

# 1                   **Methods for optimized design and management of CHP systems** 2                   **for district heating networks (DHN)**

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## 10 11 12 **Abstract**

13 The paper analyzes some of the problems connected with the design, construction and management of cogeneration  
14 plants for district heating networks (CHP-DHN). Although the advantages of cogeneration systems compared with  
15 conventional ones for separate energy production, one of the unresolved problems is that of the variability of operating  
16 conditions, can often render the application of these solutions ineffective. In particular, the aim of this study is to  
17 propose a multi-objective optimization methodology that tries to take into account both energy and economic aspects.

18 After an analysis of the current scenario, the application and use of CHP plants in the international context and the main  
19 technological features, followed by the identification of incentive systems that have allowed or limited the spread,  
20 attempts are made to define a design methodology based on a multi-level optimum design based approach for increasing  
21 the operation share of CHP. The methodology starts from a general system vision, up to detailed aspects such as the  
22 management of a CHP-DHN system, taking into account the multiplicity of variables and constraints involved. This  
23 methodology has been applied to two case studies representative of the different applications, to verify its robustness  
24 and analyze the possible results obtainable.

25 In particular, a general case was taken into consideration, in which a first level design was performed by analyzing  
26 various possible system configurations and evaluating their goodness through the tools provided by the aforementioned  
27 multi-objective methodology. Then the methodology has been applied to an intermediate level, taking into  
28 consideration an existing CHP-DHN plant and going to evaluate the performance considering possible modification of  
29 the operation.

30 The results obtained confirm that a combined energetic and economic approach to design allows to obtain an  
31 economically feasible system, but at the same time avoids incurring over-sizing, under-sizing or functioning phenomena  
32 far from the concept of energy efficiency, difference of what happens for many plants today in operation. Furthermore,  
33 through a simple variation of the modularity of the plant, significant benefits can be obtained.

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40

41 **Nomenclature**

42	c	specific cost [€/kWh];
43	C	total cost value [€];
44	f	gain function [€];
45	F	dimensionless function;
46	G	gain from the sale of energy [€];
47	I	exergy losses [W];
48	p	price [€/kWh];
49	P	power [W];
50	Q	thermal energy required for the operation [kWh];
51	$\dot{Q}$	thermal power [W];
52	$r_p$	relationship between prices of electricity and thermal energy;
53	$t_{eq}$	equivalent time [h];
54	w	weight factor;
55	$\dot{W}$	electrical power [W]

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58 **Greek symbols**

59	$\alpha_{CHP}$	cogeneration share;
60	$\lambda$	cogeneration ratio;
61	$\eta$	efficiency

62  
63

64 **Pedices, acronyms and abbreviations**

65	biom	obtained using biomass as input fuel
66	boiler	of the boiler
67	CHP	Combined Heat and Power or of the cogeneration system
68	cn	cumulative normalized
69	DHN	District Heating Network
70	el	of the electricity
71	h	instantaneous value
72	grid	from the grid
73	GT	Gas Turbine
74	i	relative to the single user
75	I	relative to the irreversibilities (exergy losses)

76	ins	relative to the installation
77	load	of the whole thermal load
78	O&M	relative to operation and management
79	ref	reference value
80	ST	steam turbine
81	th	of the thermal energy
82	tot	total value

## 83 **1. Introduction**

84 The combined production of electricity and heat (Combined Heat and Power, CHP) allows, in  
85 principle, to improve the overall energy efficiency of complex energy systems compared to the case  
86 of separate electricity production in thermoelectric plants and heat in conventional systems [1].

87 A district heating network (DHN) is a heat supply system based on centralized production or  
88 localized in a few production units and on distribution to the end user through an energy vector  
89 consisting of a fluid in temperature. with further savings prerogatives [2]. The idea of combining  
90 cogeneration systems with district heating (CHP-DHN) arises from combining the advantages of the  
91 two technologies, which can be reconciled in a natural way, to obtain a more efficient energy  
92 system, with a total cost reduction and an improvement in terms of environmental impact.

93 Anyway the problem is that thermal civil/residential loads are often difficult to be predicted because  
94 they are characterized by a strong seasonal and daily variability, also due to the different use of  
95 buildings; moreover, the thermal demand sometimes presents high ratios between maximum and  
96 minimum values (peaks of 3-10 times the base load). This does not allow the plants to be used in  
97 conditions close to those of the project, imposing the mandatory use of thermal integration systems,  
98 like auxiliary boilers, with the specific function of covering the peaks of the thermal load [3].

99 To date the design of CHP plants for district heating (CHP-DHN) is performed according to various  
100 methods, linked to technological needs, to economic incentive systems taking into account the  
101 characteristics of the loads to be satisfied. The choice of the management logic of these systems is  
102 one of the aspects that often constrain the sizing, producing, for similar applications, different  
103 engineering solutions [4].

104 In recent years, the diffusion of CHP plants has been strongly encouraged by the various national  
105 governments, especially in Europe [5]. The incentive system has often been linked to generic  
106 technical concepts such as "high performance" and "primary energy savings", by qualifying the  
107 plants through the use of synthetic indicators, the evaluation of which is often carried out in a  
108 particular condition. The use of these indicators, being connected to the design conditions does not  
109 evaluate the real operation of the plant. The economic advantage that derives from incentives tends  
110 therefore to overshadow some negative aspects related to the real operation of the systems [6]. In  
111 particular, observing the various CHP applications, there is a tendency to phenomena such as over-  
112 sizing or under-sizing, which cause distortions in the energy saving potential of those systems [7].

113 After carefully analyzing the problems related to the design and operation of the plants, the paper  
114 tries to develop an optimized multi-level design methodology, starting from a general analysis up to  
115 dealing with aspects of detail, and multi-objective , as it proposes a combined energy and economic  
116 analysis [8] assigning a penalty cost to the energy degradation: the aim is to maximize the share of  
117 cogeneration production by minimizing the contribution of additional thermal units (auxiliary

118 boilers) thus reducing the irreversibility of the system. Then the methodology is applied to two case  
 119 studies, one considering the design of a new plant starting from a typical load conditions, while the  
 120 second is an optimization of the operation management of an existing plant considering the possible  
 121 introduction of a storage system.

122  
 123

## 124 2. Cogeneration plants and district heating: technology, state of the art and open problems

125 The first element to be considered in the analysis of a CHP plants is the reference technology.  
 126 Although often this is considered almost as a predetermined variable, this being mainly linked to the  
 127 size, there are some peculiarities that make the various solutions quite different. A very important  
 128 element is the parameter known as a cogeneration ratio  $\lambda$ , defined as the ratio between thermal and  
 129 electrical power produced by the plant in nominal conditions:

130

$$131 \lambda = \frac{\dot{Q}}{W} \quad (1)$$

132

	Technology	$\lambda$ values	Positive characteristics	Negative characteristics
Medium to high size	Steam turbine (ST)	0.5÷10	Modulability, quite low costs	Quite low electrical efficiency, not good for intermittent operations
	Gas turbine (GT)	0.5÷2.5	High temperature recovery, high flexibility	Low operational flexibility, medim to low efficiency values
	Combined cycle (CC)	0.5÷3	High electric efficiency, possibility of modulation	Reduced starts-and-stops, high specific costs
Medium to low size	Internal combustion engines (ICE)	1÷5	Flexibility, quite good efficiency at partial load	Direct link between electricity and thermal energy
	ORC plants (ORC)	0.5÷10	Adaptability at Renewable Energy Sources	Use of a different operating fluid
	Fuel cells (FC)	0.5÷2	Very low power	Technology not commercially developed
	Microturbines ( $\mu$ TG)	0.5÷2.5	High quality technology	Reduced flexibility, quite low efficiency values, high costs

