

# Dynamic modeling of a Low-Concentration Solar Power Plant: a control strategy to improve flexibility

M. Antonelli\*, A. Baccioli, M. Francesconi, U. Desideri

*University of Pisa, largo Lucio Lazzarino, Pisa 56125, Italy*

---

## Abstract

This paper deals with a dynamic analysis on a low concentration solar power plants coupled with Organic Rankine Cycles (ORC), which can be an alternative to PV systems because of their capability of providing a smoother electricity production due to their thermal inertia. At least within certain restraints, moreover they are able to exploit diffused solar radiation.

The dynamic model of a plant with static compound parabolic collectors and an ORC cycle, using a rotary volumetric expander, was developed using the simulation tool AMESim. All the main components of the plant are modelled: solar collectors field, heat transfer fluid circuit, heat exchangers and the ORC cycle. The plant response to the radiation of different days was analyzed to quantify the daily production and the trend of various plant parameters. Real ambient conditions were employed for the simulations by using data obtained by historical series.

The results showed that the employment of a volumetric expansion device with variable rotating speed allows the plant to operate at different radiations

---

\*telephone number: +39 050 2217133 - fax: +39 050 2217160

*Email address:* marco.antonelli@ing.unipi.it (M. Antonelli )

and ambient temperatures without the need of any storage system or external heat sources. Results can be extended to other applications, such as low temperature waste heat recovery or geothermal systems.

*Keywords:*

Dynamic modelling; ORC solar power plant; AMESim; control strategy; volumetric expansion device; Compound Parabolic Collectors

---

## 1. Introduction

The interest towards solar energy has been increasing in the last years. In the micro-generation field, Photo-Voltaic (PV) systems are widely used due to their installation simplicity, simple management, and low costs of maintenance. However the lack of inertia of these systems and the unprogrammable nature of the source, are causing problems on the electric grid. Low concentration solar plants can limit fluctuations of delivered power because of their thermal inertia. Obviously, since we are talking about systems that are addressed to domestic or small industrial or commercial activities, simple, low cost and small size units have to be developed. Compound Parabolic Collectors (CPC) and volumetric expansion devices can help in the accomplishment of this objective. CPCs have been studied for several years [1, 2] and are characterized by a wide operational flexibility [3]. Because of their wide acceptance angle, CPCs do not need any tracking system, and allow to reach higher temperatures with better efficiencies than flat plate collectors [4]. Volumetric rotary expanders are more suitable than micro-turbines for small power output applications, because of the higher isentropic expansion efficiency, lower rotational speed, lower costs [5–7] and wider possibility of

19 control [8]. The variation of the rotational speed in particular can be easily  
20 achieved and keeps the isentropic efficiency of the device almost constant [9].  
21 Using this control, the power output can be varied without the need of a  
22 storage system, simplifying the layout, saving space and reducing installa-  
23 tion costs. Because of the strong variation of thermal input and the lack of  
24 a storage system or integration with an external source, it is important to  
25 consider the effective dynamic behavior of the system, in order to properly  
26 set parameters, improve performances and management.

27 Dynamic modelling in facts has become an important tool for solar plants  
28 and in general for applications characterized by large variations of the input  
29 power. Manenti et al. [10, 11] carried out numerical simulations to perform  
30 the start-up operations of Archimede Concentrating Solar Plant in Sicily, us-  
31 ing DYNsIM. In their papers they identified the critical aspects of start-up  
32 and shut-down operations and optimized the control strategy of the plant.  
33 El Hefni [12] employed ThermoSysPro - Modelica in modeling a solar plant  
34 with different type of collectors and a solar hybrid combined-cycle power  
35 plant with PTC collectors. Rodat et al. [13] simulated the dynamic response  
36 of two solar concentrating plants with Fresnel collectors in the Modelica en-  
37 vironment. They monitored the temperature of the superheated steam after  
38 the cloud passage and highlighted the difficulty to tune a proper control sys-  
39 tems to handle both slow and fast phenomena. Other authors focused on the  
40 optimization of a part of the plant: Eck et al. [14] studied the superheated  
41 steam control system of a PTC loop, Henrion et al. [15] used dynamic simula-  
42 tion in the design of an innovative evaporator, with a particular attention to  
43 start-up operations. Quoilin et al. [16] showed the possibility of controlling

44 and optimizing a small power output Waste Heat Recovery system through  
45 the variation of the speed of a scroll expander.

