

## Article

# Design of a $H_\infty$ Robust Controller with $\mu$ -Analysis for Steam Turbine Power Generation Applications

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**Abstract:** Concentrated Solar Power plants are complex systems subjected to quite sensitive variations of the steam production profile and external disturbances, thus advanced control techniques that ensure system stability and suitable performance criteria are required. In this work, a multi-objective  $H_\infty$  robust controller is designed and applied to the power control of a Concentrated Solar Power plant composed by two turbines, a gear and a generator. In order to provide robust performance and stability in presence of disturbances, not modeled plant dynamics and plant-parameter variations, the advanced features of the  $\mu$ -analysis are exploited. A high order controller is obtained from the process of synthesis that makes the implementation of the controller difficult and computational more demanding for a Programmable Logic Controller. Therefore, the controller order is reduced through the Balanced Truncation method and then discretized. The obtained robust control is compared to the current Proportional Integral Derivative-based governing system in order to evaluate its performance, considering unperturbed as well as perturbed scenarios, taking into account variations of steam conditions, sensor measurement delays and power losses. The simulations results show that the proposed controller achieves better robustness and performance compared to the existing Proportional Integral Derivative controller.

**Keywords:** Concentrated Solar Power plants; steam turbine; robust control; H-infinity; structured singular value; Proportional Integral Derivative controller

## 1. Introduction

The interest in the use of renewable energy sources has grown significantly in the recent years, since the supply of fossil hydrocarbon resources is decreasing as a consequence of the growing energy demand, but especially due to the ever increasing need to reduce the relevant environmental impact of fossil-based energy systems. Solar energy is the energy source with the greatest potential of all the renewable sources [1] and it can be harvested and stored for power generation. There are two mainstream categories of devices utilized for this purpose: Photovoltaics (PV) and Concentrated Solar Power (CSP) plants. This last category is gaining an ever-increasing diffusion worldwide [2], as it offers great efficiency and is amongst the most promising cost-effective technologies for renewable electricity energy production [3].

A CSP plant generates electrical power by using different kind of technologies [4] (e.g., parabolic trough, solar towers, etc.) to concentrate a large area of solar thermal energy onto a small area of collecting surface, which exploits such energy to generate steam. Electric power is generated by means of a steam turbine connected to an electrical power generator. The main peculiarity of the application

of steam turbines in CSP lies in the fact that the available solar energy shows considerable variations and oscillations due to the daily cycle of irradiation and to the weather conditions. In particular, the power generation unit may undergo a start-up and shut down cycle on a daily basis and quite sensitive variations in the steam production profile are possible during the day. The possibility of incorporating thermal energy storage or backup systems in the plant [5] and non-standard control techniques allows operating continuously.

Steam turbines were originally designed for producing energy from fossil fuels: their mechanics and their control systems are designed assuming a quite stable steam production and few start-up and shut down cycles. Therefore, the standard control techniques currently applied to turbomachinery, which are exploited also for CSP plants, are often unable to automatically adapt to changing operating conditions and cannot guaranteed the desired performance [6]. Control system parameters are set during the commissioning phase of the brand-new machine, through time consuming and effort-intensive procedures. Afterwards, such parameters are only seldom re-adjusted based on semi-heuristic procedures. This implies the machine to work in non-optimal efficiency conditions during its lifetime. The control procedures need to allow correct and efficient operation of the turbomachine also in transient conditions and without compromising its integrity.

CSP plants exhibit large variations of steam features, nonlinearities, different sources of uncertainties, characteristics that result in detuned performance with classical Proportional Integral Derivative (PID) control [2]. Hence, the main purpose of this work is to study the application of advanced control techniques that can cope with these issues, focusing on CSP plants application and typical power loading profile. The turbine control with variable operating conditions can be addressed by investigating the applicability of several advanced control strategies. Adaptive control approaches, which are capable to adapt gains in different loading conditions and uncertainties are known. Examples of these kind of strategies were presented in [7], where a Model-Reference Adaptive Controller (MRAC) was applied to a non-linear boiler-turbine unit with parametric uncertainties, and in [8], where an improved adaptive backstepping method was designed to control a turbine speed governor system with parametric uncertainties and exogenous disturbances. In the field of robust control,  $H_\infty$  control has received relevant attention in the scientific and technical community and has been widely used for industrial applications. Through its design philosophy, the  $H_\infty$  approach improves in an optimal way the robustness of the control system. Examples of  $H_\infty$  robust controller based on loop-shaping or mixed-sensitivity design were proposed in recent studies [9,10]. In particular, two robust  $H_\infty$  Multiple-Input Single-Output (MISO) controllers were developed and designed by setting out a mixed sensitivity problem in [9], while an output tracking control system for improving the load-following capability of a boiler-turbine unit by using feedback linearization and loop-shaping  $H_\infty$  method was presented in [10]. An application of  $H_\infty$  control technique coupled with the structured singular value  $\mu$  analysis and synthesis was presented in [11]. In [12] an  $H_\infty$  controller was applied to a boiler-turbine system modelled through Fuzzy technique. Predictive control approaches have been investigated in [13], where a linear Model Predictive Control (MPC) controller was proposed for a derived nonlinear model of a steam turbine solar power plant, and in [14], where the General Predictive Control (GPC) and Constrained Receding-Horizon Predictive Control (CRHPC) were exploited for the control of large steam turbines during load variations. In addition, intelligent control approaches were addressed through the control of steam turbines. For instance, in [15,16] fuzzy logic was used in order to adjust on-line the gains of a PID controller. In [15], a steam turbine governing system was controlled through a non-linear self-adaptive fuzzy PID controller adopting fuzzy rule and inference to adjust the PID parameters, while in [16] a fuzzy gain scheduled proportional and integral was applied to the power plant. In [17], a feed-forward controller, whose core is a neuro-fuzzy-based Hammerstein model, was employed to control a boiler-turbine unit and artificial intelligence (AI) methods were adopted in [18–20] in order to adjust the parameters of a PID controller. In particular, fuzzy, Genetic Algorithms (GA), Particle Swarm Optimization (PSO), and Adaptive Neuro-Fuzzy Inference System (ANFIS) techniques were compared in [18], PSO was used in [19], PSO combined

with radial basis function neural networks (RBFNN) algorithms were exploited in [20] and GA were applied in [21]. In addition, Model-Based Control (MBC) schemes, such as Feedback Linearization and Linear Quadratic Regulator (LQR) were investigated for the control of a two-stage steam turbine [22], and Internal Model Control (IMC) with a cascade PID controller was adopted in order to control the superheated steam temperature system [23]. All control techniques provide good results in turbine power applications. Methods like adaptive control or MPC have the main drawback of a considerable computational cost due to their variable structure. A fuzzy logic controller, which extends the simplicity of PID and adapts the control action at actual operating condition using knowledge and experience on the system behavior, has already been developed in [24]. Robust control was selected, as it provides a parametric solution in presence of uncertainties, it yields a structure that is easy to implement on a Programmable Logic Controller (PLC) and is characterized by a low computational cost. The controller design can be automated through a numerical procedure by using the available software [25] and it relies on validated linear approximations of the system model, which cover the majority of the operating envelope of the plant itself. A typical drawback of the proposed approach is represented by the controller order, which is typically high. However, it is possible to reduce the order of original controller with moderate degradation of robustness and performance of the feedback system.

This paper presents a multi-objective  $H_\infty$  robust controller implemented with a signal-based approach [26]. The purpose of this work is to show the applicability of the  $H_\infty$  control approach and the structured singular value  $\mu$  tool in the context of renewable energy systems, in particular on the CSP plants. The  $H_\infty$  strategy can be applied to Multiple-Input Multiple-Output (MIMO) systems and allows designing a controller that stabilizes the plant and minimizes a fixed cost function. The signal-based design is similar to mixed sensitivity design and provides tool for incorporating the desired control requirements in the form of well-known frequency response shaping. This technique allows achieving good nominal stability margins and performance in terms of disturbance rejection, set point tracking and limit of the control effort. In order to improve robust stability and robust performance, the structured singular value analysis ( $\mu$ -analysis) [26,27] was performed. The proposed method is compared to the current PID-based governing system. The design of the multi-objective  $H_\infty$  robust controller as well as the simulation tests were performed through the Matlab/Simulink® environment.

## 2. Steam Turbine Power Plant Control System

The complex of turbines considered in the present work is composed by a non-condensing high pressure (HP) steam turbine, coupled with a gearbox, a condensing low pressure (LP) steam turbine, a steam re-heater and a 55 MW electric generator. The system is completed with a condensing system receiving the exhaust steam at the LP turbine outlet and two steam by-pass systems. The governor is the main controller of the steam turbine machine and is responsible of the unit operation. The electro-hydraulic system controls the inlet valves of each turbine. Figure 1 shows a scheme of the involved system.

Many studies have been performed on the modeling of the steam turbine power plants for control, monitoring and optimization purposes. In [28], an overview of models for turbine-governor were analyzed and provided with particular attention to the behavior during the transient operations, to the frequency control and stability. A steam turbine simulation model based on thermodynamic principles and semi-empirical equations was described in [29], where the related parameters were adjusted by applying GA based on experimental data obtained from field experiments for control purposes. A hybrid thermodynamic method and a neural network approach for on-line monitoring applications were recently presented in [30].

The model developed in the present work is focused on the steam turbine power control taking into account the variability in the steam header system of the considered CSP plant application. The power control model is schematically depicted in Figure 2. The generator is synchronized and connected with the grid, the by-pass valves are ramping to closure and the governor must follow

a demand of power ramp. In particular, the power reference is varied from a minimum power value to a maximum one and, finally, achieves the power shutdown value under normal conditions. In this scenario, the overall control system is a cascaded controller mainly composed of an outer power loop and an inner valve stroke loop. The former one has the task to follow a demand of power and to request a control signal demand to the inner loop. This latter one has the task to control the oil pressure of the electro-hydraulic system and to follow a demand of valve stroke.

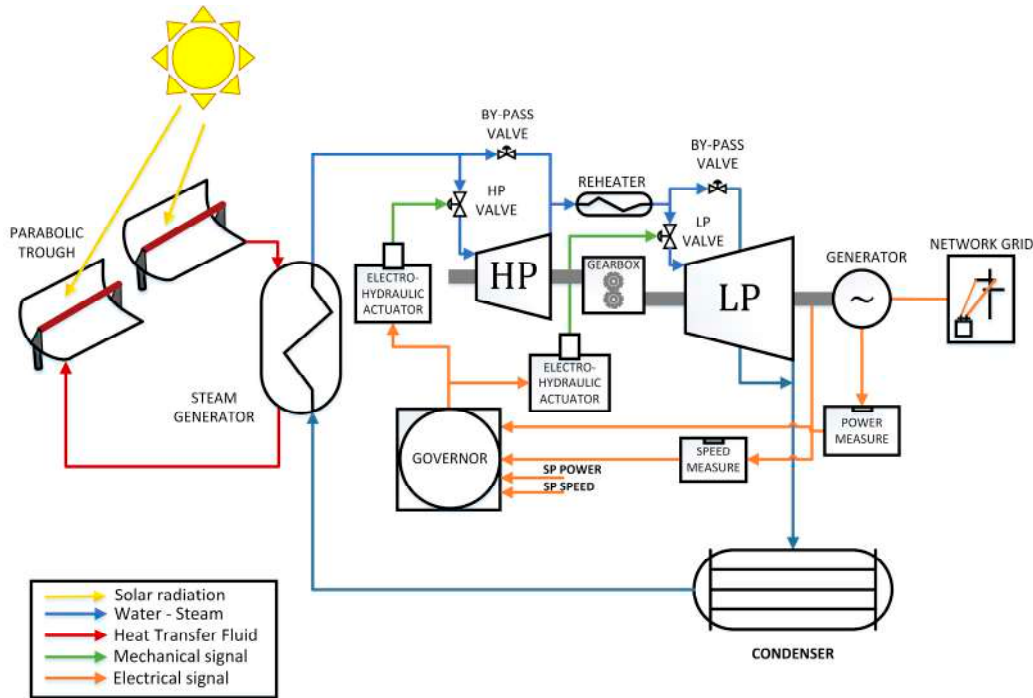


Figure 1. CSP plant schematic diagram considered in the present work.