133

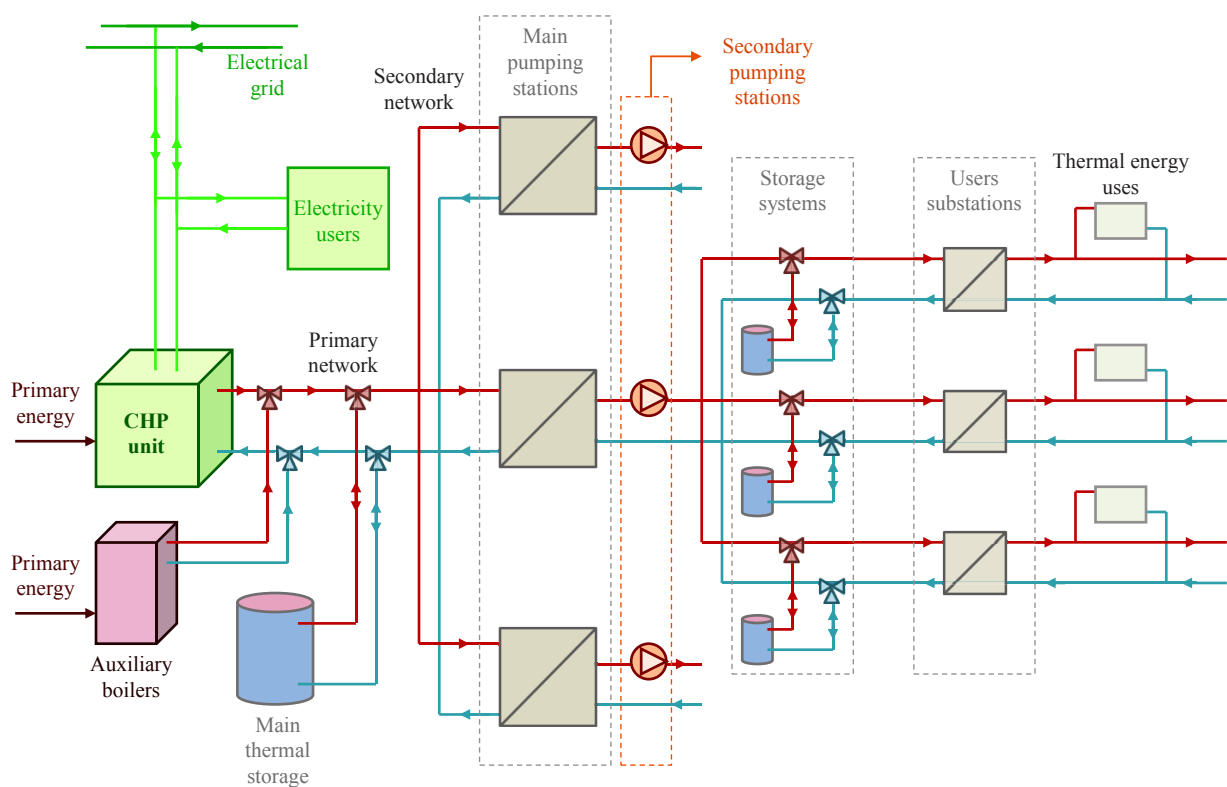
**Table 1: cogeneration technologies and main features.**

134

135 the main CHP technologies currently available are shown in Table 1. A primary distribution system  
 136 and a secondary one are required, deriving from the main line of distribution a network of pipes  
 137 with reduced diameters and operating pressures. The network hosts secondary heat exchange  
 138 substations and pumping substations. The exchange substations allow transferring heat for the final  
 139 uses.

140 Fig. 1 shows a typical scheme of a district heating network with the various components (CHP  
141 units, auxiliary boilers, heat exchangers, storage systems and piping network); the typical values of  
142 the main operating parameters are shown in Table 2.

143 The international scenario of development and diffusion of cogeneration systems is quite variable  
144 from country to country, but in general the role that the incentive systems introduced in each  
145 country play, has been important. These tools have often led to a development linked to purely  
146 economic reasons to replace the original energy objectives [9]. Some countries have obtained  
147 important benefits from a more effective and structured incentive system (e.g. Denmark and South  
148 Korea). Alongside incentives, other factors that have diversified the spread of these systems are the  
149 typical climate, population and geographical extent. Table 3, constructed referring to the data from  
150 Euroheat & Power 2015, shows what is the current state of diffusion of CHP-DHN systems in the  
151 Italian case and in the two virtuous countries mentioned.



152  
153 **Fig. 1. General scheme of a district heating network.**

154  
155 The difficulties related to design, combined with the distortion of the objectives often generated by  
156 the incentives, have determined a series of problems still open, first of all the already mentioned  
157 over sizing of the CHP units resulting in poor efficiency in operation outside the nominal conditions

158 and the frequent use of supplementary thermal units with CHP systems used to cover only the basic  
 159 heat load values. It is therefore necessary to identify suitable methods to redirect the development  
 160 and implementation of these systems in the energy optics. To obtain results from a method such as  
 161 the one described, however, it is necessary the knowledge of loads.

162

Network	Fluid velocity	Max pressure	Input Temperature	Return temperature
Primary	2÷3.5 m/s	10 bar	90 °C	70 °C
Secondary	1÷2.5 m/s	6 bar	80÷85 °C	60÷65 °C
Substations	Thermal power	Input Temperature	Return temperature	
Primary	250÷2000 kW	80÷85 °C	60÷65 °C	
Users	15÷200 kW	70 °C	50÷55 °C	

163

**Table 2. Main features of the district heating networks: primary heat exchangers and substations.**

164

	Denmark	South Korea	Italy
CHP power installed (GW)	6.0 GW	7.7 GW	27.0 GW
CHP vs. electricity production	66%	5%	48%
CHP for DH production	73%	67%	68%
Thermal energy for DH (GWh)	29323 GWh	47859 GWh	9200 GWh
Poputation (Millions)	5.64	50.42	60.80
Population served by DH (%)	63%	15%	6%
Incentivation policies	Carbon taxes; feed-in tariffs; fiscal incentivations	Subsides	White certificates; incentivations
Climatic characteristics	Cold; quite homogeneous in the territory	Climate; reduced disomogeneity	Variable and not homogeneous

165

**Table 3. Comparison of the spread of cogeneration and district heating in three different countries**

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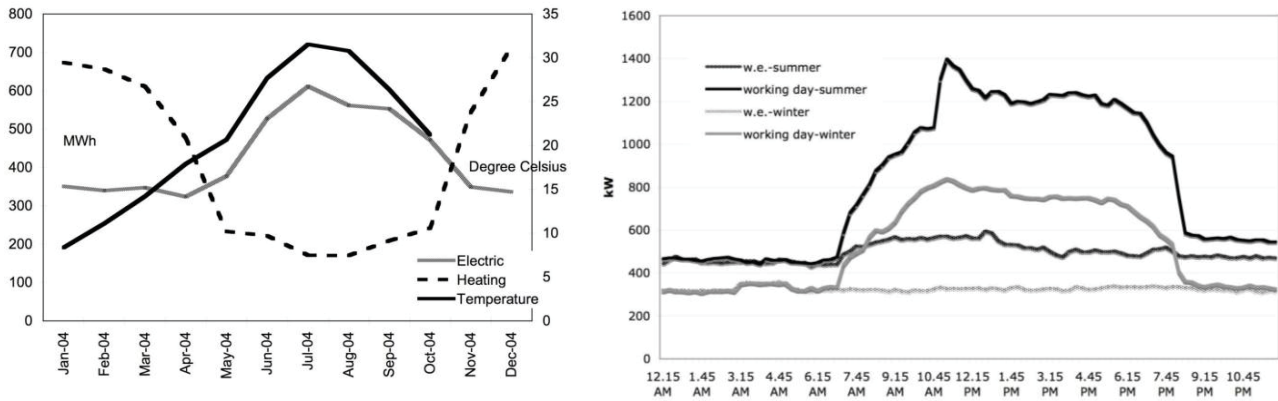
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### 3. Definition of electrical and thermal loads for CHP design

169 The most important problem connected with the design of CHP systems is the variability of loads in  
 170 the different operating conditions, both during the single days and in the different seasonal  
 171 conditions. This difference is particularly relevant for what concerns the thermal load.