46 This paper shows the numerical modelling of a 25 kW ORC solar plant by  
47 means of the AMESim simulation tool, showing the capability of the model  
48 of highlighting the optimal working condition of the plant from the point of  
49 view of the solar field parameters (concentration and tilt). This paper clearly  
50 indicates the need for a dynamic simulation which was able to evaluate the  
51 influence of warm-up period on the electrical production of the plant.

52 This work also demonstrates the effectiveness of the control strategy based  
53 on the rotating speed of the expander, which proved to be able of operating  
54 under variable radiation conditions, without the need for any storage system  
55 or integration with external heat sources.

56 The novelty which is introduced in this work consists in the application  
57 of this kind of simulation and control strategy in a small-size power plant,  
58 which employs non-tracking, low concentration collectors, whose parameters  
59 have been chosen in order to optimize the overall production along several  
60 working days. The conditions which have been taken as a reference were  
61 both ideal conditions (fully sunny day) and real ones, derived from historical  
62 series.

### 63 **Nomenclature**

$a$	Azimuth angle ( $^{\circ}$ )
$A$	Exchange area ( $\text{m}^2$ )
$C$	Concentration
$G$	Global incident radiation ( $\text{W}/\text{m}^2$ )
$i$	Incident angle ( $^{\circ}$ )

$I_{bn}$	Ground direct radiation (W/m <sup>2</sup> )
$I_{d0}$	Ground diffuse radiation (W/m <sup>2</sup> )
$\dot{m}$	Mass flow rate (kg/s <sup>-2</sup> )
$p$	Pressure (bar)
$r$	Ambient reflectivity (-)
$t$	Time (s)
$T$	Temperature (K)
$u$	Specific internal energy (J/kg)
$U$	Internal energy (J)
$V$	Volume (m <sup>3</sup> )
$\dot{V}$	Volume flow rate (m <sup>3</sup> /s)
$\dot{W}$	Power (kW)

*subscripts*

$c$	collector
$el$	electrical
$exp$	expander
$is$	isentropic
$mec$	mechanical
$p$	pump
$ad$	admission
$sat$	saturation
$sh$	superheating
$HTF$	Heat Transfer Fluid
$r$	receiver

*Greek*

$\alpha$	Solar height ( $^{\circ}$ )
$\beta$	Collectors tilt angle ( $^{\circ}$ )
$\eta$	Efficiency
$\lambda$	heat exchange coefficient ( $\text{W}/\text{m}^2\text{K}$ )
$\rho$	Density ( $\text{kg}/\text{m}^3$ )

*Acronyms*

*PV* Photovoltaic

*CPC* Compound Parabolic Collectors

64 **2. System description and fluids**

65 The studied system consists of a non-tracking CPC field, an HTF circuit  
 66 and an ORC (fig. 1). The cycle is composed by a pump, an evaporator, an  
 67 expansion device, a recuperator and an air cooled condenser. Superheating  
 68 and regeneration are employed because in a previously published work [17]  
 69 they proved to improve the overall efficiency of the plant. The choice of  
 70 the heat transfer fluid and of the working fluid is critical. In fact the heat  
 71 transfer fluid should have good thermal properties to efficiently transfer the  
 72 heat, high density and low viscosity to limit the pumping power loss. Since  
 73 the maximum temperature of this system is expected to be about  $160^{\circ}\text{C}$ ,  
 74 pressurized water was chosen as heat transfer fluid. The working fluid is  
 75 R-600a since it gave the best results in the stationary analysis of the plant  
 76 [4].

