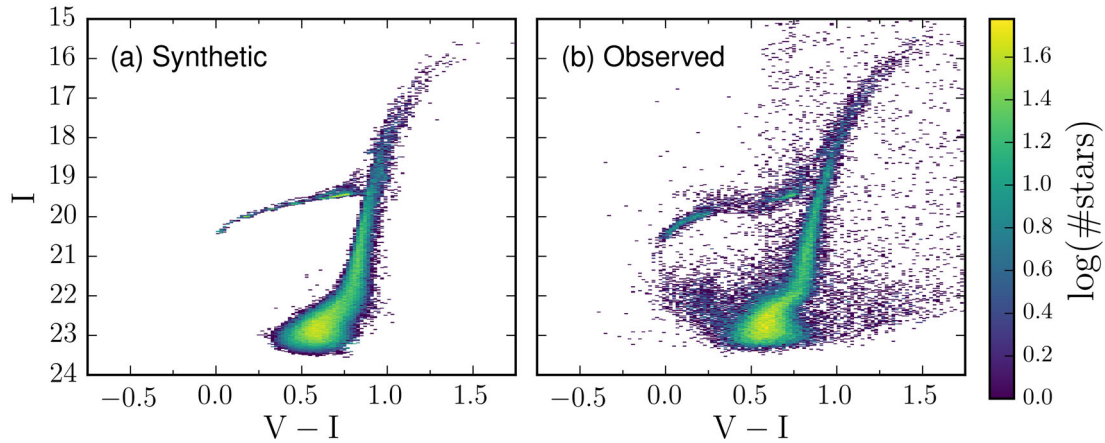
In this Section, we present the results of our photochemical model for the CMD of the Sculptor dSph. The main result of our work is shown in Fig. 5, where the synthetic CMD of Sculptor (left-hand diagram) is compared with the observed one (right-hand diagram). In order to better understand where the discrepancies between the observed and the synthetic CMD reside, in Fig. 6 we plot the residuals, which correspond to the colour-coding in the figure. In particular, to better visualize the differences, we define the residual in the  $ij$ th grid element as:

$$R_{ij} = \frac{n_{ij,\text{obs}} - n_{ij,\text{syn}}}{\sqrt{n_{ij,\text{syn}}}}, \quad (2)$$

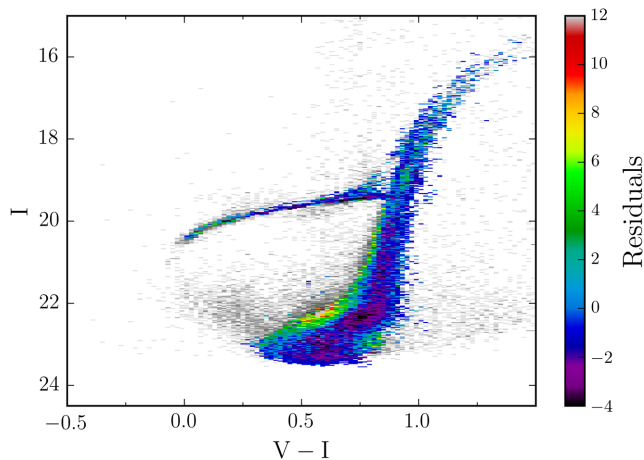
with  $n_{ij,\text{obs}}$  and  $n_{ij,\text{syn}}$  being the number of stars in the observed and synthetic CMD, respectively. The regions of the observed Sculptor CMD without any synthetic star are shown in Fig. 6 as a grey-scale density plot.

On the one hand, by a visual inspection of Figs 5 and 6, we can obtain a quite good agreement for the red giant branch (RGB), the horizontal branch (HB) and the asymptotic giant branch (AGB) of the observed CMD. On the other hand, at fainter magnitudes, particularly in the sub-giant branch (SGB) and at the MSTO, the observed CMD extends towards slightly bluer colours than the synthetic one. Moreover, our model cannot reproduce the observed population of blue straggler stars which extend the main sequence towards blue colours and could be – in principle – reproduced by including the effect of merging binary stellar systems. We do not include blue straggler stars in our photochemical model.