172 A first topic that need to be carefully analyzed when one thinks about the design of a CHP plant for  
 173 a DHN is the definition of thermal and electrical loads. Both the electrical and thermal load show a  
 174 seasonal and a daily variability, in comparison with the trend of the outside temperature and  
 175 considering the various hours of the day. In a lot of application of civil structures, the differences  
 176 between working days and holidays of daily loads must be taken into account. Fig. 2 shows the  
 177 particular trend of thermal and electrical load for some University buildings, during the different  
 178 months of the year and during the different hours of the day, with reference to the particular day.

179 Fig. 2, obtained from [10] provides the experimentally obtained value of electrical and thermal  
 180 loads for a typical working day during winter and summer time and typical weekend day during  
 181 winter and summer time, obtained in two Italian University buildings. The data are obtained by  
 182 means of direct measurements.  
 183



184  
 185 **Fig. 2. Variability of electrical and thermal loads (data for the University of Siena Science Building according to**  
 186 **the data of [10]).**  
 187

188 Given the importance of the loads and in light of the strong variability associated with them, an  
 189 analysis of some typical cases has been performed. Attention has been focused on the aggregation  
 190 of the data in groups of utilities and buildings. This can be considered as a mean for a preliminary  
 191 homogenization of the loads in view of the realization of a CHP plant, proposing a general method  
 192 for quantifying the advantages obtainable from the use of this tool. In particular, an analysis was  
 193 carried out on four different uses: residential, offices, hospital and university.

194 In the case of a single user it can be quite simple to obtain the typical load profile by means of  
 195 direct measurements. The problem is more complex in case of a generic users before the installation  
 196 of the plants: in this case a profile of the user has to be identified using typical load profiles.

197 Typical curves defining electrical and thermal loads have been constructed in the form of  
 198 "normalized cumulative" curve, obtained by calculating the cumulative instantaneous values as the  
 199 sum of the values of the various individual users divided for the maximum of the sum of the  
 200 instantaneous values of the same:

201  
 202 
$$P_{h,cn} = \frac{\sum_i^n P_{h,i}}{\max\{\sum_i^n P_{h,i}\}} \quad (2)$$
  
 203

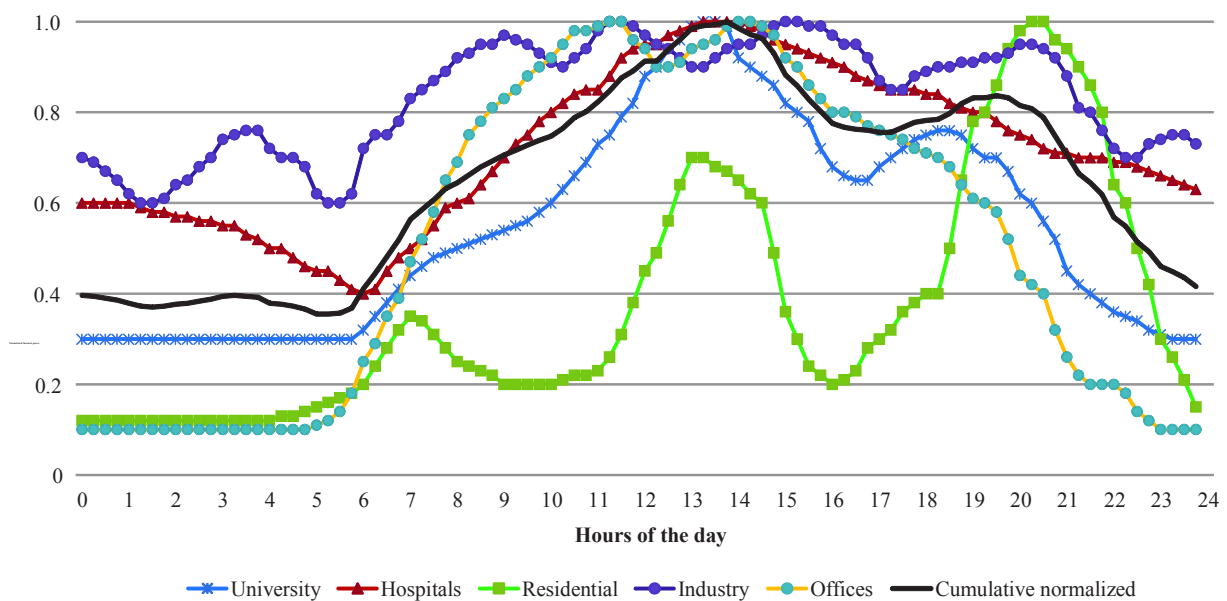
204 Where P is the generic power, the subscript h indicates the instantaneous value and the subscript cn  
 205 stands for cumulative normalized. Considering the right side of the equation, index i of the sum  
 206 indicates the different type of users (assuming to assign a progressive number to the four available)



207 and n is the total number of cumulative users (which will vary between 2 and 4 for the various  
 208 combinations). The users are grouped considering different typologies (residential user, various  
 209 civil users like hospitals, university buildings, offices and industrial users) and for each group of  
 210 users the graphic shows a value of the normalized power ranging between 0 and 1. Obviously, to  
 211 obtain a dimensional value it is necessary to multiply the value reported in the graphs and the total  
 212 power installed to serve the different users: the value can be quite different.

213 This procedure allows obtaining benefits in terms of homogenization of the energy demand, through  
 214 reduction of peaks in the corresponding graph, benefits that become exploitable from the point of  
 215 view of a better sizing of the plants and their more efficient operation. Fig. 3 shows for example the  
 216 diagrams relative to the electric loads in all the analyzed combinations of typical buildings use  
 217 compared to the various loads. The dimensionless value reported in the ordinate axis represents the  
 218 ratio between the power required and the maximum power required during the day. A similar  
 219 behaviour could be found for the thermal loads.

220 The aggregation of data is a preliminary operation before the design: if there is the possibility to  
 221 choose the utilities to be fed with a cogeneration plant and in particular the load trends are available  
 222 from measurements or different forecasting methodologies, the application of the method  
 223 introduced in this paragraph allows taking a step forward in the design. The choice of an overall  
 224 load having a performance with functional characteristics for a more correct operation of the plant  
 225 constitutes an advantage and creates conditions that favour, in addition to operating management,  
 226 the definition of an optimal size of the plant. This can be interesting before the preliminary design  
 227 of a CHP-DHN system even if it is quite difficult to verify this kind of opportunity in the practical  
 228 experience.