77 INSERT FIG. 1 ABOUT HERE

78 The CPCs employed evacuated pipes to suppress convection losses as

79 shown in a previous paper [4]. The number of collectors was chosen to provide  
80 the thermal input needed by the plant when the expansion device rotated at  
81 its maximum speed (3000 rpm). CPCs were arranged in arrays composed of  
82 9 collectors linked in series, and each array was in parallel with the other,  
83 as reported in fig. 2. A schematic view of an array tilted by a generic  
84 angle is reported in fig. 3. In fig. 4 the efficiency of the collectors provided  
85 by manufacturers is reported. The collector field outlet temperature was  
86 controlled by the circulating pump speed. The collectors were disposed in  
87 the East-West direction, for the sun rays to be incident on the CPC aperture  
88 within the acceptance angle [18].

89 INSERT FIG. 2, 3 and 4 ABOUT HERE

90 The expander displacement and introduction grade, defined as in [5], were  
91 respectively  $316 \text{ cm}^3$  and 0.2 and the rotational speed was varied in the range  
92 500-3000 rpm. The velocity of the expander was used to control the evaporating  
93 pressure set point. An inverter is therefore needed to connect the  
94 plant to the grid. Condensing temperature was  $15^\circ\text{C}$  higher than the ambi-  
95 ent temperature and therefore was variable during the day. The choice of a  
96 variable condensing temperature was possible since the expander is volumet-  
97 ric and the only restriction on the pressure ratio is given by over-expansion  
98 phenomena [19], which should be avoided by means of an appropriate value  
99 of saturation pressure [9].

### 100 3. Numerical model

101 The numerical model of the plant was developed with AMESim v.12,  
102 a 1-D multi-physics commercial code. Elements of the thermal-hydraulic,

103 thermal and two-phase flow libraries were used to model the system. An  
104 overview of the model is reported in fig. 5.

105 INSERT FIG. 5 ABOUT HERE

### 106 3.1. CPCs model

107 Collectors were modelled in order to take into account the main thermal  
108 exchange phenomena, as reported in fig. 4 and table 1.

109 INSERT FIG. 4 ABOUT HERE

110 INSERT TABLE 1 ABOUT HERE

111 The interaction with solar radiation was simulated through an appro-  
112 priate sub-model of the thermal library, which allows to calculate the solar  
113 radiation on a planar surface, according to eq. 1 - 3, using as input the solar  
114 altitude, the azimuth, the ground radiation, the collector azimuth and the  
115 tilt angle.

$$G = I_{bn} \cos(i) + \frac{I_{d0}}{C} \cos^2\left(\frac{\beta}{2}\right) + [I_{bn} \sin(\alpha) + I_{d0}] r \sin^2\left(\frac{\beta}{2}\right) \quad (1)$$

$$C = \frac{A_c}{A_r} \quad (2)$$

$$\cos(i) = \cos(a - a_w) \cos(\alpha) \sin(\beta) + \sin(\alpha) \cos(\beta) \quad (3)$$

116

117 where  $a_w$  is the angle formed between the normal of the panel and the  
118 south direction on the horizontal plane. Since no data were available about  
119 the diffuse and reflected radiation, only ground direct radiation was con-  
120 sidered, neglecting the diffuse and reflected component. The effect of the



121 acceptance angle of the concentrator and of the panel was taken into account  
122 by cutting radiation data off the range of the acceptance angle. Thermal  
123 inertia of the panels was computed by introducing the mass and the material  
124 properties of various components. The receiver was modelled as an evacuated  
125 pipe consisting of two glass envelopes and a single inner copper pipe. The  
126 heat transfer within the enclosure was calculated using radiative, convective  
127 and conductive resistances according to fig. 6 available in the software. The  
128 value of each resistance was evaluated by referring to literature data [20, 21].  
129 The efficiency of the collector was finally computed as the ratio between the  
130 useful heat and the incident radiation, and its trend was validated by the  
131 manufacturers specification, as shown in fig. 7. The whole solar field heat  
132 flow rate was calculated by multiplying the mass flow rate of a single array  
133 by the total number of arrays.