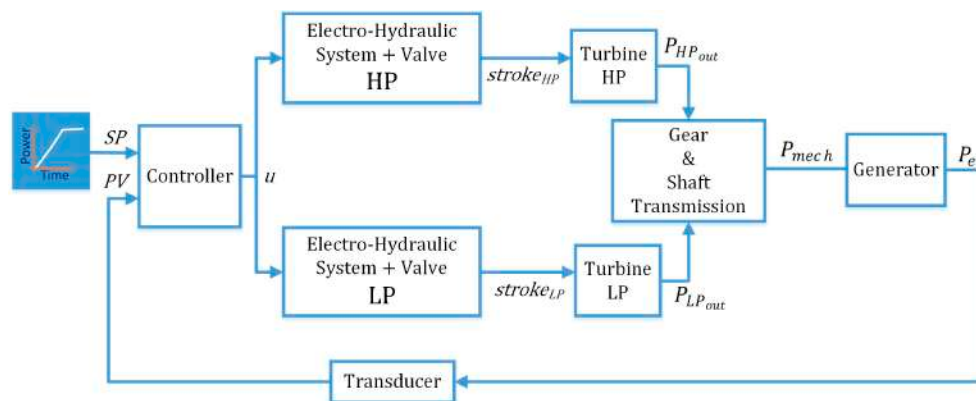


Figure 2. Block-diagram of the power control in the CSP plant.

### 2.1. System Model

The system depicted in Figure 2 was described through a complex non-linear model developed in the Matlab/Simulink® environment. Both the steam turbines models are composed by a block that computes the inlet steam mass flow as a function of control valve stroke, a steam gain  $K_{steam}$ , that provides the characteristics of the flow rate and power of steam, and a friction model, which evaluates the friction power losses  $P_{T_{fric}}$  as function of shaft rotational speed  $\omega$ . Figure 3 shows the Simulink model of both turbines.

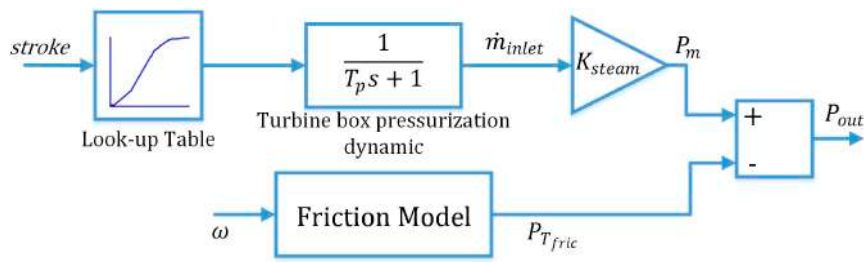


Figure 3. Simplified Simulink model of a turbine.

The inlet steam mass flow  $\dot{m}_{inlet}$  is computed by means of a simplified model with dynamics characterized by a transfer function of the first order and a lookup table calibrated with a steam at rated conditions.  $K_{steam}$  can be expressed as:

$$K_{steam} = \frac{P_{rated}}{\dot{m}_{rated}} k_{actual} \quad (1)$$

where  $k_{actual}$  is a corrective factor that takes into account the actual condition of the steam and its value changes between 0 and 1,  $P_{rated}$  is the rated power and  $\dot{m}_{rated}$  is the maximum steam mass flow.

The turbine mechanical drive power is computed as:

$$P_m = K_{steam} \dot{m}_{inlet} \quad (2)$$

The useful power output  $P_{out}$  can be described as:

$$P_{out} = P_m - P_{T_{fric}} \quad (3)$$

where  $P_{T_{fric}}$  is defined as:

$$P_{T_{fric}} = \frac{P_{b_{loss}}}{\omega_{synchro}^2} \omega^2 \quad (4)$$

with  $P_{b_{loss}}$  being the bearing power losses at the rated synchronous speed  $\omega_{synchro}$ .

The gearbox and the electric generator are modelled by taking into account all the possible additional power losses of the train. The gearbox model computes the balance of the power acting on the LP shaft. In particular, it is assumed that both torques and angular velocities are reported at the same LP shaft. The angular velocity is computed through the balance of both HP and LP turbine torques  $\tau_{HP}$  and  $\tau_{LP}$ , the electric generator torque  $\tau_{GE}$  and the gearbox friction torque  $\tau_{GB}$ ; it is integrated and divided by the total moment of inertia acting on the LP shaft  $J_T$ , according to the Equation (5):

$$J_T \dot{\omega} = (\tau_{HP} + \tau_{LP} - \tau_{GB} - \tau_{GE}) \quad (5)$$

where:

$$J_T = J_{GB} + J_{HP} + J_{LP} + J_{GE}$$

The gearbox friction torque  $\tau_{GB}$  is equal to the sum of two contributions, one due to windage and bearing friction  $\tau_{wb}$  and the other one due to full load power losses  $\tau_{load}$ , and is computed as:

$$\tau_{GB} = \tau_{wb} + \tau_{load} = \frac{P_{wb_{loss}} \omega}{\omega_{synchro}^2} + \frac{P_{f_{loss}} - P_{wb_{loss}}}{\tau_{HP_{Max}} \omega} \tau_{HP} \quad (6)$$

where  $P_{wb_{loss}}$  are the rated windage and bearing power losses,  $P_{f_{loss}}$  are the full load power losses and  $\tau_{HP_{Max}}$  is the maximum value reached by the HP turbine torque. The electric generator model



computes the generated electric power  $P_e$  as the useful mechanical power at generator shafts minus the gearbox power losses  $P_{GB_{fric}}$  and electrical and mechanical losses on the electrical generator  $P_{GE_{losses}}$ :

$$P_e = P_{HP_{out}} + P_{LP_{out}} - P_{GB_{fric}} - P_{GE_{losses}} \quad (7)$$

The complex hydraulic parts of both HP and LP electro-hydraulic actuators and related valves were modelled with the Simscape Toolbox of Matlab®/Simulink. The electro-hydraulic system is composed by a current to pressure converter (CPC), which controls the hydraulic pilot cylinder (HPC) movements. The HPC allows the passage of the volume oil flow to the chamber of the hydraulic double acting cylinder (HDAC), which controls the input valve position of the steam turbines. A detailed scheme of the electro-hydraulic system is depicted in Figure 4. The parameters of the hydraulic components modeled were derived from schemes and datasheets provided by General Electric Oil & Gas.

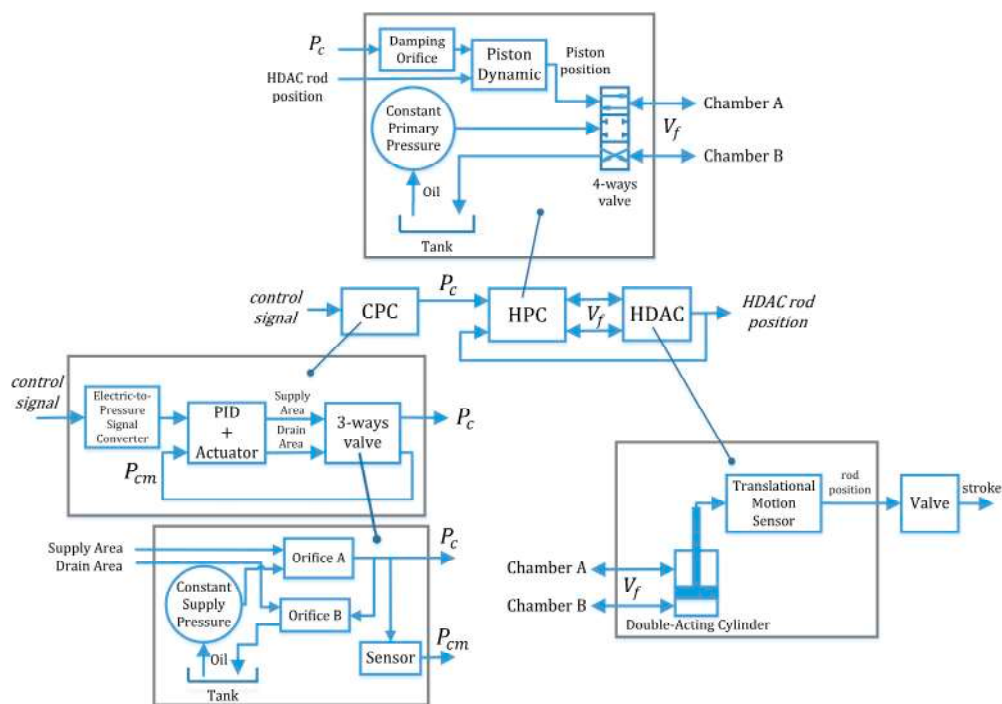


Figure 4. Detailed Simulink model of the electro-hydraulic system.

The Governor is a non-standard Proportional-Integral (PI) controller, hereafter also called PID Governor, with the task of following a demand of power and to request a control signal demand to the actuators. The controller software is property of General Electric Oil & Gas and has the following three main features:

1. An anti-windup obtained by differential formulation of the integral component.
2. limiter in the output.
3. proportional gain involved as well in the integral component calculation.

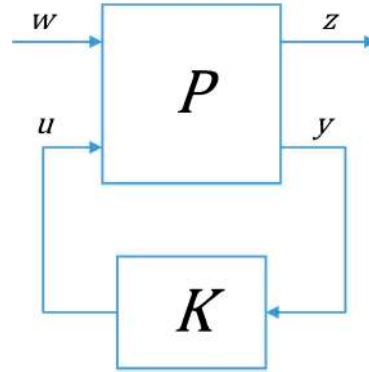
Finally, power transducers and filters are also represented by transfer functions.

### 3. $H_\infty$ Controller for Steam Turbine Power Control

For the power control loop, a multi-objective  $H_\infty$  robust controller was selected and implemented. In this section, the  $H_\infty$  robust control problem statement and design are presented.

### 3.1. Problem Statement

Let us consider the general plant represented by the transfer matrix  $P(s)$  and the control system configuration shown in Figure 5.



**Figure 5.** General closed-loop interconnection.

The plant  $P(s)$  has two inputs and two outputs:

- the generalized disturbance  $w$ , which cannot be affected by the controller  $K(s)$  and includes references, disturbances and noise signals;
- the output signal of the controller  $u$  called control input;
- the input signal of the controller  $y$  called measurement output;
- the controlled variable  $z$ , which denotes the performance requirements.

The open loop interconnection can be generally described by the equations system:

$$\begin{pmatrix} z \\ y \end{pmatrix} = P(s) \begin{pmatrix} w \\ u \end{pmatrix} = \begin{bmatrix} P_{11} & P_{12} \\ P_{21} & P_{22} \end{bmatrix} \begin{pmatrix} w \\ u \end{pmatrix} \quad (8)$$

where  $P(s)$  is partitioned in 4 main subsystems.

The closed-loop system is given by the Lower Linear Fractional Transformation (LLFT) of  $P(s)$  and  $K(s)$ , denoted by  $F_l(P, K)$ :

$$z = F_l(P, K)w = T_{zw}(s)w = [P_{11} + P_{12}K(I - P_{22}K)^{-1}P_{21}]w \quad (9)$$

The  $H_\infty$ -optimal control problem [26] consists in finding all stabilizing controller  $K(s)$  that minimize the cost function:

$$J_\infty(K) = \|F_l(P, K)\|_\infty \quad (10)$$

where  $\|\cdot\|_\infty$  is the  $H_\infty$ -norm defined as:

$$\|T_{zw}(s)\|_\infty := \max_{\omega \in \mathbb{R}} \bar{\sigma}[T_{zw}(j\omega)] \quad (11)$$

with  $\bar{\sigma}$  the maximum singular value of  $T_{zw}(j\omega)$ . The direct minimization of  $J_\infty(K)$  is a very hard problem and finding the optimal controller is difficult; therefore a sub-optimal problem is solved and conditions to ensure the existence of a stabilizing controller are found. Let  $\gamma_{min}$  be the minimum value of  $J_\infty(K)$  over all stabilizing controllers  $K$ . The sub-optimal problem consists in finding all stabilizing controller  $K(s)$  such that  $\|T_{zw}(s)\|_\infty < \gamma$ , for a given  $\gamma > \gamma_{min}$ . There are two main methods for solving this sub-problem:

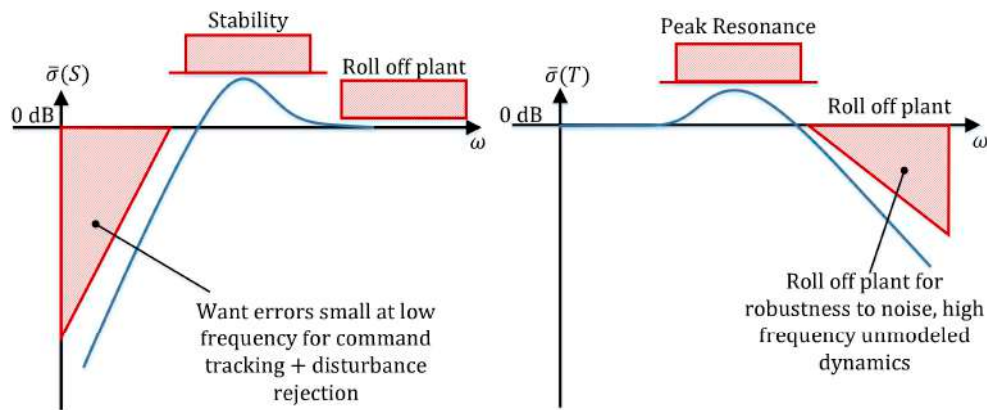
1. Riccati equations approach.