229  
 230

**Fig. 3. Normalized electrical power for different aggregation of energy “users” in Italy**

231 **4. Methodologies for optimized design and management of CHP for DHN network**

232 The design of cogeneration systems is often based on satisfying a specific thermal load, usually  
 233 low, by assigning to auxiliary units and storage systems the task of regulating and modulating the  
 234 system. This tends to reduce the percentage of operation in cogeneration defined as the ratio of  
 235 thermal energy from CHP,  $Q_{CHP}$  and the total thermal energy required  $Q_{load}$ :

236  
 237 
$$\alpha_{CHP} = \frac{Q_{CHP}}{Q_{load}} \tag{3}$$

238  
 239 Several attempts are available in the literature to provide design methods that are qualitatively better  
 240 than those commonly used today based mainly on economic elements, in the field of CHP systems:  
 241 some more or less homogeneous groups can be identified, reported in Table 4.

242 Despite the apparent wide availability of methodologies for the optimized design of CHP systems,  
 243 many of those analyzed correlate with particular application situations and plant types: each author  
 244 investigates some relevant aspects associated with cogeneration systems, trying to propose  
 245 optimizations of the system components or specific design criteria related to certain contexts.

246

Approach	Characteristics and main objectives	References
Design	Search for the best plant configuration combined with an optimal distribution system and an interconnection between functional utilities and design objectives	[11-14],
Operation and management	Determination of the operational management to be adopted, in particular by using the instrument constituted by the thermal storage	[15-17]
Performance	Design of self-sufficient CHP systems with minimum energy excesses; search for methods and indicators to correctly evaluate the achievement of the objectives	[7], [18-19]

247 **Table 4: Studies available in the literature on the topic of the optimized design of CHP-DHN systems.**

248

249 However, two open issues can be identified. The first is the extremely high non-uniformity, which  
 250 presents very general cases together with particular problems, not allowing information to be  
 251 obtained in situations that go beyond those proposed. The second concerns the lack of a general  
 252 vision that allows to characterize the problem related to the design of CHP-DHN systems in a valid  
 253 way for any application, and not bound to the individual case, so as to be able to identify solutions  
 254 that can be readjusted to different situations.

255 What is needed is the union of all the approaches under a single design method of CHP-DHN  
 256 systems: the interest should pass from a detailed vision to a general one, involving all the positive  
 257 aspects emerging from the available studies to enclose them under a common methodology of  
 258 analysis. The idea is to start from a broader vision, at a system level and to develop design step by

259 step, with the aim of identifying at first the not optimal solutions to be discarded at an initial step,  
260 and proceed to investigate at a level of detail only those that are valid from an energy point of view.  
261 A relevant example is given by over sizing of the thermal integration units (auxiliary boilers): a  
262 cogeneration plant for district heating that works at full capacity throughout the year will certainly  
263 operate for a high number of hours and will achieve the objectives related to the return on  
264 investment in a short time. However, a plant of this type will certainly require an additional thermal  
265 input from one or more auxiliary thermal devices, and therefore from the point of view of the  
266 exergy efficiency it will not be optimal at all. Following the analysis of the literature and the  
267 problems identified, therefore, this work proposes a method that allows facing in general the design  
268 of CHP-DHN plants and to develop it with a multi-objective approach through a declination of the  
269 multi-level design approach thus structured:

270

- 271 - system design;
- 272 - nominal design;
- 273 - operational design.

274

275 The optimized design consists in the definition of a problem in which there are some objective  
276 functions and some boundary conditions that constitute the constraints. This concept is important  
277 because it is the one that creates the fundamental distinction between designs aimed only at  
278 compliance with specifications and optimized design: in the first the constraints are precisely the  
279 design specifications, while in the second are also some conditions that guide the problem towards  
280 optimal solutions. It is therefore possible to identify a structure that underlies the optimized design:

281

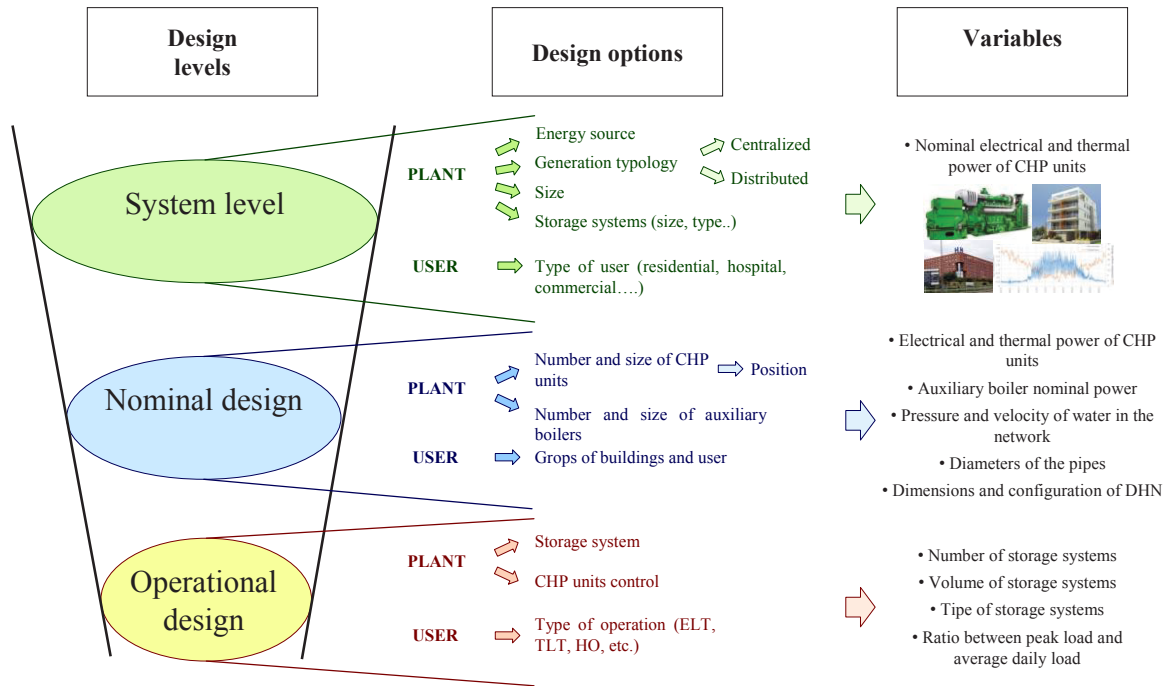
- 282 - model of the physical system;
- 283 - definition of the variables;
- 284 - determination of the objective functions;
- 285 - identification of the constraints.