134     INSERT FIG. 7 ABOUT HERE

### 135 *3.2. HTF circuit*

136     The HTF circuit was modelled as an open loop which receives the heated  
137 fluid from the solar field. Whithin the loop the HTF heated the working fluid  
138 of the ORC and then it was sent back to the solar field by means of a variable  
139 speed circulating pump, which controlled the collectors outlet temperature  
140 through a proportional control. Pressure loss of the circuit were taken into  
141 account through various punctual orifices. A pressurized expansion tank was  
142 inserted to compensate the volumetric expansion of the heat transfer fluid.

143 *3.3. Heat exchangers*

144 The preheater, the vaporizer and the superheater were modelled as dis-  
145 tinct elements, each of one was divided into several nodes to account for HTF  
146 and working fluid temperature variation. All the heat transfer sections were  
147 modelled as shell and tube exchangers. The HTF flows inside the tubes,  
148 while R-600a flows inside the shell. In order to model the HTF, the elements  
149 of thermo-hydraulic library were used, while the elements of the two phase  
150 flow library were adopted for the working fluid.

151 For each node and for each fluid the code computed the variation of  
152 internal energy using the first law of thermodynamics applied to an open  
153 system:

$$\frac{dU}{dt} = \sum_{i=1}^n \dot{m}_i \cdot h_i + \frac{d\dot{Q}}{dt} = \rho V \frac{du}{dt} + u V \frac{d\rho}{dt} \quad (4)$$

$$\frac{dQ}{dt} = \lambda \cdot A \cdot \Delta T \quad (5)$$

154 The heat transfer coefficient were evaluated by the numerical code by  
155 using built in correlations. For the HTF side, the Nusselt number was eval-  
156 uated by using the Sieder and Tate correlation [23]. For the two phase side,  
157 the heat transfer was modelled using correlations for pipes and adding sev-  
158 eral chambers to take into account the major volume of the shell, since the  
159 software does not allow to model the shell of an heat exchanger.

160 On the R600a side, the Gnielinski and VDI (Verein Deutscher Ingenieure)  
161 correlations were used in single phase turbulent regime and when the fluid  
162 boils in horizontal tubes respectively [24].

163 A sensitivity analysis about the influence of the two phase flow correlation  
164 was carried out by using constant heat transfer coefficients and the results  
165 showed that these coefficients did not provide any important variation on  
166 production and on plant behavior, being one order of magnitude larger than  
167 the HTF heat transfer coefficient.

168 The total volume of the chambers used to model the shell was about 100  
169 liters, as a result of the heat exchanger design calculation.

#### 170 3.4. Expansion device

171 The expansion device was modelled by using, the "two phase turbine"  
172 model, which uses several look-up tables to calculate the volumetric flow  
173 rate and isentropic efficiency as a function of the pressure ratio and of the  
174 rotational speeds. These data were gathered from the results of the numerical  
175 model of the expansion device [4–6]. The fitted surface of the volumetric flow  
176 rate is shown in fig. 8.

177 INSERT FIG. 8 ABOUT HERE

178 The expander speed was controlled in order to keep the saturation pres-  
179 sure at the set point value. The value of the speed was controlled in the range  
180 of 500-3000 rpm in order to keep the value of saturation pressure at the set  
181 point if the exchanged heat is enough to warm up the fluid up to the tem-  
182 perature corresponding to the set point saturation pressure. In other cases  
183 the device rotates at its minimum speed. The mechanical efficiency (0.95)  
184 and the electrical efficiency (0.85) were considered constant and average for  
185 similar applications. Output power was calculated as:

$$\dot{W}_{exp} = \rho_{ad} \cdot \dot{V} \cdot \Delta h_{is} \cdot \eta_{is} \cdot \eta_{mec} \cdot \eta_{el} \quad (6)$$

186 *3.5. Feed Pump*

187 The pump was modelled as a volumetric fixed displacement pump with  
188 a constant efficiency ( $\eta_p = 0.8$ ) and its work consumption was calculated as:

$$\dot{W}_p = \frac{\dot{m} \cdot \Delta p}{\rho \cdot \eta_p} \quad (7)$$

189 The pump rotational speed controlled the superheating temperature.

190 *3.6. Condenser*

191 The condenser was modelled as a two phase flow separation chamber  
192 with set internal temperature, variable over time. The internal temperature  
193 was kept 15 °C above the ambient temperature to ensure the heat transfer  
194 between the working fluid and the air. The air condenser consumption was  
195 calculate by multiplying the specific consumption by the condensing thermal  
196 power. The value of the specific consumption was 17  $W/kW_{th}$ , obtained from  
197 state of the art commercial equipments.