These requirements may be combined into an  $H_\infty$ -problem, which is defined as:

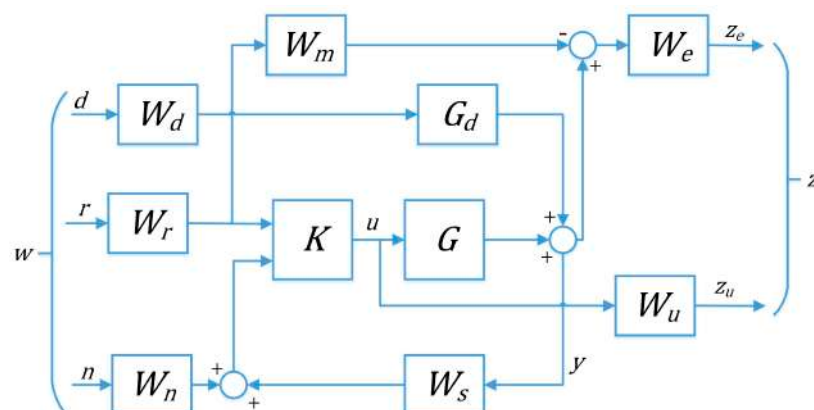
$$J_{\infty}(K) = ||F_l(P, K)||_{\infty} = \left\| \begin{bmatrix} W_1 S \\ W_2 T \\ W_3 R \end{bmatrix} \right\|_{\infty} \quad (15)$$



**Figure 7.** Singular value frequency response performance requirements for sensitivity and complementary sensitivity functions (taken from [34] with permission).

Instead of shaping the basic transfer functions, it is possible to work with the so-called signal-based approach [26] shown in Figure 8. The meaning of the weights are as follows:

- $W_d$  forms the frequency content and magnitude of the exogenous disturbance affecting the plant.
- $W_r$  shapes the magnitude and the frequency of the reference command.
- $W_n$  represents the frequency-domain models of sensor noise.
- $W_m$  represents the desired model for the closed-loop system with tracking.
- $W_e$  shapes the tracking error.
- $W_u$  forms the frequency content and magnitude of the control signal use.
- $W_s$  represents the model of the sensor dynamics. This model might also be lumped into the plant model  $G$ .



**Figure 8.** Signal-based  $H_\infty$  control problem.

It is straightforward to show that:

$$\begin{bmatrix} z_e \\ z_u \end{bmatrix} = \begin{bmatrix} W_e(S_o GK - W_m)W_r & W_e(S_o G_d)W_d & -W_e(S_o GK)W_n \\ W_u(S_i K)W_r & -W_u(S_i KW_s G_d)W_d & -W_u(S_i K)W_n \end{bmatrix} \begin{bmatrix} r \\ d \\ n \end{bmatrix} \quad (16)$$

$$J_\infty(K) = \left\| \begin{bmatrix} W_e(S_o GK - W_m)W_r & W_e(S_o G_d)W_d & -W_e(S_o GK)W_n \\ W_u(S_i K)W_r & -W_u(S_i KW_s G_d)W_d & -W_u(S_i K)W_n \end{bmatrix} \right\|_\infty \quad (17)$$

with  $S_o = (I + GKW_s)^{-1}$  and  $S_i = (I + KW_s G)^{-1}$ .

This objective is similar to the usual mixed  $S/R$  sensitivity optimization. The weighting functions are used to scale the input/output transfer functions such that  $\|T_{zw}(s)\|_\infty \leq 1$ .

### 3.3. Linear Model Description

For the control purposes, a linear approximation model of the system was considered. Taking into account the model developed in the Section 2.1, the linear model was obtained with the following assumptions:

- Offsets as well as saturations were eliminated.
- A linear model of the electro-hydraulic system with the valve of both HP and LP turbine was identified and introduced as transfer function. Since the dynamic of the system must take into account several dynamic components and the delay due to the oil flow, the system was identified with a fourth-order, stable and not minimum phase transfer function with the structure:

$$\bar{G}_{Ai} = \frac{b_1 s + b_0}{s^4 + a_3 s^3 + a_2 s^2 + a_1 s + a_0} \quad (18)$$

The presence of a nonminimum phase zero in (18) limits the amplification of the loop gain and the general performance. This is however independent of the controller used.

The goodness of fit between the linear and the real model was valued using the Normalized Root Mean Square Error (NRMSE) cost function defined as follows:

$$NRMSE = 100 \left( 1 - \frac{\|y - \hat{y}\|}{\|y - \left( \frac{1}{N} \sum_{i=1}^N y_i \right)\|} \right) \quad (19)$$

where  $\|\cdot\|$  is the 2-norm of a vector,  $y$  is the vector of the real model output subjected to different input step command and  $\hat{y}$  is the vector of the estimated model output.

- The nonlinearities introduced by the look-up tables were replaced by constant gains defined as the ratio between the maximum inlet steam mass flow  $\dot{m}_{rated}$  and the maximum stroke valve:

$$K_\alpha = \frac{\dot{m}_{rated}}{stroke_{Max}} \quad (20)$$

The linear model of the system is depicted in Figure 9, where  $K$  represents the transfer function of the controller, and  $G_i$  the transfer functions of the main elements of the turbine power system.

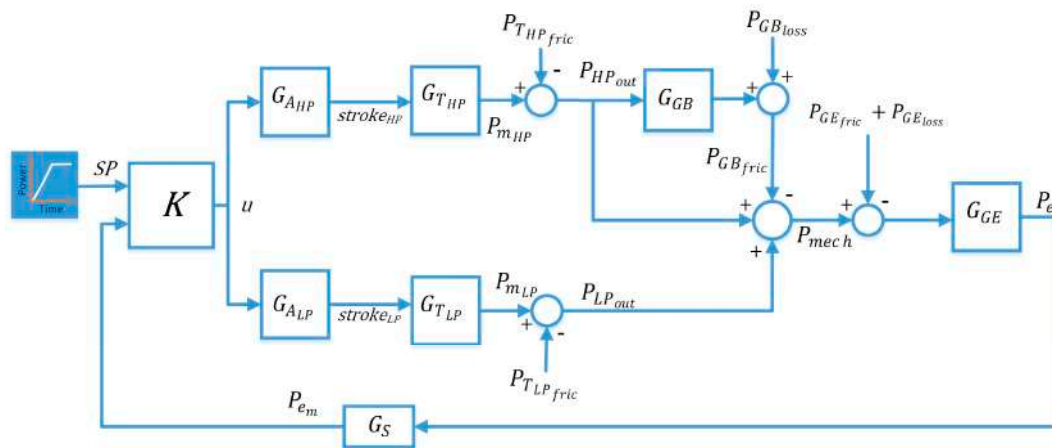


Figure 9. Block-diagram of the power control in the CSP plant linear model.

### 3.4. Derivation of Uncertainty Model

The design of robust control methods allows the incorporation of uncertainties in the plant model. Not modeled dynamics of actuators, sensors and turbine plant-parameter variations are the common uncertainties of the system. In the next subsections a representation of these kind of uncertainties is presented, for the process considered in this work.

#### 3.4.1. Actuator System Uncertainties

In order to take into account the unmodeled dynamics of the valves actuation system, the uncertainties in the actuator models are approximated by input multiplicative uncertainties as shown in Figure 10.

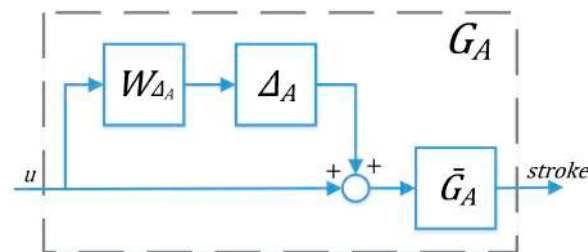


Figure 10. Actuator with input multiplicative uncertainty.

The perturbed system is described as:

$$G_A = \bar{G}_A (I + W_{\Delta_A} \Delta_A) \quad (21)$$

where  $\bar{G}_A$  is the nominal transfer function of the electro-hydraulic system with valve (Equation (18)),  $\Delta_A$  the unknown uncertainty stable and norm bounded ( $\|\Delta_A\|_\infty \leq 1$ ) and  $W_{\Delta_A}$  the weight uncertainty defined as:

$$W_{\Delta_A} = a \frac{s + \alpha k}{s + \alpha a} \quad (22)$$

The unmodeled dynamics uncertainty is somewhat less precise and thus more difficult to quantify. Therefore, the simplified form of the previous equation is usually adopted [26], where the value  $k$  represents the percentage of the modelling error at low frequency while  $a$  the percentage error at high frequency. The 100% uncertainty in the model occurred when the weight function achieves a magnitude value of 1, approximately at the value of  $\alpha$ . The weighting functions considered here were

derived according to the nominal transfer function and the bandwidth of the actuators, taking into account a good model of these latter ones at low frequency. The multiplicative weights are described as:

$$W_{\Delta_{A_{HP}}} = 2 \frac{s + 0.9}{s + 36} \quad (23)$$

$$W_{\Delta_{A_{LP}}} = 2 \frac{s + 0.85}{s + 34} \quad (24)$$

### 3.4.2. Turbine Parameter Uncertainties

The main parameter variation of the turbines is due to the actual condition of the steam. It is related to the heat profile during the day. The variation of the steam condition  $k_{actual}$  can be represented by a parametric uncertainty:

$$k_{actual} = \bar{k}_{actual} (1 + \rho_{\delta_k} \delta_k) \quad (25)$$

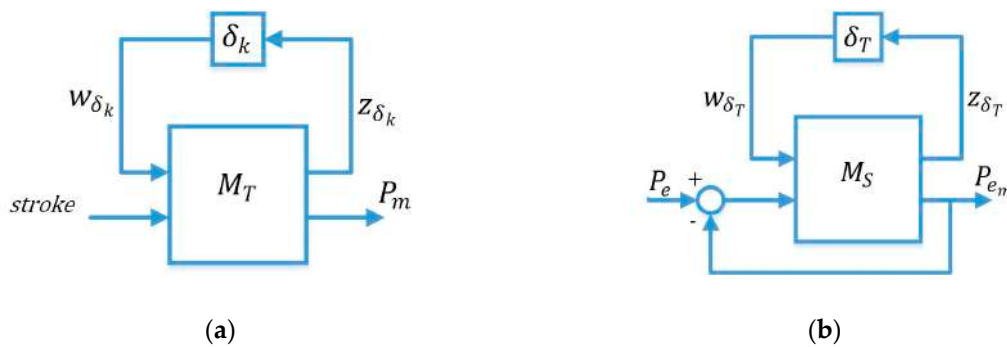
where  $\bar{k}_{actual}$  is the nominal value,  $\rho_{\delta_k}$  represents the percentage of variation and  $\delta_k$  is a real parameter bounded ( $|\delta_k| \leq 1$ ). It was observed from the experimental data that, in a typical day where the weather conditions are quite good, the turbine power is on average 70%, and for the 80% of the time, the power lies in the range [50%, 100%]. Therefore, the values 0.77 and a 30% were selected for  $\bar{k}_{actual}$  and  $\rho_{\delta_k}$  for HP and LP turbines, respectively.