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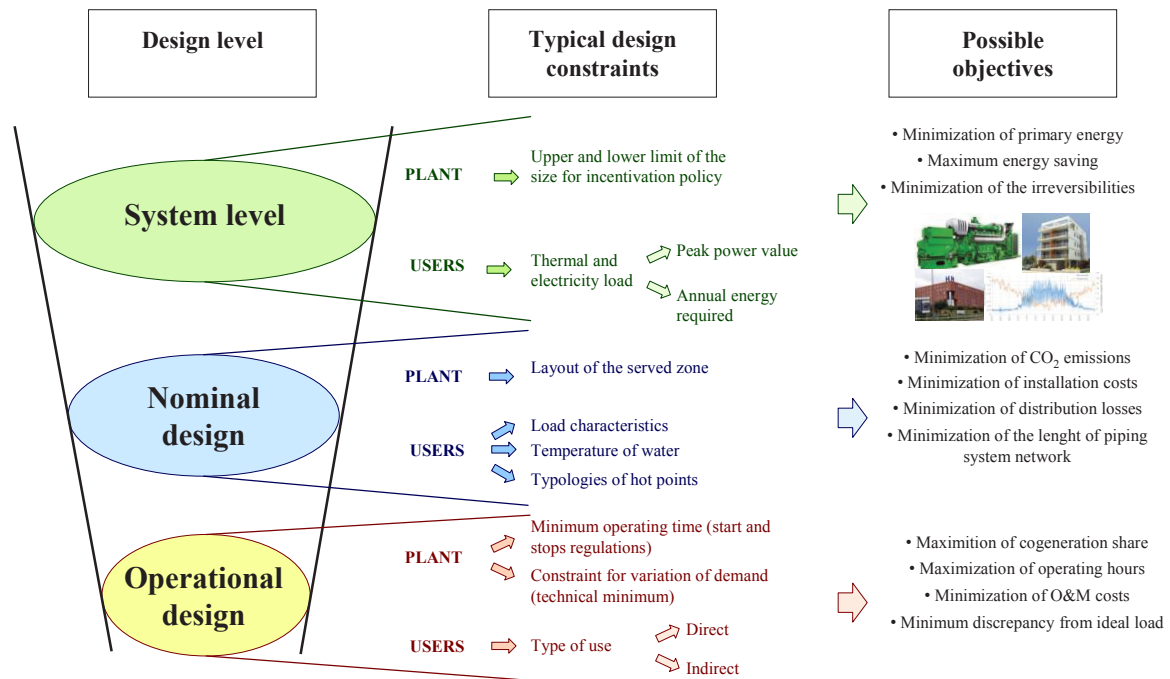
287 Fig. 4 introduces the logic on which the optimized design methodology proposed in this work is  
288 developed. The methodology is articulated at three different levels identifying, for each of them, the  
289 main aspects related to the system under analysis (in this case a CHP-DHN) and to the users of the  
290 district heating. In Fig 4(a) some possible design options and possible variables are described, while  
291 in Fig 4(b) possible objective functions and design constraints for the different levels are defined.

292 The analysis starts from the identification of the constraints and of the possible objectives to be  
293 achieved for the optimum design. The problem is then to finally determine the values assumed by  
294 the variables involved. The process is iterative: by acting on boundary conditions, objectives and

295 design variables, it is possible the determination of the optimal values for the variables that describe  
 296 the analyzed system.  
 297



(a)



(b)

Fig. 4: three-level scheme proposed for the development of the design of cogeneration systems for DHN:  
 (a) variables and parameters at the three levels; (b) typical objectives and design constraints

300  
 301  
 302  
 303

304

#### 305 **4.1. Multi-objective optimization methodology for the design of CHP-DHN systems**

306 The optimization methodology proposed in this work is based on the idea of assigning a penalty  
307 cost to the irreversibility. The main idea is that in the economic analysis of the CHP-DHN system  
308 the energy degradation connected to the operation of both CHP units and supplementary boilers  
309 assumes an economic value and therefore constitutes a cost item.

310 The minimization of the indicator so defined permits of defining a kind of multi-objective  
311 optimization in which economic and energetic elements are considered.

312 To implement such a methodology, a first analysis of the costs attributable to a CHP-DHN plant  
313 was performed, identifying three main items: installation costs,  $C_{ins}$ , operating and maintenance  
314 costs,  $C_{O\&M}$  and the cost of the resource used,  $C_{res}$ . To them it is added the cost assigned to the  
315 irreversibility of the system, indicated with  $C_I$ . The total cost function, defined as the sum of all  
316 costs, is given by:

317

$$318 \quad C_{tot} = C_{ins} + C_{O\&M} + C_{res} + C_I \quad (4)$$

319

320 The objective function for the optimization is a gain function  $f_g$  defined as:

321

$$322 \quad f_g = (p_{el}W + p_{th}\dot{Q}) \cdot t_{eq} - C_{tot} = f - C_{tot} > 0 \quad (5)$$

323

324 Where  $f_g$  is defined as the gain factor;  $f$  is the gross gain function; and  $p_{el}$  and  $p_{th}$  the selling prices  
325 of electricity and heat given in €/kWh;  $t_{eq}$  is the equivalent annual operating time, expressed in  
326 hours. The most important element of the methodology is the definition of an appropriate value of  
327 the cost of irreversibility (exergy losses),  $c_I$ .

328 Assuming to assign to a system that produces only electrical energy a cost of irreversibility  
329 proportional to the value of the price of electricity and thermal energy; equal to  $p_{el}\eta_{el,ref}$ , and to one  
330 for thermal energy production only, a cost  $p_{th}\eta_{th,ref}$ , for a CHP system it is possible to think to a  
331 structure of the type:

332

$$333 \quad c_I = \frac{w_{el}p_{el}\eta_{el,ref} + w_{th}p_{th}\eta_{th,ref}}{w_{el} + w_{th}} \quad (6)$$

334

335 where  $\eta_{el,ref}$  and  $\eta_{th,ref}$  are reference values that can be identified considering the current  
336 technological level, while weight factors are  $w_{el}$  and  $w_{th}$  respectively. Considering a typical  
337 situation, the values of the references efficiency values for  $\eta_{el,ref}$  and  $\eta_{th,ref}$  can be for example 0.4

338 and 0.85, while the weight factors can be chosen arbitrarily. In general cases, the expression of the  
339 cost of the irreversibility becomes:

340

$$341 \quad c_I = \frac{\eta_{el,ref} + \eta_{th,ref} \cdot \frac{\lambda}{r_p}}{\lambda + 1} \cdot p_{el} \quad (7)$$

342

343 where  $\lambda$  is the ratio of cogeneration and  $r_p = p_{el}/p_{th}$  is the relationship between prices of electricity  
344 and thermal energy. The value can be obtained as a ratio between the actual cost of electricity and  
345 the cost of natural gas: it can be considered typically in the range between 2 and 4.

346 The expression thus obtained makes use of only dimensionless parameters, with the exception of  
347  $p_{el}$ , which is assumed in this treatise as the main economic reference parameter. It is possible to  
348 formulate the problem of multi-objective optimization by using the utility function method [20],  
349 which envisages defining a function given by the sum of the individual objective functions, each  
350 multiplied by a weight. The optimization problem will therefore consist in finding the vector of  
351 variables

352

$$\mathbf{X} = \{x_1, x_2, \dots, x_n\}$$

353

354 for which it is possible to minimize the utility function defined by the total cost of the system:

355

$$U = C_{tot}(\mathbf{X})$$

356

357 subject to the constraints:

$$g_j(\mathbf{X}) \leq 0, \quad j = 1, 2, \dots, m$$

358

359 being the constraints defined by the appropriate boundary conditions identified in the design. The  
360 operational cost of the plant will be expressed in €/year, considering an economic life time of the  
361 plant, which allows an objective comparison of different configurations.

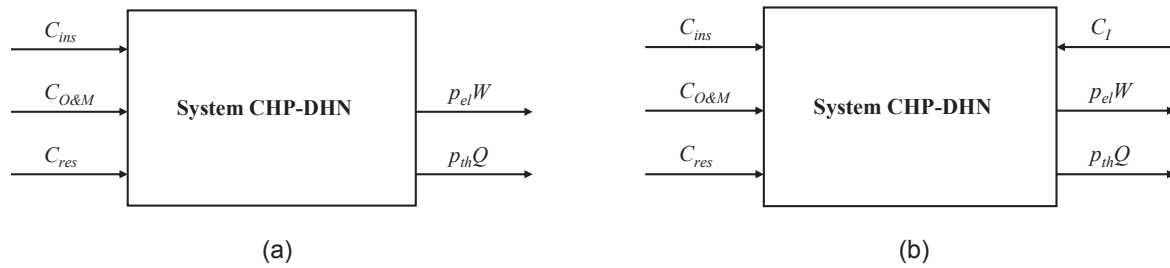
362 The situation is represented in Fig. 5 in which the difference between the classical economic  
363 analysis and the proposed analysis is evidenced.