We remark on the fact that it is not obvious that a model reproducing the chemical evolution of Sculptor can also capture the main features of the observed galaxy CMD. In fact, the final configuration of the synthetic CMD turns out to be highly affected by the variation of the free parameters of chemical evolution models. In particular, by increasing the SFE, the stellar metallicities accordingly increase at any fixed galactic time, causing the entire synthetic CMD to shift



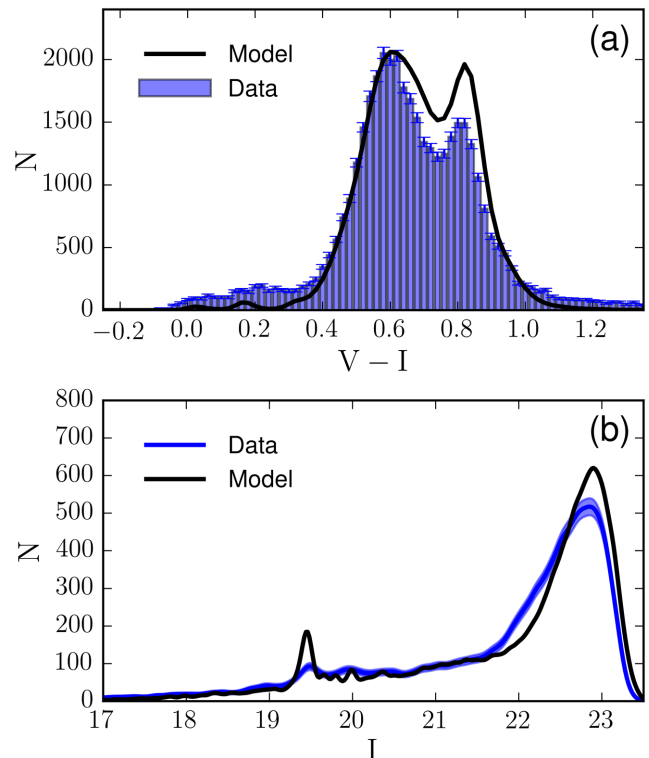
**Figure 5.** In the left-hand panel of this figure, we show the prediction of our photochemical model for the CMD of the Sculptor dSph, whereas on the right-hand panel we show for comparison the observed CMD. The synthetic and the observed CMDs are shown as 2D histograms, with the bin size in both the  $x$ - and  $y$ -dimensions being 0.02 dex and the colour-coding representing the number of stars, on a logarithmic scale, residing within each grid element.



**Figure 6.** In this Figure, we show the residuals (see equation 2) for the comparison between the observed and the synthetic CMD. The grey-scale density plot represents the regions of the observed Sculptor CMD where no synthetic stars are predicted. We find a good agreement for the RGB, HB and AGB stars, whereas the MSTO and the SGB of the observed CMD extend towards bluer colours than the synthetic CMD. We cannot reproduce the population of blue straggler stars in the observed CMD, since we do not include them in our model.

towards redder colours. The IMF acts in a similar way as the SFE, with the additional effect of filling up the various stellar evolutionary phases in the CMD with different relative fractions. Finally, the wind parameter and the infall time-scale crucially affect the spread of the predicted CMD, since they determine the length of the bulk of the galaxy star formation activity.

In Fig. 7(a), we compare the predicted stellar ( $V-I$ )-colour distribution (black solid line) with the observed one (blue histogram); this quantity turns out to be particularly sensitive to metallicity variations among the galaxy stellar populations. In Fig. 7(b), the predicted stellar luminosity function in the  $I$ -band (black solid line) is compared with the observed one (blue line with error bars, which are shown as a shaded blue area); the trend of this second quantity is more affected by the galaxy SFH and stellar lifetimes. An age indicator for the galaxy is given by the fraction of stars on the HB relative to the one on the RGB; we predict  $N_{\text{HB}}/N_{\text{RGB}} \approx 0.17$ .



**Figure 7.** In the top panel of this figure, we compare the predicted stellar ( $V-I$ )-colour distribution (black solid line) with the observed one (blue histogram with errorbars). In the bottom panel, we compare the predicted stellar luminosity function in the  $I$ -band (black solid line) with the observed one (blue line, with the shaded blue area representing the  $1\sigma$  errors). MSTO stars are predicted to reside in the synthetic CMD at  $m_I \gtrsim 23.0$  mag, whereas SGB stars at  $22.0 \lesssim m_I \lesssim 23.0$  mag. The peak in the  $I$ -band stellar luminosity function at  $m_I \approx 19.5$  mag is caused by HB stars.

At a first glance, our photochemical model is able to predict and qualitatively reproduce the main features of the observed ( $V-I$ )-colour distribution; in particular, the first peak in Fig. 7(a) (the one at bluer colours) is determined by the MSTO and SGB stars, whereas the second peak (the one at redder colours) is the signature left by the ascending RGB and HB stars.

Concerning the blue portion of the colour distribution, from a visual inspection of Fig. 7(a), we cannot reproduce the observed population of blue straggler stars, which – as aforementioned – are not included in our photochemical model. Furthermore, a remarkable discrepancy resides in the decaying trend of the blue wing of the predicted colour distribution, which contains a lower number of stars than the data, and in the predicted ‘saddle’, which turns out to be higher than the observed one. This can be also appreciated by looking at the residual plot in Fig 6, where the observed CMD clearly contains a larger number of MSTO and SGB stars with blue colours than the synthetic CMD. This discrepancy seems likely the signature of metal-poor stellar populations in the Sculptor dSph, which our one-zone chemical evolution model has not been able to capture. Nevertheless, in principle, it could also indicate a predicted age–metallicity relation which is steeper than what seems to be required by observations; in fact, one would obtain a similar discrepancy if also the synthetic metal-rich stars are older than the observed ones.