A representation of the turbine block with separated uncertain parameter using the Upper Linear Fractional Transformation (ULFT) of  $M_T$  and  $\delta_k$ , denoted by  $F_u(M_T, \delta_k)$ , is shown in Figure 11a, where

$$P_m = F_u(M_T, \delta_k) stroke = [M_{T22} + M_{T21} \delta_k (I - M_{T11} \delta_k)^{-1} M_{T12}] stroke \quad (26)$$

with:

$$M_T = \begin{bmatrix} M_{T11} & M_{T12} \\ M_{T21} & M_{T22} \end{bmatrix} = \begin{bmatrix} 0 & \frac{K_R \frac{P_{rated}}{\dot{m}_{rated}} \bar{k}_{actual}}{T_p s + 1} \\ \frac{K_R \frac{P_{rated}}{\dot{m}_{rated}} \bar{k}_{actual}}{T_p s + 1} & \rho_{\delta_k} \frac{K_R \frac{P_{rated}}{\dot{m}_{rated}} \bar{k}_{actual}}{T_p s + 1} \end{bmatrix}$$



**Figure 11.** (a) Turbine model with uncertainty parameter pulled out; (b) Sensor model with uncertainty parameter pulled out.

### 3.4.3. Sensor Parameter Uncertainties

The time constant of the sensor is another uncertain parameter of the actual system. The inaccuracy of the sensor time constant  $T_s$  can be represented by a parametric uncertainty:

$$T_s = \bar{T}_s (1 + \rho_{\delta_T} \delta_T) \quad (27)$$

where  $\bar{T}_s$  is the nominal value,  $\rho_{\delta_T}$  represents the percentage of variation and  $\delta_T$  is a bounded real parameter ( $|\delta_T| \leq 1$ ). It was observed from the site data that the data transmission delay lies between

0.5 and 1.5 s. Thus a value of 1 and a 50% of tolerance were chosen for  $\overline{T_s}$  and  $\rho_{\delta_T}$ , respectively. Clearly, the amount of tolerance used may produce a more conservative design, but this is coherent with typical worst case operating point(s) used in classical PID control.

A representation of the sensor block with separated uncertain parameter using the ULFT is shown in Figure 11b, where:

$$P_{e_m} = F_u(M_S, \delta_T)(P_e - P_{e_m}) \quad (28)$$

with:

$$M_S = \begin{bmatrix} M_{S11} & M_{S12} \\ M_{S21} & M_{S22} \end{bmatrix} = \begin{bmatrix} -\rho_{\delta_T} & \frac{1}{\overline{T_s}} \\ -\rho_{\delta_T} & \frac{1}{\overline{T_s}} \end{bmatrix}$$

### 3.5. Performance Specifications

The designed control system must achieve good disturbance rejection and noise attenuation, as well as good tracking error; therefore, performance weights must be selected. Finding appropriate weighting functions is a crucial step in robust control design: there must be a trade-off between the nominal performance and robust performance of the closed loop system and their selection usually involves trial and error procedures.

A signal-based approach was adopted for the  $H_\infty$  optimization and the following main weight functions were defined:

- $W_d$  forms the frequency content and magnitude of the exogenous disturbance affecting the plant.
- $W_n$  represents the frequency domain model of the sensor noise.
- $W_m$  is an ideal model of performance, to which the designed closed-loop system tries to match.
- $W_u$  represents the control action constraint.
- $W_a$  introduces the constraints on the maximum stroke of both HP and LP valve.
- $W_e$  shapes the error between the response of the close-loop system and the ideal model  $W_m$ .

Figure 12 shows the block diagram of the closed-loop system, which includes the feedback structure and the controller as well as the elements representing the model uncertainties (highlighted in green) and the performance objectives (highlighted in orange).

The generalized disturbance  $w$  of the system consists of the reference input ( $r$ ), the input disturbance ( $d$ ), and the noise ( $n$ ), while the vector of performance requirements  $z$  is composed by the control variables  $z_u$ ,  $z_a$  (is a vector of two components) and  $z_e$ :

$$w = \begin{bmatrix} r \\ d \\ n \end{bmatrix}, z = \begin{bmatrix} z_u \\ z_a \\ z_e \end{bmatrix} \quad (29)$$

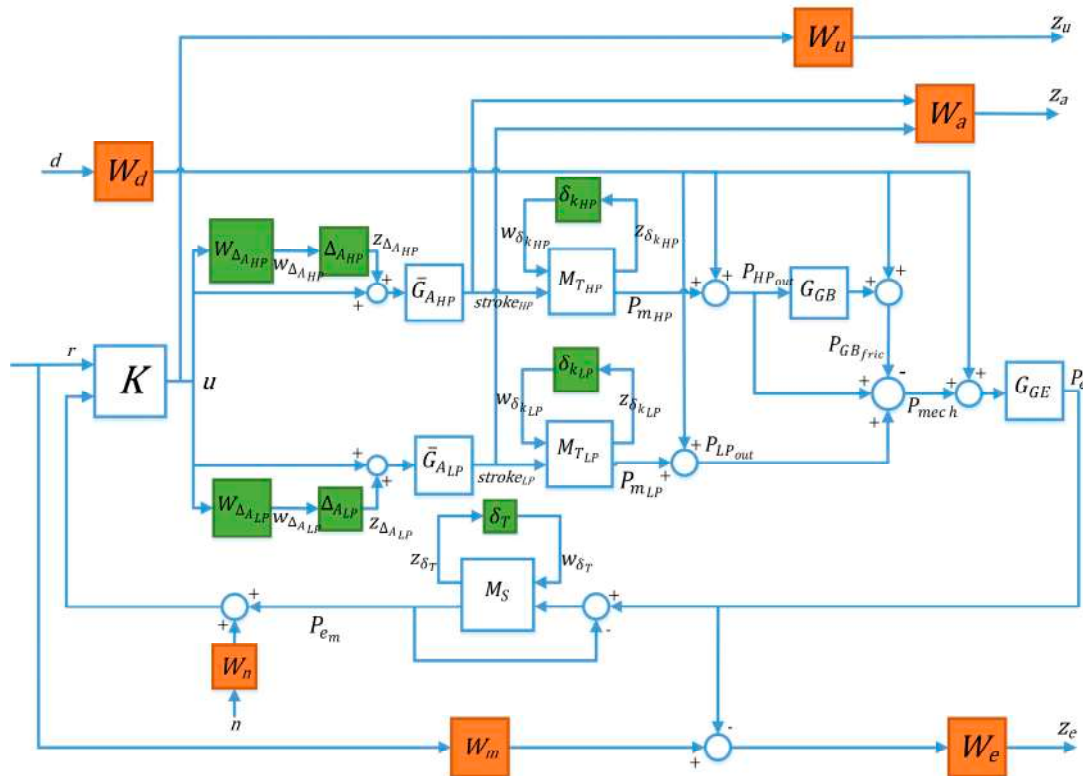
The system uncertainties can be separated from the model and grouped into a diagonal structured block  $\Delta$  norm bounded  $\|\Delta\|_\infty \leq 1$  with input  $z_\Delta$  and output  $w_\Delta$ :

$$\Delta = \begin{bmatrix} \Delta_{A_{HP}} & 0 & 0 & 0 & 0 \\ 0 & \Delta_{A_{LP}} & 0 & 0 & 0 \\ 0 & 0 & \delta_{k_{HP}} & 0 & 0 \\ 0 & 0 & 0 & \delta_{k_{LP}} & 0 \\ 0 & 0 & 0 & 0 & \delta_T \end{bmatrix}, z_\Delta = \begin{bmatrix} z_{\Delta_{A_{HP}}} \\ z_{\Delta_{A_{LP}}} \\ z_{\delta_{k_{HP}}} \\ z_{\delta_{k_{LP}}} \\ z_{\delta_T} \end{bmatrix}, w_\Delta = \begin{bmatrix} w_{\Delta_{A_{HP}}} \\ w_{\Delta_{A_{LP}}} \\ w_{\delta_{k_{HP}}} \\ w_{\delta_{k_{LP}}} \\ w_{\delta_T} \end{bmatrix} \quad (30)$$

The signal  $u$  is the controller output, while the input of the controller  $y$  consists of the reference signal  $r$  and the measured electrical power  $P_{e_m}$ , which is affected by noise:

$$y = \begin{bmatrix} r \\ P_{e_m} + n \end{bmatrix} \quad (31)$$

Now, the defined weight functions will be described, and the performance objectives will be discussed in the next section.



**Figure 12.** Block diagram of the closed-loop system with uncertainties and performance specifications.

### 3.5.1. Disturbance Weight Function

In the power control scenario the different power losses are constant and are introduced in the system by the vector weight function  $W_d$ .

$$W_d = \begin{bmatrix} -P_{T_{HP}fric} \\ -P_{T_{LP}fric} \\ P_{G_{B}loss} \\ -P_{G_{E}fric} \\ -P_{G_{E}loss} \end{bmatrix} \quad (32)$$

The input disturbance  $d$  of  $W_d$  was considered as a step signal.

### 3.5.2. Noise and Control Action Weight Functions

The noise shaping function is determined on the basis of the spectral content of the sensor noise signal and usually has its peak value at high frequency because the noise is mainly concentrated at high frequencies. In this context, the noise shaping function was modeled with a constant function  $W_n = 1$  due to the lack of sensor technical data, considering a worst-case design, where the power spectral density of the noise signal is constant for all frequencies. However, the robust control design structure derived with the assumed  $W_n$  can be refined if better statistics become available. The input noise  $n$  of  $W_n$  was considered as a zero mean Gaussian white noise.

In order to avoid actuators saturation, it is necessary to have a control action smaller than a constant value. Therefore, the normalizing weight function  $W_u$  is taken equal to unity.



### 3.5.3. Stroke Valve Weight Function

In order to avoid exceeding the maximum stroke (100%) of both HP and LP valve, constant bounds are introduced by means of the weight function  $W_a$ , which is defined as:

$$W_a = \begin{bmatrix} 1/100 & 0 \\ 0 & 1/100 \end{bmatrix} \quad (33)$$

### 3.5.4. Closed-Loop Ideal Model Weight Function

$W_m$  is an ideal model of performance, which the designed closed-loop system tries to match. The model transfer function is selected so that a set of performance indexes adapted to the input power ramp reference shown in Figure 13 are satisfied. Such indexes are settling time (time elapsed from ramp command start to actual power within  $\pm 5\%$  of target value), rise time (time elapsed from ramp command start to 90% of target value), overshoot (the maximum peak value measured from the target value) and integral absolute error (IAE, evaluated along the entire ramp), which is defined as:

$$IAE = \int_0^{t_f} |e(t)| dt \quad (34)$$

where  $e$  is the tracking error between set point and actual value.

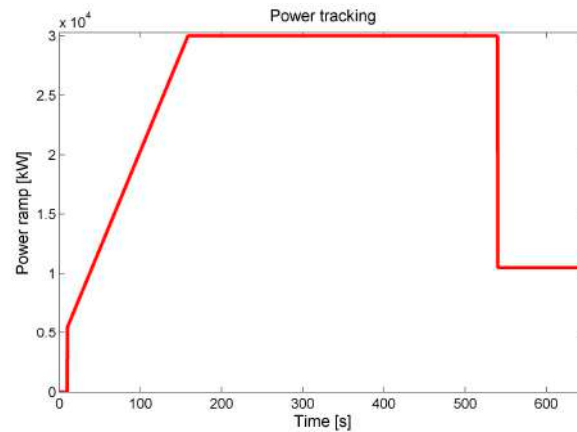


Figure 13. Power ramp reference.

The set-point specifications constraints defined by the company are the following:

- Settling time <141 s
- Rise time <131 s
- Overshoot <2%
- $IAE < 4 \times 10^4$

For a good tracking of reference signal, a second order well-damped system has been selected:

$$W_m = \frac{\omega_n^2}{s^2 + 2\sigma\omega_n s + \omega_n^2} \quad (35)$$

where  $\omega_n$  is a desired natural frequency and  $\sigma$  a desired damping ratio.