364 The basic idea of the method is the following: considering a typical CHP plant with an auxiliary  
365 boiler for the thermal integration from a qualitative point of view the classic economic approach,  
366 represented in Fig. 5(a) determines a reduction of the size of the CHP plant and a relevant use of the  
367 auxiliary boiler, that has a low economic cost and a quite high First Law efficiency even if very low  
368 Second Law efficiency and quite high irreversibility. This is not good in general because does not  
369 permit to really appreciate the beneficial effect of CHP plants that are often designed on the base of

370 a minimum thermal load. An approach like the one proposed in the paper and represented  
 371 schematically in Fig. 5(b) by means of an introduction of a penalty to the irreversibility (represented  
 372 by the cost  $c_I$  will surely determine an increase of the size of the CHP and a reduction of the size  
 373 and of the operating time of the auxiliary boiler.

374 The method exposed in Fig. 5(b), that can be considered similar to a “thermo-economic” based  
 375 approach, has been already applied by one of the author of the present paper, to the context of  
 376 different energy systems, like exposed in [21].

377



378

379

**Fig. 5: Scheme of costs and gains associated with a CHP-DHN system:**

380

**a) in a traditional economic analysis; b) in a combined energy and economic analysis.**

381

382 It was considered appropriate to define another expression of the cost of irreversibility that is based  
 383 on that already obtained and that adequately penalizes the degradation connected to the thermal  
 384 integration units. By assimilating a boiler to a cogeneration unit in which the installed electric  
 385 power is set at zero, it is possible to obtain an expression for the costs of the irreversibility due to  
 386 the operation of the auxiliary boiler:

387

$$388 \quad c_{I,boiler} = f_{c,b} \cdot \frac{\eta_{th,ref}}{r_p} \cdot p_{el} \quad (8)$$

389

390 where  $f_{c,b}$  is a corrective factor chosen appropriately in such a way as to guarantee compliance with  
 391 the condition  $c_{I,boiler} > c_I$ , in order to avoid that optimization leads to an unbalanced system in  
 392 favour of production from auxiliary units determined by lower relative cost of the irreversibility of  
 393 this last component. Similarly, it is possible to state that the method adequately penalizes the  
 394 solutions that make extensive use of electricity taken from the national network, to avoid a strong  
 395 underproduction aimed at transferring costs to the end user. To do this, a cost of irreversibility has  
 396 been introduced. It is associated with the electric energy withdrawn, a function of the average  
 397 national electrical efficiency:

398

$$C_{I,el} = c_{I,el} \cdot I_{el} = c_{I,el} \cdot \frac{1-\eta_{el,ref}}{\eta_{el,ref}} \cdot W_{grid} = c_{I,el}^* \cdot W_{grid} \quad (9)$$

400

401 where  $W_{grid}$  is the electricity from the grid,  $I_{el}$  the energy degradation associated with it and  $c_{I,el}^*$   
 402 represents a specific cost of the irreversibility according to the average national generation  
 403 efficiency, dependent on the specific cost,  $c_{I,el}$  which can be identified as the price of electricity,  $p_{el}$   
 404 An allocation of costs to the irreversibility thus articulated guarantees:

405

- 406 - the penalization of operational mode characterized by greater irreversibility;
- 407 - a more significant penalization of the irreversibility deriving from the use of thermal integration
- 408 units compared to that associated with the degradation in the CHP;
- 409 - a penalty associated with electricity taken from the grid, which avoids solutions characterized by a
- 410 low percentage of cogeneration share.

411

412 In particular, the method proposed allows to identify an optimum that has the following  
 413 characteristics:

414

- 415 - from an electrical point of view, production is as close as possible to that required;
- 416 - from a thermal point of view, production from auxiliary units is reduced to a minimum and is the
- 417 one that minimizes the energy degradation associated with the energy produced in cogeneration.

418

419 The cost of the overall irreversibility will therefore be given by:

420

$$C_{I,tot} = C_I + C_{I,boiler} + C_{I,el} = p_{el} \cdot \left( \frac{\eta_{el,ref} + \eta_{th,ref} \frac{\lambda}{r_p}}{\lambda + 1} \cdot I_{CHP} + f_{c,b} \cdot \frac{\eta_{th,ref}}{r_p} \cdot I_{boiler} + \frac{1-\eta_{el,ref}}{\eta_{el,ref}} \cdot W_{grid} \right) \quad (10)$$

422

423 It should be observed that, for a qualitative analysis, in which only a first assessment of costs has  
 424 been made, the condition  $f_g = f - C_{tot} \geq 0$  may not be verified. In this case, it would be advisable to  
 425 make a comparison referring to the gross profit/cost ratio, of the dimensionless type, capable of  
 426 providing an effective comparison criterion independent of this aspect. This function is the ratio  
 427 between the gross gain function  $f$  and the total cost:

428

$$F = \frac{f}{C_{tot}} \quad (11)$$

430



431 The F function can be used both as objective function to be maximized and as multi-objective  
432 indicator for a comparative analysis of different solutions.

433

434

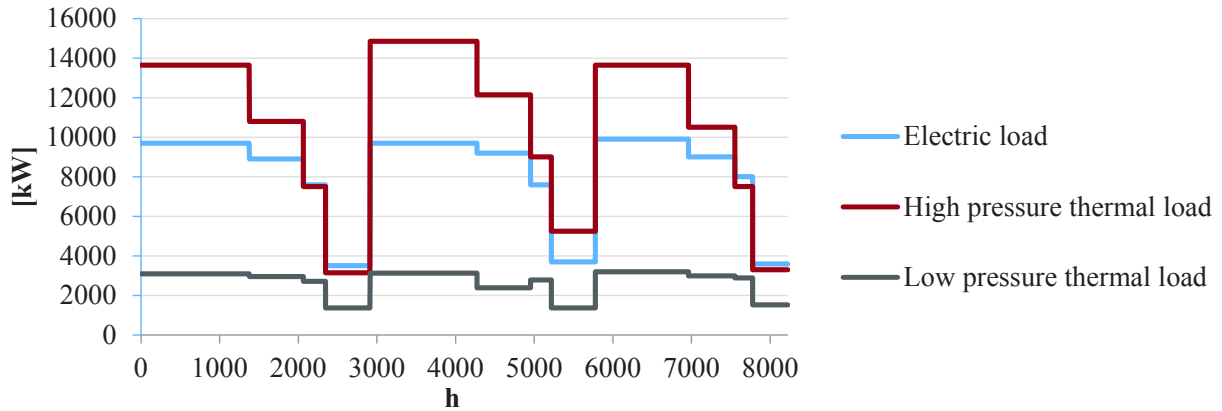
## 435 **5. Examples of application of the methodology developed to case studies**

436 The developed methodology has been applied to two different case studies in order to understand  
437 the modification that can be obtained with respect to conventional design. These two different  
438 applications make it possible to investigate the effectiveness of the two-design methodologies  
439 described in Fig. 4. In the first case the optimum design is carried out at the upper level: “system  
440 level”. The optimal configuration to be implemented is investigated as a function of an electrical  
441 load and two different thermal loads. This makes it possible to address the issue of the choice of the  
442 optimal plant configuration of a hypothetical plant able to satisfy a given load. The second case  
443 moves the analysis to a “nominal design level”: the limits of the operation adopted in an existing  
444 plant are discussed, proposing solutions for the modulation according to the thermal load.