198 *3.7. Recuperator*

199 The efficiency of the recuperator was assumed as constant and equal to  
200 0.85.

201 *3.8. Control System*

202 Three control loops was defined in this model:

- 203 1. control of the outlet temperature of the collector field at the set point  
204 value, by changing the rotational speed of the circulating pump;
- 205 2. control of the evaporating pressure, by changing the expander speed;

206 3. control of the superheating temperature, by changing the feed pump  
207 speed.

208 This control strategy allows to operate the plant at the best thermo-  
209 dynamic conditions which are very near to the conditions studied in  
210 the stationary analysis [17]. If the temperature of the HTF fluid were  
211 not controlled and the pump were kept at constant speed, on one hand  
212 there would be the risk of choosing a too low flow rate, which can  
213 cause water vaporization when irradiation occurs, and on the other  
214 there would be the risk to operate with a too low temperature, which  
215 reduces the thermodynamic efficiency of the ORC. The saturation pres-  
216 sure of 28.4 bar and the superheating temperature of 150 °C gave the  
217 best results in terms of overall efficiency.

#### 218 4. Boundary conditions

219 The model was simulated in different conditions of radiation and for sev-  
220 eral consecutive days using data from historical series for the city of Pisa,  
221 available in [22]. This data provided ground irradiation and air temperature  
222 hour by hour for every day of the year.

223 Air temperature was used both to calculate the condenser temperature  
224 ( $T_c = T_a + 15$ ), and to calculate convection and radiation losses of the col-  
225 lectors.

226 Since the acceptance angle of the concentrators is 60°, the tilt angle of the  
227 panel was varied in the range 35-50°. Larger values prevent the collection of  
228 sun rays in the middle of the day, when the solar altitude is maximum during  
229 the summer period, whereas lower values prevent the collection of sun rays

230 when the solar altitude is lower, i.e. in winter and shortly after the sunrise  
231 and before the sunset.

232 Solar altitude and azimuth were provided to the model to calculate the  
233 incidence angle with the glass cover of the collectors. The number of panel  
234 was set in order to provide the maximum thermal power of about 150 kW  
235 to the plant ( $P_{sat} = 28.4 \text{ bar}$ ,  $T_{sh} = 150^\circ\text{C}$ ,  $T_{HTF} = 160^\circ\text{C}$ ) on the 21th of  
236 June. Mutual shading between the various rows was calculated as a function  
237 of the tilt angle, of the solar altitude angle and of the distance between the  
238 rows.

## 239 5. Simulations and Results

### 240 5.1. Clear sky conditions

241 A first simulation with clear sky conditions and on the 21st of June (fig.  
242 9) was performed to set up the control parameters of the plant. The efficiency  
243 of the recuperator was set to 0.85. Lower values lead to lower performances,  
244 despite the increase of the temperature of the HTF at the collectors inlet,  
245 which lowered their efficiency.

246 INSERT FIG. 9 ABOUT HERE

247 As an example, the results of the calculations with  $\beta = 35^\circ$  are reported  
248 in fig. 10 and 11 in terms of radiation, thermal input, delivered electrical  
249 output and HTF temperatures. As expected, without any storage system,  
250 the mechanical output followed the trend of the incident radiation, but with  
251 a slight delay due to the thermal inertia of the system. After the sun set on  
252 collectors the plant continued to operate for almost an hour. The trend of  
253 production is slightly wrinkled because of the daily variation of the condens-

254 ing pressure which is bounded by the ambient air temperature. The delay  
255 after the sun rised in collectors was due to the time which was needed to  
256 warm up the HTF and to produce vapor with a unit vapor quality. The  
257 circulating pump speed was kept at the minimum during warm-up and it  
258 was increased as the temperature approached the set-point (160 °C).