A model satisfying the above mentioned requirements is:

$$W_m = \frac{9}{s^2 + 5.1s + 9} \quad (36)$$

### 3.5.5. Tracking Error Weight Function

The difference between the response of the closed loop system and the ideal model  $W_m$  is reflected in the weight function  $W_e$ . The aim of this weight is to achieve a small difference between the system and model output and a small effect of the disturbance on the system output. The form of  $W_e^{-1}$  is usually a high-pass filter [26], but the selection of the appropriate parameters is not simple, as it should represent a trade-off between nominal and robust performance. Therefore, two types of function were tested, namely a transfer function of the first and second order, with one or two zeros, respectively. The performance weighting function expressed by the Equation (37) was obtained through a trial and error approach, evaluating the nominal performance and the robust performance of the control system, and preferring a simple structure:

$$W_e = 5 \times 10^{-5} \frac{s + 3}{s + 3 \times 10^{-4}} \quad (37)$$

If one needs to enforce the performances (e.g., the rise time condition) both numerator and denominator coefficients of  $W_e$  have to be increased by shifting the weighting frequency response toward higher frequency values.

### 3.6. $H_\infty$ Control Synthesis

The controller synthesis problem is to find a linear, output feedback controller  $K(s)$  that has to ensure the following properties of the closed-loop system:

- *Nominal Performance:*

$$\|F_l(P_{nom}, K)\|_\infty \leq 1 \quad (38)$$

where  $P_{nom}$  is the unperturbed open-loop system and  $\|\cdot\|_\infty$  is the  $H_\infty$  -norm.

- *Robust Stability:*

$$\mu_\Delta(M) < 1 \quad (39)$$

for structured uncertainty  $\Delta$  where  $\mu_\Delta(M)$  is the structured singular value, corresponding to the transfer matrix from  $w_\Delta$  to  $z_\Delta$ , the so called matrix  $M$ .

- *Robust Performance:*

$$\mu_{\tilde{\Delta}}(N) < 1 \quad (40)$$

for the structured uncertainty  $\tilde{\Delta}$  where  $\mu_{\tilde{\Delta}}(N)$  is the structured singular value, corresponding to the transfer matrix from  $\begin{bmatrix} w_\Delta \\ w \end{bmatrix}$  to  $\begin{bmatrix} z_\Delta \\ z \end{bmatrix}$ , the so called matrix  $N$ , with regard to  $\tilde{\Delta} = \begin{bmatrix} \Delta & 0 \\ 0 & \hat{\Delta} \end{bmatrix}$  where  $\hat{\Delta}$  is a fictitious  $3 \times 4$  complex uncertainty block.

- *Low-Order Controller:*

$$\min_{K_r(s)} \|K(s) - K_r(s)\|_\infty \quad (41)$$

where  $K(s)$  is the full order controller and  $K_r(s)$  is the reduced order controller.

#### 3.6.1. Nominal Performance Analysis

The  $H_\infty$  sub-optimal problem was solved through the command “hinfyn” of the Robust Control Toolbox of Matlab®. The interval of  $\gamma$ -iteration was chosen between 0.1 and 10 with tolerance 0.01. The synthesized controller has two input and one output and is of 35th order. The value of  $\gamma$  at the end of the  $\gamma$ -iteration is equal to 0.5051 as shown in Figure 14. Therefore, Equation (38) is satisfied and nominal stability and performance are guaranteed. The performance of the controller could be improved acting on the performance weighting functions, but a faster time-response and