445

### 446 **5.1. First case study: analysis at the system level applied to the design of a medium to high size** 447 **new plant**

448 The plant under analysis is a typical CHP plant in which electricity and thermal load can be  
449 previously defined. Concerning the thermal load, two users are present: a first identifiable as a  
450 district heating network, with associated thermal demand at medium to low temperature (water at  
451 90 °C), and an industrial user, characterized by a thermal demand in the form of medium and high  
452 pressure steam and by electric power requirements. Knowing the various electrical and thermal load  
453 assumed over a reference period corresponding to about one year as represented in Fig. 6, the  
454 problem of design has been studied from the point of view of determining the number and type of  
455 cogeneration units and the auxiliary boiler. In the actual configuration the plant is based on a CHP  
456 unit with a GT system for electricity production with a heat recovery system and an auxiliary boiler  
457 for the production of thermal energy surplus. In a considerable part of the operating time, the  
458 auxiliary boiler is in operation and this component is responsible for a great amount of exergy  
459 losses.



460  
461 **Fig. 6. Thermal and electrical load trend during the operating time of approximately one year**  
462

463 The objective of the optimum design process based on the application of the optimum design  
464 procedure described in section 4.1 is the maximization of the operating share of CHP. In this  
465 perspective it can be possible to consider the possible elimination or the reduction of the size and of  
466 the operating time of the auxiliary boiler. The following step of the optimum design procedure  
467 consists in selecting the available technologies that can be used, fall on gas turbine (GT) and steam  
468 turbine (ST), and then identifying the machines, available on the market, of a size suitable for a  
469 quantitative assessment.

470 As described in Fig. 6, the maximum electrical and thermal load required are about 10000 kW and  
471 15000 kW respectively: so this can be considered a medium to high plant. Four types of system  
472 configurations have been analyzed: single GT, double GT, single ST, double ST (for a total of 20  
473 different configurations).

474 Fig. 7 shows the trend of the total costs (represented by the istograms) and of the function F,  
475 represented by the black line, for the different configurations analyzed. It appears clearly that the  
476 best configuration is the one that minimize the total cost and/or maximize the function F: in the case  
477 under analysis is the configuration with two gas turbines of different size: SGT200 + GPB17D).

478 Fig. 8a shows the trend of the electric power produced compared to the electric load, while Fig.8b  
479 shows the trend of the thermal power produced by the cogeneration units and by the auxiliary boiler  
480 compared to the thermal load (graphs relative to the optimal configuration with 2 GT: SGT200 +  
481 GPB17D).

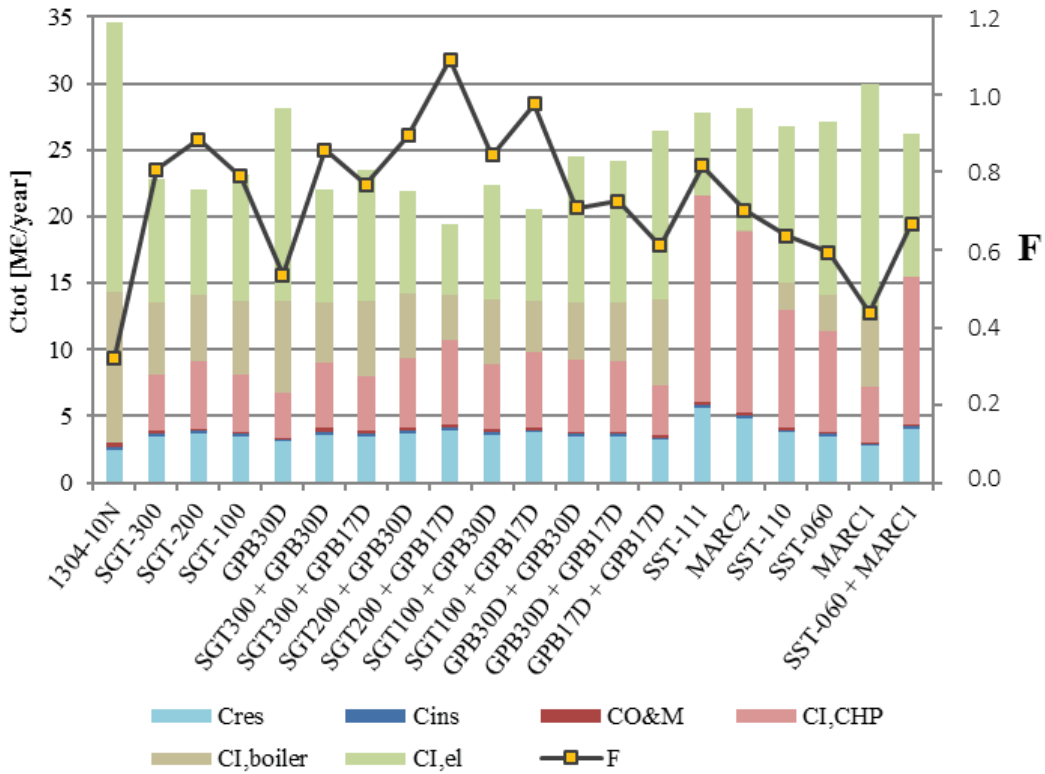


Fig. 7. Results obtained from the methodology applied to the first case study

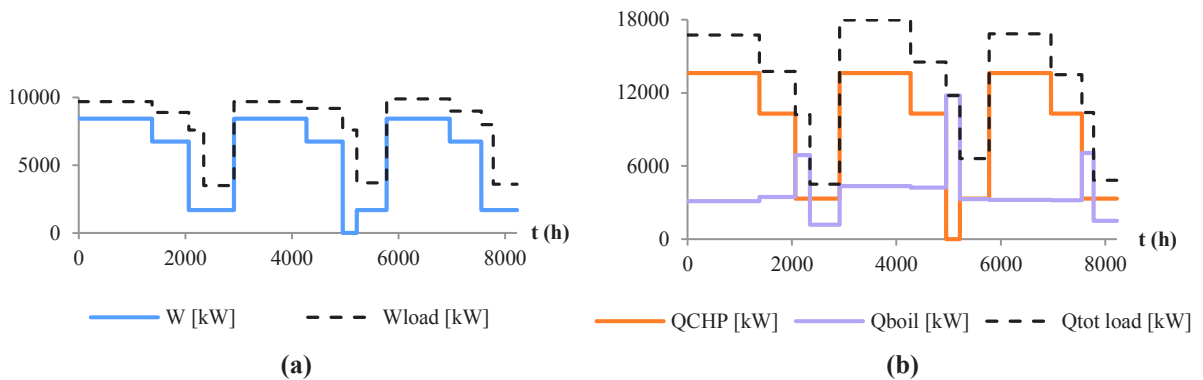
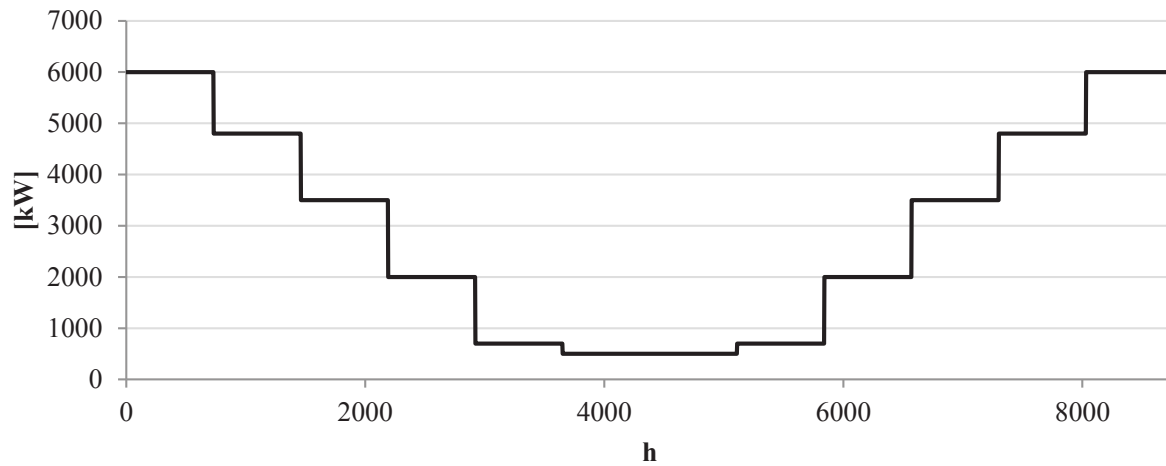


Fig. 8. Load conditions (dashed lines) and satisfaction with CHP and auxiliary boilers during the year

### 5.2. Second case study: analysis at intermediate level applied to an existing plant for the modification of the operational strategy

The second case study concerns an existing CHP plant located in the north area of Italy, powered by biomass and connected to a district heating network. The power plant is a typical CHP plant based on a solution of a steam turbine. Fig. 9 provides the trend of the thermal load during the whole year: it varies from approximately 700 kW during summer time up to 6000 kW (6 MW) during winter.