259 INSERT FIG. 10 ABOUT HERE

260 INSERT FIG. 11 ABOUT HERE

261 As shown in fig. 12, the variation of the expander rotating speed was an  
262 effective mean to control the evaporating pressure; the superheating temper-  
263 ature also proved to be quite constant along the day (fig. 13). The global  
264 data regarding the collected radiation, the electrical production and the av-  
265 erage efficiency of the plant are reported in tab. 2. In this case the plant was  
266 able to follow the variations of radiation and set point value were retained  
267 during operations.

268 INSERT FIG. 12 ABOUT HERE

269 INSERT FIG. 13 ABOUT HERE

270 INSERT TAB. 2 ABOUT HERE

## 271 5.2. *Real conditions*

272 The plant was simulated in real sky conditions to verify its operational  
273 flexibility. On the basis of the analysis described in the previous paragraph,  
274 the tilt angle of the panels was increased to 45° to collect more radiation and  
275 consequently the sunrise angle of the panel decreased to 15°. To limit the  
276 ground occupied surface, mutual shading was accepted and the closest rows  
277 to the ground saw the sun when its altitude was higher than 25°.

278 Because of the different incidence angle the number of concentrators was  
279 increased to 666, to collect the same maximum thermal power of 150 kW,  
280 with a surface of the panels of 197 m<sup>2</sup> and an occupied area of 656 m<sup>2</sup>. If  
281 mutual shading is avoided the occupied ground surface of the collectors field  
282 raises up to 1480 m<sup>2</sup>, reducing the plant specific energy production per unit  
283 of ground surface.

284 Five consecutive days on the month of October were simulated (fig. 14).  
285 These days were chosen since they are representative of different radiation  
286 conditions, as reported in fig. 15, both for the lowest collector (the closest  
287 to the ground) and for the highest.

288 INSERT FIG. 14 ABOUT HERE

289 INSERT FIG. 15 ABOUT HERE

290 As expected, because of the absence of the storage, collectors heat output  
291 and mechanical output (fig. 16) followed the trend of solar radiation with  
292 a later start up after the sunrise and a later shut down after the sunset.  
293 Under a certain radiation value production did not start-up, since the useful  
294 heat was not enough to compensate thermal losses and warm-up. Shut-down  
295 occurred an hour after the collectors did not see the sun (fig. 15).

296 INSERT FIG. 16 ABOUT HERE

297 INSERT FIG. 17 ABOUT HERE

298 Mutual shading of some rows of collectors has a negative impact on the  
299 production start-up and shut-down, increasing the start-up and decreasing  
300 the shut-down delay. In fact shaded rows do not collect useful heat and more-  
301 over behave as a radiator, wasting heat in convection and radiation losses and  
302 lowering the temperature at the inlet of the solar field. As a result, the heat-



303 ing process is slower and the temperature of HTF does not quickly reach  
304 values at which the system may be started-up, delaying start-up. On the  
305 other hand, during shut-down the HTF is cooled by the shaded rows and  
306 useful heat is wasted, reducing plant inertia. This effect is particularly evi-  
307 dent analyzing the HTF temperature at the collectors outlet at the beginning  
308 of day 2 (fig. 18) and the collectors radiation at the same time (fig. 13, 15).

309     INSERT FIG. 18 ABOUT HERE

310     Superheat temperature was kept constant at about 150 °C by the feeding  
311 pump acting on the liquid level of the evaporator (fig. 17) while the trend of  
312 temperature at the evaporator inlet was wrinkled by the effect of condensing  
313 temperature and by the effect of expander speed variation (fig. 19). Satu-  
314 ration pressure was kept at its set-point value (fig. 20). Obviously the lack  
315 of a thermal storage cause strong fluctuations in power generation. However  
316 a constant (or almost constant) power generation means that the expander  
317 rotates at constant speed at its design point (1500 rpm in the case of this  
318 analysis), requiring thermal storage, a larger solar multiple and therefore a  
319 larger collector field or an integration with an external heat source. Without  
320 the storage the production is not able to follow the radiation trend, but it  
321 allows to reduce the size of the solar field which is designed for the maximum  
322 plant power output when the expander rotates at 3000rpm. Due to the flex-  
323 ibility of the volumetric expander the plant can adapt itself to the variation  
324 of the boundary conditions.