consequently, a larger closed-loop system bandwidth, reduce its robust performance, thus the controller was not improved.

```

Test bounds:      0.1000 < gamma <=      0.5394

gamma  hamx_eig  xinf_eig  hamy_eig  yinf_eig  nrho_xy  p/f
0.539  3.0e-04 -4.3e-13  1.1e-04  0.0e+00  0.0001  p
0.320  3.0e-04 -1.5e-16  5.8e-16 #  *****  *****  f
0.430  3.0e-04 -3.4e-12  6.2e-15 #  *****  *****  f
0.485  3.0e-04 -7.6e-12  1.5e-14 #  *****  *****  f
0.512  3.0e-04 -1.5e-12  6.4e-05  0.0e+00  0.0001  p
0.498  3.0e-04 -1.2e-16  6.1e-15 #  *****  *****  f
0.505  3.0e-04 -2.4e-16  4.3e-05  0.0e+00  0.0001  p

Gamma value achieved:      0.5051

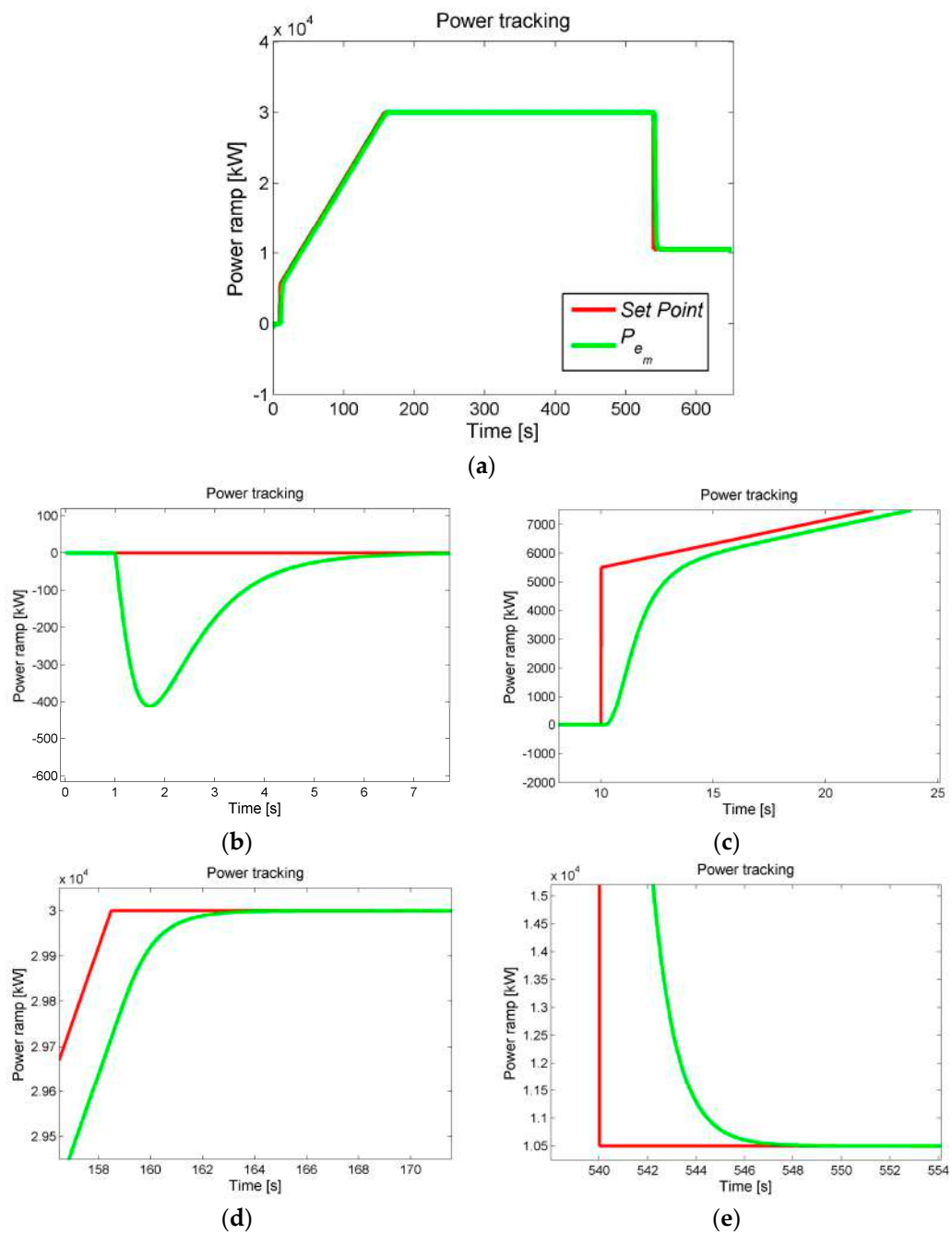
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**Figure 14.**  $\gamma$ -iteration computed through the command “hinfoyn”.

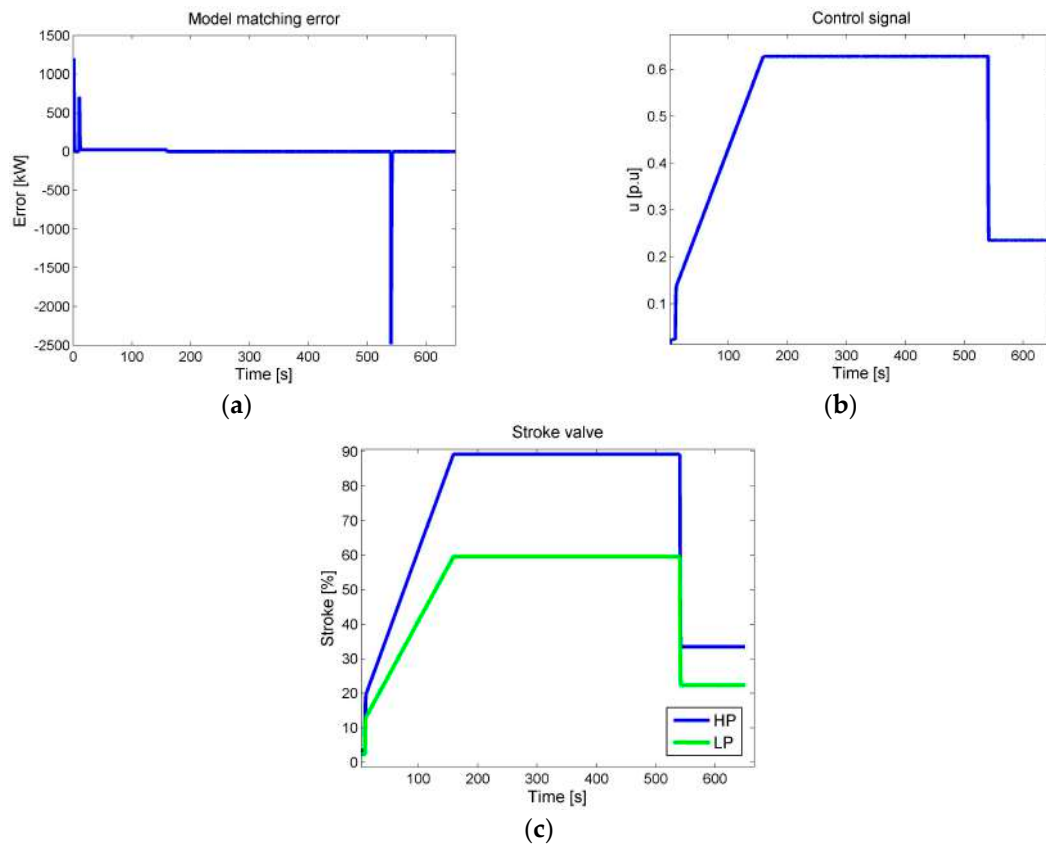
The set-point following performance indexes are synthetized in Table 1. The power tracking of the closed-loop system is shown in Figure 15. The input disturbance in the initial stage of the power ramp is quickly rejected and the reference tracking is good. The behavior of the error when the closed-loop system tries to match the ideal model  $W_m$ , the control action, and the stroke valve of both HP and LP turbine are shown in Figure 16. The model error is small and the constraints on control signal and stroke valves are respected, thus the performance objectives are satisfied.

**Table 1.**  $H_\infty$  controller set-point performance indexes.

Index	Value
Settling time (s)	140.1
Rise time (s)	130.3
Overshoot (%)	0
IAE	$3.5933 \times 10^4$



**Figure 15.** Closed-loop power reference tracking of the nominal system: (a) Complete view; (b) Disturbance rejection in the initial stage; (c) Ramp command start ; (d) Steady-state at 30 MW; (e) Power profile in the final stage.

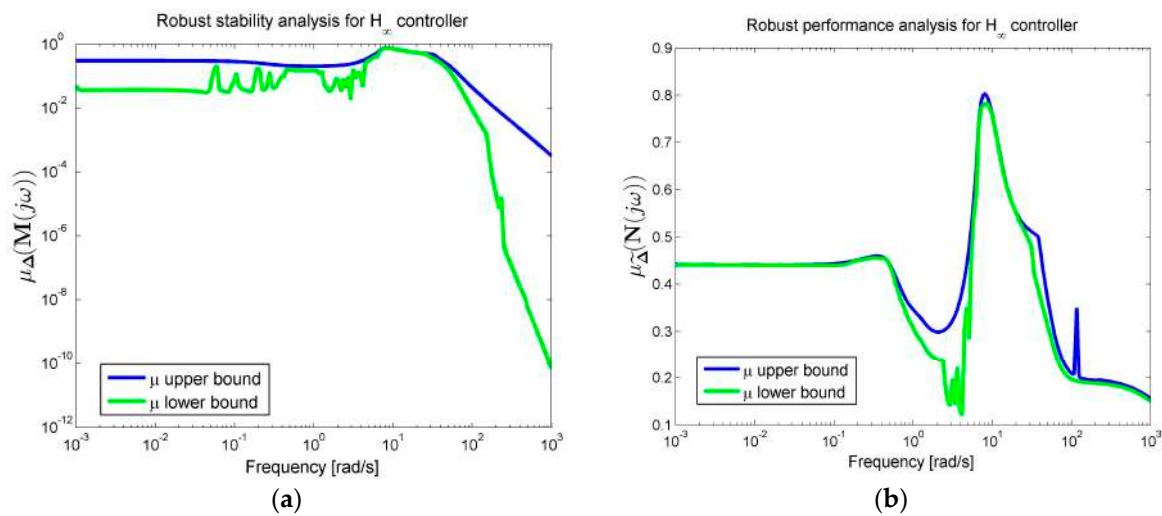


**Figure 16.** Nominal performance objectives: (a) Ideal model matching error; (b) control action; (c) stroke valves.

### 3.6.2. Robustness Analysis

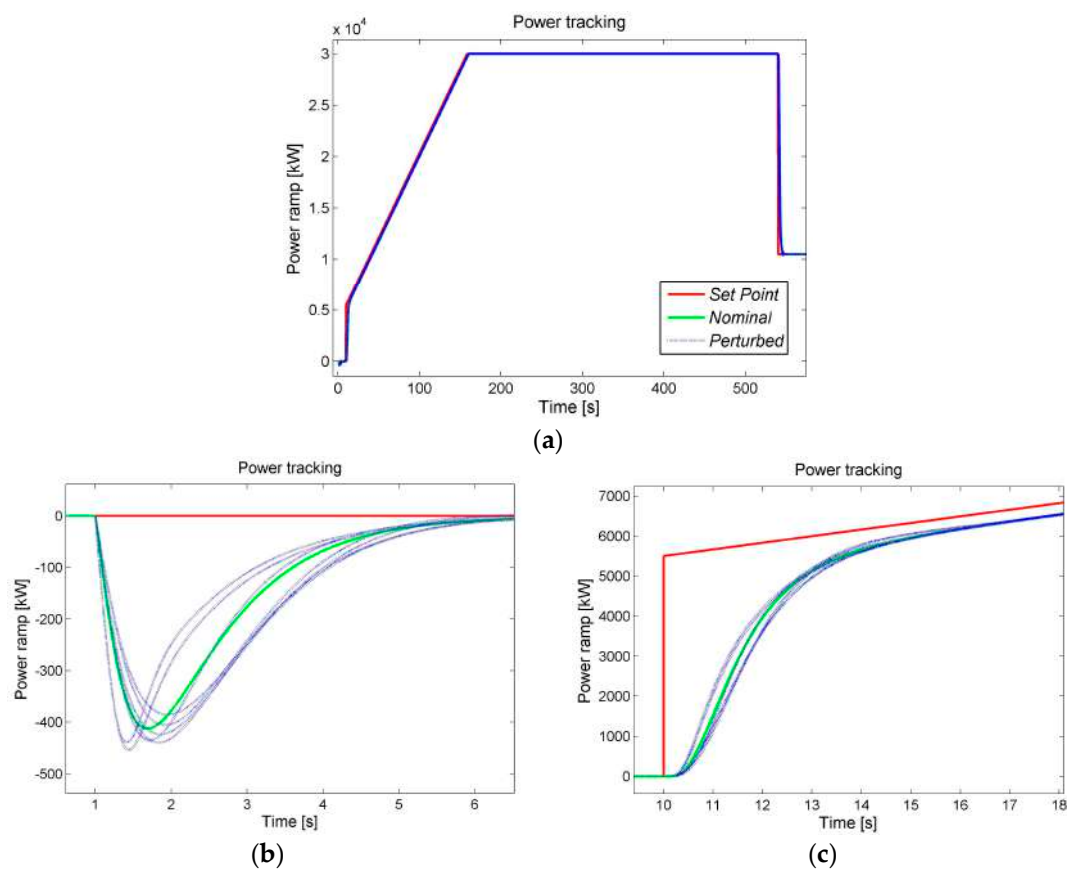
The robust properties were checked by exploiting the theory of structured singular value ( $\mu$ ) [26,27]. For robust stability and performance the frequency responses of  $\mu_{\Delta}(M)$  and  $\mu_{\tilde{\Delta}}(N)$  must be computed, and its supremum evaluated, since robustness to the largest expected uncertainty set requires  $\mu$  to be less than one.

The  $\mu$ -analysis can be performed through the command “mu” of the Robust Control Toolbox of Matlab®. The function mu computes upper and lower bounds for the structured singular value with sufficiently high accuracy in our problem. For practical purposes, the evaluation of  $\mu$  was carried out in the frequency range [0.001, 1000] rad/s. The structured singular value of both  $M$  and  $N$  are depicted in Figure 17.



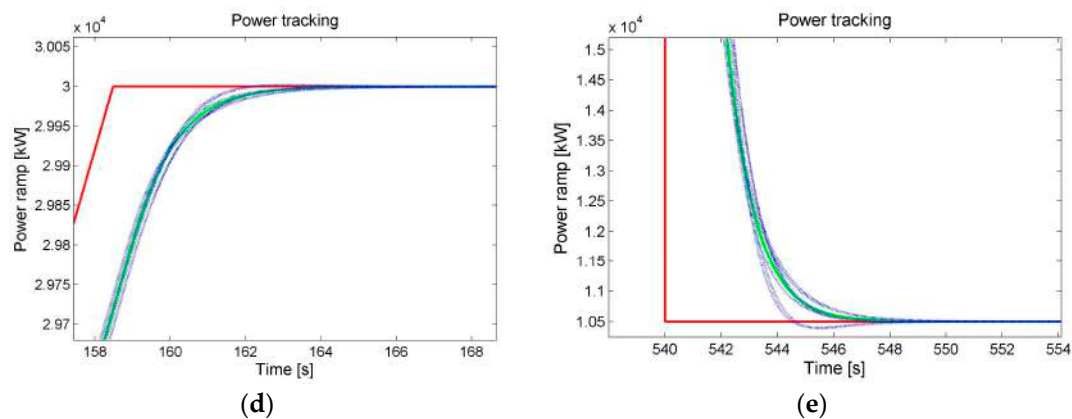
**Figure 17.** (a) Upper and lower bound of  $\mu_\Delta(M)$ ; (b) Upper and lower bound of  $\mu_\Delta(N)$ .

The maximum values of the upper bound for the structured singular value of both matrices  $M$  and  $N$  with respect of uncertainties are 0.76 and 0.8, respectively: such values are lower than one, thus Equations (39) and (40) are satisfied and the controller guarantees robust stability and performance. The power tracking of the closed-loop system with some random samples of the uncertain system is shown in Figure 18.



**Figure 18.** Cont.





**Figure 18.** Closed-loop power reference tracking with random samples of the uncertain system: (a) Complete view; (b) Disturbance rejection in the initial stage; (c) Ramp command start; (d) Steady-state at 30 MW; (e) Power profile in the final stage.

### 3.6.3. Controller-Order Reduction

A high order controller was obtained from the process of synthesis. In order to implement a controller which is easy to handle by a PLC and is computationally less demanding, the controller order must be reduced. There are different techniques in the literature to reduce the controller order. The most commonly adopted ones are the Balanced Truncation and the Hankel-Norm Approximation. A detailed discussion of these techniques is provided in [27]. In the present work, the Balanced Truncation was applied.

The reduced order controller was selected by evaluating the approximation error according to the Balanced Truncation method and comparing the nominal and robust performance of the obtained controllers. Controllers with order greater than 4 provided a small approximation error and similar nominal as well as robust performance with respect to the full order controller, while further reduction of the controller order led to deterioration of the control system performance. The fourth order controller was selected, as it represented a good compromise between performance and an easy implementation. In effect, an approximation error (see Equation (41)) of  $3.4771 \times 10^{-6}$  is satisfactory for the considered process; the nominal performance is very similar to the one of the full order controller, such as shown in Table 2, as well as the robustness analysis, which reports the same values of the full order controller. The Bode plots of full order and reduced order controller are shown in Figure 19. The corresponding plots practically coincide with each other, which implies similar performance in the closed-loop system. The low pass and band pass nature of the controllers in channel 1 and 2 is also evident in the Figure 19.

**Table 2.**  $H_\infty$  full order and reduced order controller set-point performance indexes.

Order	Settling Time (s)	Rise Time (s)	Overshoot (%)	IAE
4	140.2	130.4	0	$3.8819 \times 10^4$
35	140.1	130.3	0	$3.6436 \times 10^4$

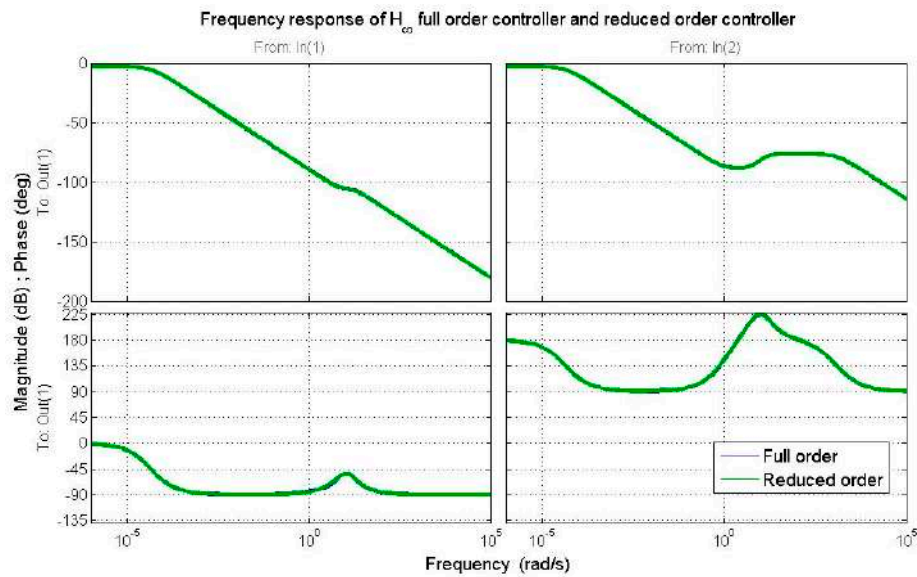


Figure 19. Frequency response of  $H_\infty$  full order controller and reduced order controller.

#### 4. Simulation Results

The designed multi-objective  $H_\infty$  robust controller was compared to the current PID-based governing system. The reduced order controller was discretized through the bilinear transformation (or Tustin transformation) technique before being introduced into the system, as it was assumed that it is implemented on a PLC. The discrete-time multi-objective  $H_\infty$  robust controller is taken hereafter as reference for the simulations. The nonlinear system was simulated with the two controllers and three experiments were performed for each tuning set:

1. Nominal conditions with the typical power ramp reference.
2. Perturbed conditions with a variation in steam conditions causing a 30% power reduction of turbines, a sensor dynamic slower of about 50% and added power losses of about 50% with respect to the nominal case, when the typical power ramp is demanded to the system.
3. Perturbed conditions with an unexpected variation of the actual conditions of the steam (as depicted in Figure 20), which causes a gradual power reduction of turbines of about 30% during the tracking of power reference.

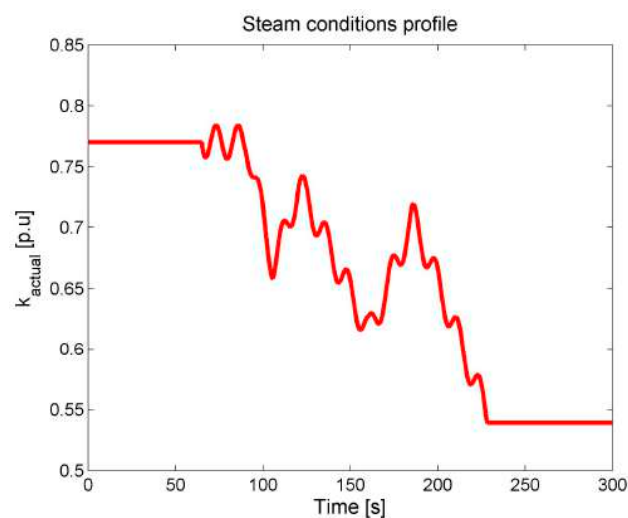


Figure 20. Unexpected steam conditions profile.

The results were compared assuming two scenarios corresponding to two different tuning set of the PID Governor: in the first scenario the actual PID gains, as set on the site under study, are considered. In the second scenario it is assumed that the PID Governor is optimally tuned according to the criterion of the minimum IAE [35]. Although this type of tuning is not applied during the commissioning phase on site, it can be considered a “theoretical limit” for the performance achievable through a PID and for this reason is taken as reference for the assessment of the potential advantages of the other less traditional control approaches.

#### 4.1. Nominal Conditions with Typical Loading Ramp

The power tracking of the nonlinear system with the two controllers is depicted in Figure 21. If the IAE tuning set is considered, the two controllers fulfill good reference tracking, whereas for disturbances rejection the robust control technique is faster than the PID. When the PID Governor holds the original gains values set on the site, the control action is very slow and consequently the disturbance rejection and the reference tracking is detuned. The multi-objective  $H_\infty$  robust controller in this case allows improving the performance of 5.8% about the settling time, 6.2% about the rise time and 94% about the IAE index. The set-point following performance indexes are synthetized in Table 3.

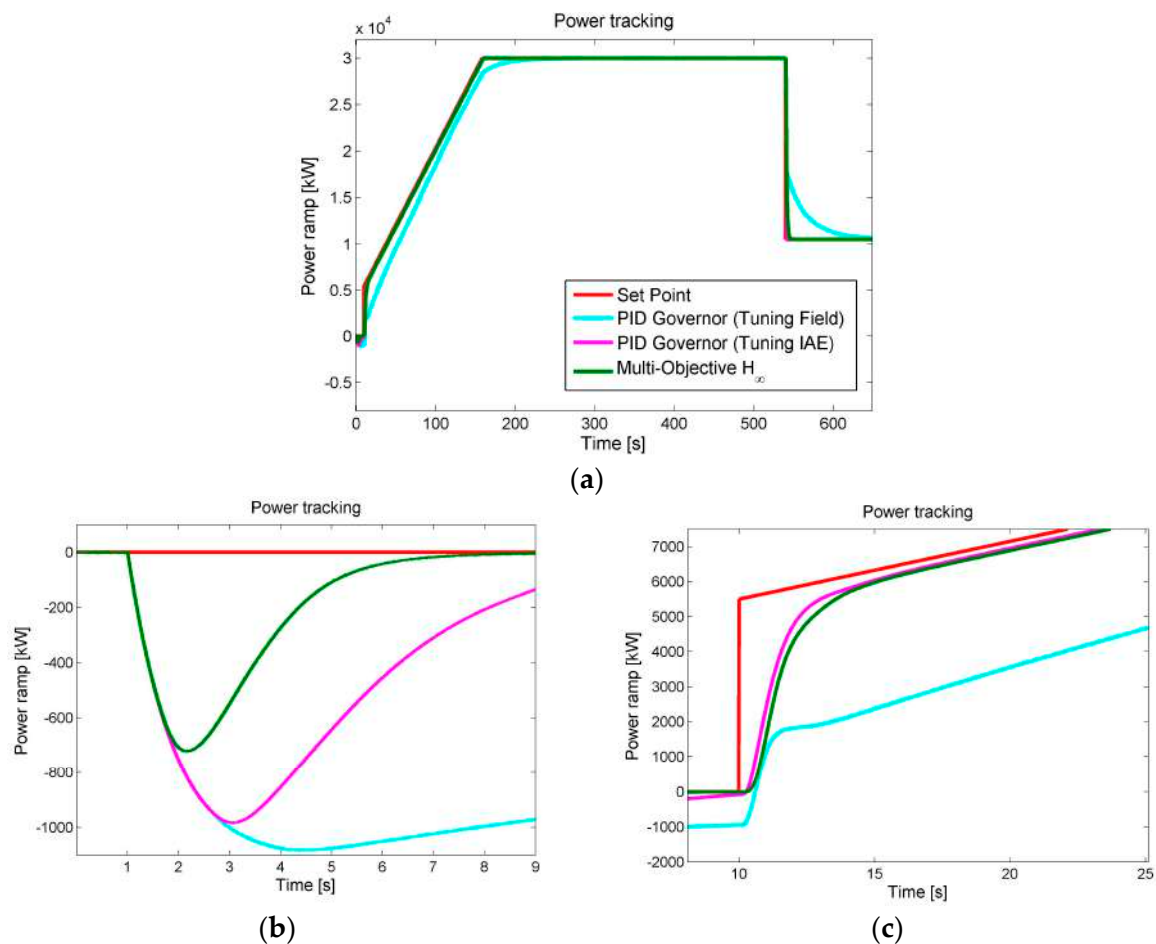
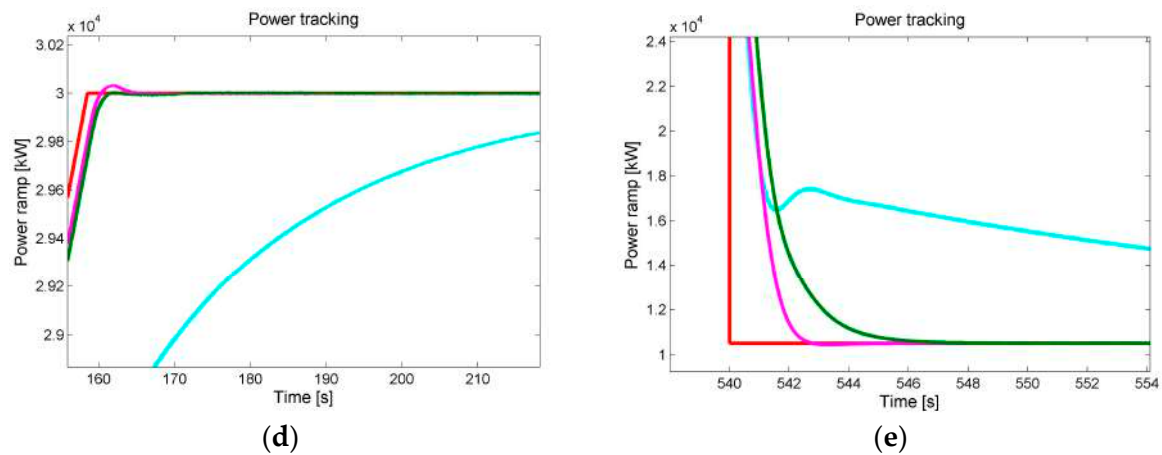


Figure 21. Cont.



**Figure 21.** Closed-loop power reference tracking of the nonlinear system. Comparison between the multi-objective  $H_\infty$  robust controller and the PID Governor tuned with IAE settings and site settings: (a) Complete view; (b) Disturbance rejection in the initial stage; (c) Ramp command start; (d) Steady-state at 30 MW; (e) Power profile in the final stage.

**Table 3.** Comparison between the set-point performance indexes of the different controllers.

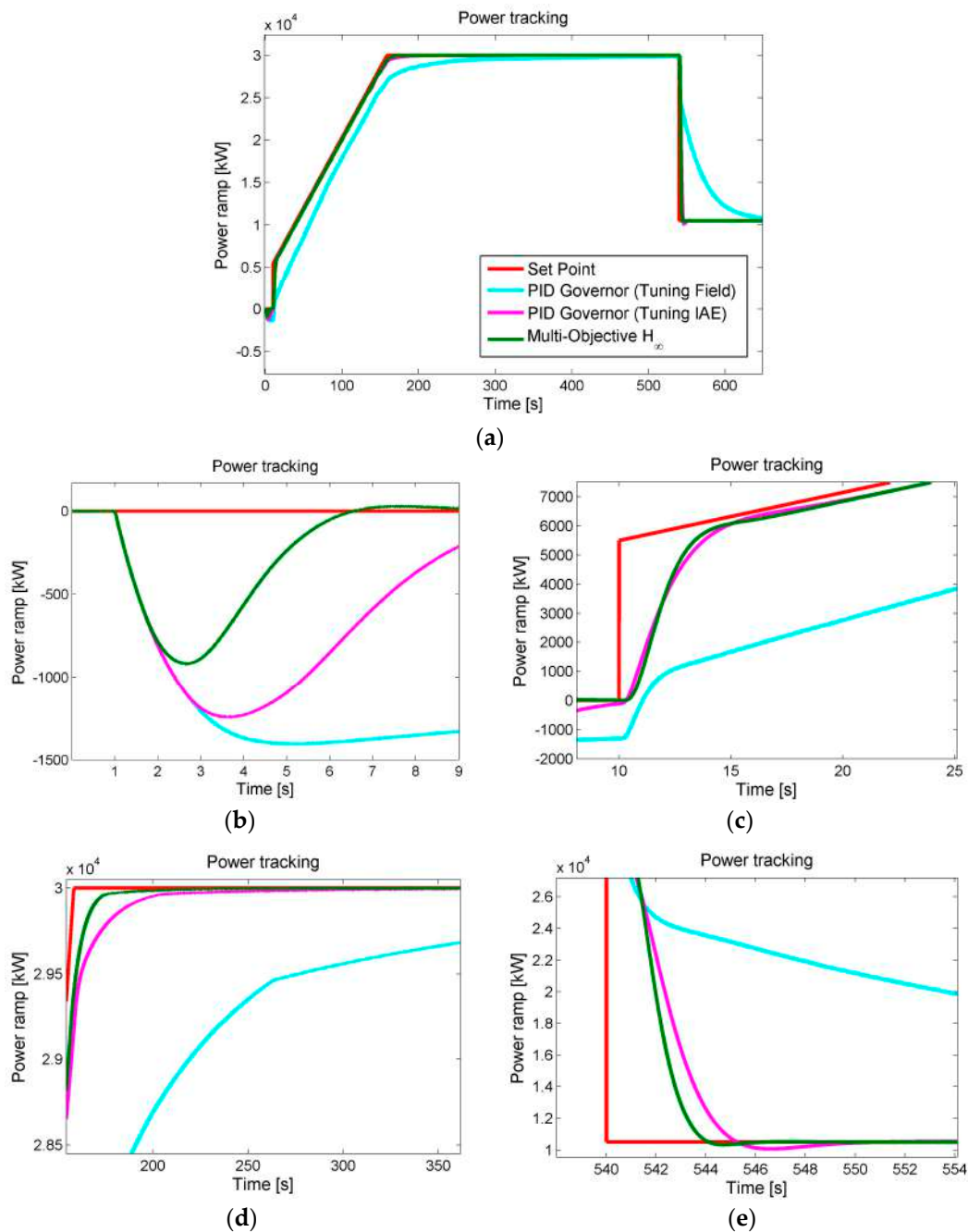
Controller	Settling Time (s)	Rise Time (s)	Overshoot (%)	IAE
PID Governor (Tuning Field)	148.5	138.7	0	$5.3188 \times 10^5$
PID Governor (Tuning IAE)	139.4	129.9	0.15	$2.3570 \times 10^4$
Multi-Objective $H_\infty$	139.9	130.2	0	$3.1240 \times 10^4$

#### 4.2. Perturbed Conditions with Typical Loading Ramp

Figure 22 shows the simulation results of the power tracking. If the IAE tuning set is considered, despite the additional power losses and the changing conditions of the steam, the set-point tracking of the two controllers is good. The proposed method allows quickly rejecting the disturbance in the initial stage of the power ramp and is faster than the PID Governor, as shown in Table 4. The performance indexes like settling time and rise time are slightly changed from the nominal case, although the perturbed conditions, only the IAE index is worse but the performances are still satisfactory. When the PID Governor holds the original gains value set on the site, is unable to deal with the parametric variations affecting the system, as is clearly shown in Figure 22. The slow control action does not allow to timely follow the reference. The multi-objective  $H_\infty$  robust controller in this case shows the best behavior: it improves the performance of 21.2% about the settling time, 5.7% about the rise time and 94.9% about the IAE index.

**Table 4.** Comparison between the set-point performance indexes of the different controllers.

Controller	Settling Time (s)	Rise Time (s)	Overshoot (%)	IAE
PID Governor (Tuning Field)	179.4	137.9	0	$1.0283 \times 10^6$
PID Governor (Tuning IAE)	141.7	130.7	0	$6.1366 \times 10^4$
Multi-Objective $H_\infty$	140.7	130	0	$5.1867 \times 10^4$

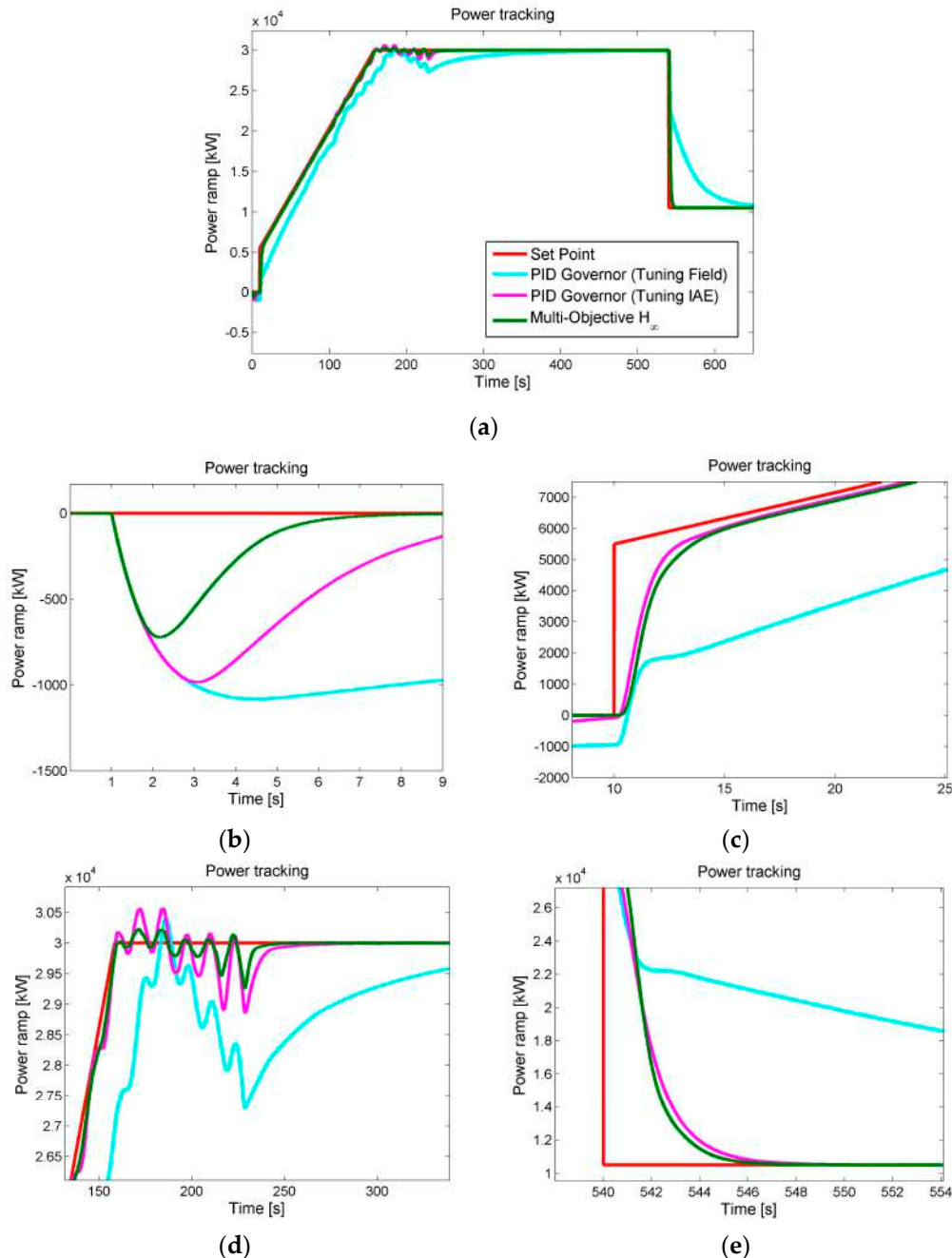


**Figure 22.** Closed-loop power reference tracking of the perturbed nonlinear system. Comparison between the multi-objective  $H_{\infty}$  robust controller and the PID Governor tuned with IAE settings and site settings: (a) Complete view; (b) Disturbance rejection in the initial stage; (c) Ramp command start; (d) Steady-state at 30 MW; (e) Power profile in the final stage.

#### 4.3. Perturbed Conditions with an Unexpected Variation of the Steam

The power tracking of the nonlinear system with the two controllers is depicted in Figure 23. If the IAE tuning set is considered, the two controllers fulfill good reference tracking and disturbances rejection but as the perturbations gradually increase, the performances of the PID Governor decrease as it shown from the performance indexes of these last two experiments. When the PID Governor holds the original gains values, the slow control action leads to poor tracking of the power reference, difficulties in managing the perturbed profile of the steam and consequently worse performances with

respect to the perturbed conditions of the second experiment. The multi-objective  $H_\infty$  robust controller does not suffer substantial degradation of performances and remains the best controller. It improves the performance of 41.7% about the settling time, 11.1% about the rise time and 94.2% about the IAE index. The set-point following performance indexes are synthetized in Table 5.



**Figure 23.** Closed-loop power reference tracking of the perturbed nonlinear system. Comparison between the multi-objective  $H_\infty$  robust controller and the PID Governor tuned with IAE settings and site settings: (a) Complete view; (b) Disturbance rejection in the initial stage; (c) Ramp command start; (d) Steady-state at 30 MW; (e) Power profile in the final stage.



**Table 5.** Comparison between the set-point performance indexes of the different controllers.

Controller	Settling Time (s)	Rise Time (s)	Overshoot (%)	IAE