495  
496 **Fig. 9. Average monthly thermal load hypothesised for the duration of one year**  
497

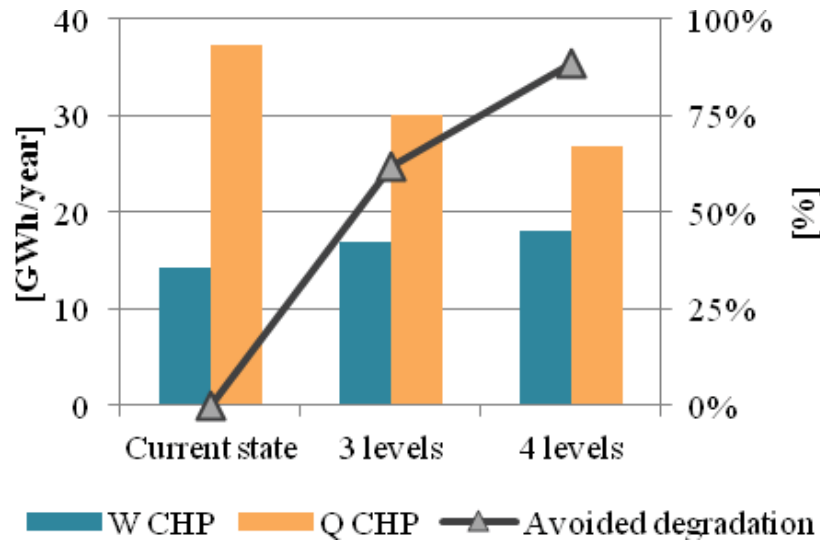
498 In the actual configuration the cogeneration plant is characterized by a steam turbine consisting of a  
499 high pressure and a low pressure section. No auxiliary boiler is used due to the fact that the plant is  
500 designed to be oversized with respect to the maximum thermal load. The modulation, in this case, is  
501 allowed by acting on the flow rate tapped by the high pressure section, with the increase of which  
502 the thermal power available for district heating is increased and the evolving steam flow in the low  
503 pressure section is reduced, and with it electrical production. The total thermal power of the steam  
504 boiler is approximately 12.5 MW, while the maximum electrical production, obtained during  
505 summer time is about 2.9 MW.

506 Two operating conditions are available now: a winter time operation mode (6 MW for DHN and 1  
507 MW of electricity production) and a summer time operation mode (0.8 MW for DHN and 2.9 MW  
508 of electricity production). The plant operates about 3000 hours in “summer mode” and the remaining  
509 5800 hours in “winter mode”. The actual operation of the plant is characterized by a high amount of  
510 irreversibility (exergy losses).

511 Two variants have been proposed for the alternative modulation to the two-level operating logic  
512 adopted today (current status), which is based on a maximum thermal (winter) or maximum electric  
513 (summer) regime and minimum thermal power. The proposed variants introduce one (3 levels) or  
514 two (4 levels) intermediate operating modes acting on the steam flow rate tapped by the turbine and  
515 on the flows circulating in the heat exchanger.

516 The results show that, just introducing one or two additional operating models for the mid-season  
517 operation, it is possible to reduce the irreversibility up to 80% and increase the value assumed by  
518 the F function up to 15% in the best case analyzed with respect to the current operating mode; the  
519 methodology has therefore shown that a simple change in the operation of the plant can bring  
520 significant energy and economic advantages. Fig. 10 shows for example the variation of energy

521 production and degradation considering the possible transition from the current state to a regulation  
 522 based on three or four levels. It is remarkable to say that a regulation based on four levels rather  
 523 than the current one based on only two permits a reduction of the energy degradation up to the 80%  
 524 with respect to the actual level.  
 525



526  
 527 **Fig. 10. Results obtained in terms of avoided energy degradation with respect to the current state with a possible**  
 528 **regulation based on different regulation based on two or three levels load.**

529  
 530

## 531 6. Conclusions

532 The present work has considered the problem of the design of CHP and in particular of CHP-DHN  
 533 for the civil/residential field and has identified possible strategies for increasing the energy  
 534 efficiency of the systems combining the perspectives of the Second Law of Thermodynamics of  
 535 reducing the global irreversibility of the system and the general economic objective of minimizing  
 536 the total operation costs.

537 After examining the studies available in the literature aimed at defining methods for the optimum  
 538 design of these systems, an original method, based on a multi-level and multi-objective perspective  
 539 has been outlined, discussed and analyzed.

540 The method proposes to approach the optimum design of the CHP-DHN system with a general  
 541 perspective considering three possible levels of the system description, starting from top (general  
 542 description) to bottom (more detailed description).

543 The optimum design, at all the levels, can be obtained using a cost function that minimize the  
 544 operational cost of the system, including both economic and energetic elements. The real novelty of  
 545 the methods stands not only in the definition of three levels of description of the system under

546 analysis, but also in the definition of a specific objective function, including a term of penalization  
547 to the irreversibility caused by the operation of the plant.

548 The method can be used both for the optimized design of new plants, knowing the electrical and  
549 thermal load and for modifying existing plants with the modification of existing components (for  
550 example the reduction of size and operational time of auxiliary boilers) or with the introduction of  
551 some additional components (like storage systems) or otherwise just for the definition of the  
552 optimal operating strategy.

553 The method has been tested with reference to two specific cases and even if the analysis is limited  
554 to the two cases discussed, the results expected with the application of the proposed method can be  
555 summarized by the following points:

556

557 - it allows to analyse systems at a reduced level of complexity with come into play many variables  
558 that greatly complicate the analysis;

559 - compared to a conventional economic analysis, it includes in the cost function an item that take  
560 into account the irreversibility deriving from the operation of the system and consequently the  
561 increase of size and operational time of CHP with respect to auxiliary boilers;

562 - if applied to CHP systems, it can represent an effective method for achieving the goal of  
563 obtaining energy efficiency and improvement of economic analysis.

564

565 The central point is the attribution of a cost to energy degradation: the criterion used to determine  
566 the value of this parameter therefore plays a key role in the application of the methodology;

567 A further element that can be extrapolated considering the results of this work is the idea of a  
568 review of incentivisation mechanisms for CHP systems: they could be formulated according to a  
569 multi-objective vision, resorting no longer to individual performance indicators, ineffective in  
570 describing a plant comprehensively, but trying to identify, on the basis of multiple objectives, a  
571 number and a typology of indicators such as to constitute, if properly combined, a good criterion for  
572 the valorisation of truly efficient solutions and for a correct allocation of economic supports.

573

574

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