325     INSERT FIG. 19 ABOUT HERE

326     INSERT FIG. 20 ABOUT HERE

327 *5.2.1. Influence of Concentration*

328 All these results were collected when  $C = 2$ . The results collected with  
329 this concentration were shown because this configuration provided the best  
330 performances, despite the limited acceptance angle.

331 As a comparison, the same analyses were performed with  $C=1.25$ . The  
332 number of collectors was increased to 1161 in order to provide the same  
333 maximum thermal power to the ORC cycle (150 kW), and the tilt angle was  
334 set at  $45^\circ$ .

335 As well known, a lower concentration results in a larger acceptance angle  
336 ( $106$  versus  $60$  degree in this case); this fact in theory would allow the collec-  
337 tors to collect the solar heat for a larger number of hours per day, however  
338 in practice the mutual shading between the rows makes ineffective this ad-  
339 vantage. In facts, when  $C=2$ , only the lower row is shaded as long as  $\alpha$  is  
340 lower than  $25^\circ$  (fig. 21), while when  $C=1.25$ , all the three rows are shaded  
341 as long as  $\alpha$  is respectively lower than  $25$ ,  $15$  and  $5^\circ$  (fig. 22).

342 INSERT FIG. 21 ABOUT HERE

343 INSERT FIG. 22 ABOUT HERE

344 Other effects make disadvantageous the use of  $C=1.25$  instead of  $C=2$ , since  
345 the electrical output proved to be more sensitive to variations of radiation:  
346 not only the collectors have a lower lower efficiency, but also a larger quantity  
347 of HTF fluid is needed due to the larger solar field, which led to a further  
348 increase in the plant warm-up period. As a result, on the fourth and fifth  
349 day production did no longer follow the solar radiation in the earliest hours  
350 of the days. Due to the longer warm-up period, the set point temperature  
351 ( $160^\circ$ ) was reached when the ORC cycle had already reached the set point

352 evaporating pressure (28,4 bar), as shown in fig. 23. The variation of HTF  
353 mass flow rate to keep the temperature at its set point caused a strong  
354 variation of thermal power input to the ORC cycle, emphasized by the higher  
355 slope of collectors efficiency [20]; in turn the expander speed increased in  
356 order to keep the evaporating pressure at its set point causing a fluctuation  
357 of the electrical output (fig. 24).

358 INSERT FIG. 23 ABOUT HERE

359 INSERT FIG. 24 ABOUT HERE

360 Even in this case, mutual shading of collectors along with low concen-  
361 tration was the cause of a long delay in the warm-up phase; the simulations  
362 showed the difficulty to properly tune the control system to handle fast phe-  
363 nomena, as reported by [13].

364 As a comparison, the results using the two different concentrations are  
365 summarized in tab. 3.

366 INSERT TAB. 3 ABOUT HERE

## 367 **6. Conclusions**

368 In this work, the dynamic model of a low concentration CPC power plant  
369 has been developed. The plant has been modelled in all its main parts and  
370 was controlled by the expander speed variation without the need of any  
371 storage system or integration with external heat source.

372 Simulations were carried out at different conditions of radiation. A first  
373 simulation was realized with clear sky conditions and a concentrating factor  
374 of collectors equal to 2, to set up parameters and showed the capacity of the  
375 plant of following solar radiation. Then five consecutive days of the month of

376 October were simulated. These days were representative of different radiation  
377 conditions and data were furnished by historical series.