PID Governor (Tuning Field)	243.1	147.2	1.64	$9.3471 \times 10^5$
PID Governor (Tuning IAE)	143.1	131.9	2.1	$7.7127 \times 10^4$
Multi-Objective $H_\infty$	141.7	130.9	0.9	$5.4491 \times 10^4$

## 5. Conclusions

The multi-objective  $H_\infty$  robust controller was applied to the power control of a CSP plant composed by two turbines, a gear and a generator. Firstly, the controller was synthesized on the linear model of the system and its performance and robustness were analyzed. The designed controller is of order 35, which makes the implementation of the controller complex. Hence, the controller order was reduced to 4th order through the Balanced Truncation method, allowing an easy implementation on PLC machine. Hereafter a discrete-time controller was obtained and tested on the nonlinear system.

The multi-objective  $H_\infty$  robust controller was compared to the current PID-based governing system with two type of setup gains. The IAE optimization method was considered here for the PID Governor tuning, although this technique is not used on site and a more conservative although less performing tuning procedure is adopted. Three experiments were performed for each tuning set: a test with unperturbed conditions, and two tests with perturbed conditions. The proposed controller effectively deals with the dynamic parametric variations of the system, showing its robustness, reporting a fast rejection of the disturbances, ensuring better performance compared of the PID Governor, which is ineffective and cannot guarantee the same performance of an advance control technique without complex automated and self-tuning on-line procedures.

Future work will deal with experiments on the use of GA, or Fuzzy Multi-Objective Linear Programming (FMOLP) techniques [36] that can be applied in different contexts and to solve problems with fuzzy constraints, such as, for instance, in the application that has been recently presented in [37]. These strategies will allow supporting the design procedure, which is often complex, as it requires experience and the accomplishment of a time-consuming series of steps before getting the required performance objectives. Currently, GA-based techniques are being investigated, to the aim of finding the optimal parameters of the weighting functions with a given structure by maximizing a fitness function that is related to the performance of the control.

**Author Contributions:** This paper is part of the Master Thesis of Vincenzo Iannino, who has therefore carried out most of the work presented here. Valentina Colla and Mario Innocenti were the supervisors of this work, provided indications and guidelines and reviewed all the steps of the work, whereas Annamaria Signorini was the technical manager of the industrial partner and supported the evaluation of the achieved results.

**Conflicts of Interest:** The authors declare no conflict of interest.

## Abbreviations

AI	Artificial Intelligence
ANFIS	Adaptive Neuro Fuzzy Inference System
CPC	Current to Pressure Converter
CRHPC	Constraint Receding Horizon Predictive Control
CSP	Concentrated Solar Power
GA	Genetic Algorithms
GPC	General Predictive Control
HDAC	Hydraulic Double Acting Cylinder
HP	High Pressure
HPC	Hydraulic Pilot Cylinder
IAE	Integral Absolute Error
IMC	Internal Model Control

LLFT	Lower Linear Fractional Transformation
LMI	Linear Matrix Inequalities
LP	Low Pressure
LQR	Linear Quadratic Regulator
MBC	Model Based Control
MIMO	Multiple Input Multiple Output
MISO	Multiple Input Single Output
MPC	Model Predictive Control
MRAC	Model Reference Adaptive Controller
PI	Proportional Integral
PID	Proportional Integral Derivative
PLC	Programmable Logic Controller
PSO	Particle Swarm Optimization
PV	Photovoltaics
RBFNN	Radial Basis Function Neural Networks
ULFT	Upper Linear Fractional Transformation

## Symbols

$K_{steam}$	Steam gain
$P_{rated}$	Rated power
$\dot{m}_{inlet}$	Inlet steam mass flow
$\dot{m}_{rated}$	Maximum steam mass flow
$k_{actual}$	Actual steam conditions
$\omega$	Rotational speed
$\omega_{synchro}$	Synchronism rotational speed
$P_m$	Turbine mechanical drive power
$P_{out}$	Turbine useful power output
$P_{T_{fric}}$	Turbine friction power losses
$P_{b_{loss}}$	Bearing power losses
$\tau_{HP}$	HP turbine torque
$\tau_{LP}$	LP turbine torque
$\tau_{GB}$	Gearbox friction torque
$\tau_{GE}$	Electric generator torque
$\tau_{wb}$	Windage and bearing friction torque
$\tau_{load}$	Full load torque power losses
$J_T$	Total moment of inertia
$J_{HP}$	HP turbine moment of inertia
$J_{LP}$	LP turbine moment of inertia
$J_{GB}$	Gearbox moment of inertia
$J_{GE}$	Generator moment of inertia
$P_{f_{loss}}$	Full load power losses
$P_{wb_{loss}}$	Windage and bearing rated power losses
$P_e$	Electric power
$P_{GB_{fric}}$	Gearbox power losses
$P_{GE_{losses}}$	Electric generator power losses
$s$	Complex Laplace variable
$P(s)$	Extended plant transfer matrix
$G(s)$	Nominal plant transfer matrix
$K(s)$	Controller transfer matrix
$T_{zw}(s)$	Transfer matrix from $w$ to $z$
$w$	Generalized disturbance
$z$	Controlled variable
$y$	Measurement output
$u$	Control input

$F_l(M, Q)$	LLFT
$F_u(M, Q)$	ULFT
$\ \cdot\ _\infty$	$H_\infty$ -norm
$\bar{\sigma}(A)$	Largest singular value of $A$
$J_\infty(K)$	$H_\infty$ cost function
$S$	Sensitivity
$T$	Complementary sensitivity
$R$	Control effort
$W_f$	Weigh function
$G_A$	Actuator transfer function
$K_\alpha$	Look-up table gain
$\Delta$	Unknown uncertainty
$\delta$	Real uncertainty parameter
$\rho$	Magnitude of $\delta$
$ \beta $	Absolute value of $\beta$
$M_T$	Turbine transfer matrix
$M_S$	Sensor transfer matrix
$T_s$	Sensor time constant
$r$	Reference input
$d$	Disturbance input
$n$	Noise input
$w_\Delta$	Uncertainty output
$z_\Delta$	Uncertainty input
$e$	Tracking error
$\mu$	Structured Singular Value
$M$	Transfer matrix from $w_\Delta$ to $z_\Delta$
$N$	Transfer matrix from $\begin{bmatrix} w_\Delta \\ w \end{bmatrix}$ to $\begin{bmatrix} z_\Delta \\ z \end{bmatrix}$

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