Interestingly, by looking at Fig. 3, the observed stellar MDF suggests the presence of two distinct peaks, corresponding to two separated main stellar populations in the galaxy. The latter feature cannot be resolved by our best chemical evolution model, which indeed predicts the stellar MDF to have a single peak, lying between the two of the observed distribution. We remark on the fact that this feature is peculiar to the Romano & Starkenburg (2013) MDF, which combines the DART sample – determining the low metallicity portion of the observed MDF – with the one by Kirby et al. (2009, 2010), concentrated towards slightly higher metallicity. The regions where the observed CMD contains a larger number of blue (metal-poor) stars than the synthetic one likely correspond to the low-metallicity peak in the observed MDF, which is also the most pronounced one. Accordingly, the higher ‘saddle’ in the predicted colour distribution (see the top panel in Fig. 7) confirms that the model predicts galaxy stellar populations which are intermediate between the observed metal-poor and metal-rich ones.

The observed stellar MDF, as derived by Romano & Starkenburg (2013), includes stars with  $r_{\text{ell}} \geq 0.6$  deg, namely beyond the radial cutoff we assume for the observed CMD. As one moves towards the outer zones of the galaxy, the Sculptor stellar populations are observed to become increasingly old and metal-poor and determine the observed stellar MDF at low metallicity. Nevertheless, the relative number of stars also increasingly diminishes when moving outwards, with almost 50 per cent of the Romano & Starkenburg (2013) sample being contributed by stars with  $r_{\text{ell}} \leq 0.2$  dex. Furthermore, the shape of the observed stellar MDF in the inner radial bins does not significantly vary at low metallicity with respect to the MDF in the outer bins (see fig. 14 of de Boer et al. 2012). Therefore, if we had applied a radial cutoff at  $r_{\text{ell}} = 0.6$  deg also to the observed MDF, our analysis would not have been significantly altered.

A viable solution to reduce the discrepancy between the observed and the synthetic CMD would be, for example, to disentangle the two different stellar populations in the observed MDF, by assuming two underlying separated distributions, peaked at slightly lower and higher [Fe/H] abundances than the predicted MDF of the best model. In this way, the metal-poor stellar population could be reproduced by assuming a lower SFE than the metal-rich one. After superimposing the two stellar populations in the synthetic CMD with appropriate weights, one would extend the synthetic CMD towards slightly bluer colour, hence obtaining a better agreement with the observed CMD. Finally, we cannot exclude that the lack of binary stars in our photochemical model might also contribute

to the discrepancy between the observed and the synthetic CMD, since their inclusion would cause a broadening of the MS and therefore a redistribution of the colours of the synthetic stars in Fig. 7(a).

In Fig. 7(b), the observed stellar *I*-band luminosity function is compared with the predicted one. For the RGB and AGB stars, there is a good agreement between the model and data. Furthermore, the model predicts a peak at  $m_I \approx 19.5$  mag, which represents the effect of HB stars; the presence of this peak is not visible in the observed *I*-band stellar luminosity function because of the large foreground contamination in the redder part of the observed CMD, both at fainter and at brighter *I*-band magnitudes than the ones of the observed HB. If we had considered only Sculptor stars in the innermost regions of the galaxy (e.g. with  $r_{\text{ell}} \leq 0.2$  deg), we would have obtained a well agreement between model and data also for the HB stars. At fainter magnitudes, the model in Fig. 7(b) contains a larger number of MSTO and a lower number of SGB stars than the data; this discrepancy might be partly due to the inherent uncertainty in the assumed completeness profile, which is particularly important for these evolutionary stages, as well as it could also indicate the need for an IMF with a lower number of low-mass stars than the Salpeter (1955) IMF assumed in this work.

## 5 CONCLUSIONS AND DISCUSSION

In this work, we have presented a new approach to draw the synthetic CMD of galaxies. In particular, we have developed *ab initio* a new photochemical model, which we have applied to reproduce the observed CMD of Sculptor dSph. Our numerical code starts from the predictions of chemical evolution models about the galaxy SFH and age–metallicity relation. Then, by assuming the PARSEC stellar evolutionary tracks, we can ‘light up’ the stars with different age, mass and metallicity of chemical evolution models, in order to draw a synthetic CMD. We have defined the best chemical evolution model for Sculptor as the one reproducing the observed galaxy stellar MDF.

Several improvements could be done in our photochemical model, by considering for example an underlying cosmological framework, whose primary effect would be to influence the evolution of the galaxy gas mass assembly with time. Interestingly, a very first attempt to draw the CMD of a dSph galaxy within a full cosmological framework by making use of a semi-analytical model for the galaxy formation and evolution is represented by the work of Salvadori, Ferrara & Schneider (2008), which adopted thefreely available IAC-STAR code (Aparicio & Gallart 2004), however, they did not provide a detailed discussion of their findings about the predicted galaxy CMD. A further improvement in our photochemical model would be to include the effects of unresolved binary stars and foreground contamination in the synthetic CMD.

The strength of our approach resides in the statistical sampling of the galaxy predicted SFH and assumed IMF, as well as in the assumption of a very fine grid of stellar isochrones, both in metallicity and in age. The main shortcoming is related to the PARSEC stellar isochrones, which are computed only for  $Z \geq 10^{-4}$ .

The SFH can be regulated in our models for dSphs by suitably varying the main parameters triggering the onset of the galactic wind and determining its intensity. In fact, once the galactic wind has started, the SFR rapidly drops to zero, since most of the infall mass has been accumulated fast within short typical time-scales. Our best model for Sculptor predicts that  $\sim 99$  per cent of the stars observable at the present time are formed within the first 2.16 Gyr of the galaxy evolution. We predict at the present time a total stellar

mass  $M_{*,\text{best}} = 1.91 \times 10^6 M_{\odot}$ , which is of the same order of magnitude as other estimates like  $M_* = (1.2 \pm 0.6) \times 10^6 M_{\odot}$  by de Boer et al. (2012). Also the predicted evolution of the SFR as a function of time is in agreement with the findings of de Boer et al. (2012).

Stellar systems or interstellar regions with low gas density, such as low-mass dwarf galaxies or the outer parts of spiral galaxies, likely follow a star formation law which deviates from the usually assumed Schmidt–Kennicutt law,  $\text{SFR}(t) = \nu M_{\text{gas}}(t)$ ; for this reason, we have done some numerical experiments by assuming the same expression for the star formation rate as in the original work of Kennicutt (1998) (see also Gatto et al. 2015 for a detailed study in the context of hydrodynamical simulations). By assuming the Kennicutt (1998) law, we predict the SFH to be more concentrated in the earliest epoch of the galaxy evolution and the metallicity  $Z$  to initially evolve more rapidly than our best-fitting model; then, at later times,  $Z$  remains quite constant when the Kennicutt (1998) law is assumed, while it increases in our best-fitting model. Finally, we find that the final total gas and stellar mass are almost the same when the two different expressions for the star formation rate are assumed.

We have shown that our photochemical model is able to capture the main features of the observed CMD of the Sculptor dSph, with the best agreement being obtained for the RGB, HB and AGB stars. The discrepancy has been found at fainter luminosity in the MSTO and SGB, where the observed CMD extends towards bluer colours than the synthetic one. That may be caused by underlying metal-poor stellar populations which our photochemical model has not been able to capture as well as to the lack of binary stars in our model, which would also broaden the synthetic CMD at faint magnitudes. In fact, the predicted stellar MDF is characterized by a single peak, whereas the observed one suggests the presence of two peaks, residing at slightly lower and higher  $[\text{Fe}/\text{H}]$  abundances than the model peak. In particular, the more pronounced peak in the observed MDF corresponds to the one at lower  $[\text{Fe}/\text{H}]$  abundances. Therefore, our photochemical model contains stellar populations which are intermediate between the metal-poor and the metal-rich ones in the observed stellar MDF.

In order to reduce the discrepancy, one could superimpose the results of multiple one-zone chemical evolution models and find the linear combination which provides the best agreement with the observed stellar MDF. This will be the subject of a future work, in which we will also show the effect of varying the free parameters of chemical evolution models on the synthetic CMD.

Although the uncertainties in the assumed completeness profile can be important at the MSTO and SGB, the discrepancy between model and data in the  $I$ -band stellar luminosity function for  $m_I \gtrsim 21.0$  mag might be alleviated by assuming an IMF which contains a lower number of low-mass stars than the Salpeter (1955) IMF assumed in this work and by including the effect of binary stars.

## ACKNOWLEDGEMENTS

FV thanks E. Brocato for insightful discussions during the visit at the Astronomical Observatory of Rome in 2014 December, and S. Recchi for his precious suggestions. FM and MT acknowledge financial support from PRIN-MIUR 2010-2011 project ‘The Chemical and Dynamical Evolution of the Milky Way and Local Group Galaxies’, prot. 2010LY5N2T. We thank an anonymous referee for his/her constructive comments.

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