378 Despite the low efficiency value, typical of these systems, the control  
379 strategy has proved to be suitable and even in various working conditions  
380 the plant has managed to follow the load variations and to keep all control  
381 parameters at their set point. Mutual shading of collectors was taken into  
382 account. Eventually results were compared to those obtained with  $C=1.25$   
383 collectors. Besides the lower overall efficiency, the slowness of warming up  
384 and the higher slope of the efficiency curve of the collectors stressed the  
385 control system, which was able to keep operative parameters at their set  
386 point value, but production has not been able to follow solar radiation. The  
387 use of higher concentration collectors coupled with a simple tracking system,  
388 may reduce warm up lag, increase efficiency of the system, and reduce the  
389 number of collectors on the field.

390 The model has shown the potential of volumetric expanders to be a valid  
391 alternative to the use of thermal storage or integration with external sources  
392 and this type of regulation can be adopted in several low power application  
393 (waste heat recovery or low temperature geothermal systems) where thermal  
394 power input is variable over time.

## 395 **References**

- 396 [1] Rabl A, Goodman NB, Winston R. Practical design considerations for  
397 CPC solar collectors. *Solar Energy* 1979; 22 (4): 373-381.
- 398 [2] Mills DR, Basset IM, Derrick GH Relative cost-effectiveness of CPC re-

- 399 flector designs suitable for evacuated absorber tube solar collectors. *Solar*  
400 *Energy* 1986; 36 (3): 199-206.
- 401 [3] Farouk Kothdiwala A, Eames PC, Norton B. Optical performance of an  
402 asymmetric inverted absorber compound parabolic concentrating solar col-  
403 lector. *Renewable Energy* 1996; 9 :576-9.
- 404 [4] Antonelli M, Baccioli A, Francesconi M, Lensi R, Martorano L. Analysis  
405 of a Low Concentration Solar Plant with Compound Parabolic Collectors  
406 and a Rotary Expander for Electricity Generation. *Energy Procedia* 2014;  
407 45: 170-9.
- 408 [5] Antonelli M, Martorano L. A Study on the Rotary Steam Engine for  
409 Distributed Generation in Small Size Power Plants. *Applied Energy* 2012;  
410 97: 642-7.
- 411 [6] Antonelli M, Baccioli A, Francesconi M, Desideri U, Martorano L. Op-  
412 erating maps of a rotary engine used as an expander for micro-generation  
413 with various working fluids. *Applied Energy* 2014; 113: 742-750.
- 414 [7] Quoilin S, Declaye S, Legros A, Guillaume L, Lemort V. Working fluid  
415 selection and operating maps for Organic Rankine Cycles expansion ma-  
416 chines. *International Compressor Engineering Conference at Purdue* 2012.
- 417 [8] Badami M, Mura M. Preliminary design and control strategies of a small  
418 scale wood waste Rankine cycle (RC) with a reciprocating steam engine  
419 (SE). *Energy* 2009; 34: 1315-1324.
- 420 [9] Antonelli, M., Baccioli, A., Francesconi, M., Martorano, L. Experimental  
421 and numerical analysis of the valve timing effects on the performances of a

- 422 small volumetric rotary expansion device (2014) Energy Procedia, 45, pp.  
423 1077-1086.
- 424 [10] Vitte P, Manenti F, Pierucci S, Joulia X, Buzzi-Ferraris G., (2012),  
425 Dynamic simulation of concentrating solar plants, Chemical Engineering  
426 Transactions, 29, 235-240.
- 427 [11] Manenti F, Ravaghi-Ardebili Z. Dynamic simulation of concentrating  
428 solar power plant and two-tanks direct thermal energy storage. Energy  
429 2013; 55: 89-97.
- 430 [12] El Hefni B. Dynamic modeling of concentrated solar power plants with  
431 the ThermoSysPro library (Parabolic Trough collectors, Fresnel reflector  
432 and Solar-Hybrid). Energy Procedia 2014; 49: 1127-1137.
- 433 [13] Rodat S, Souza JVD, Thebault S, Vuillerme V, Dupassieux N. Dynamic  
434 simulations of Fresnel solar power plants. Energy Procedia 2014; 49: 1501-  
435 1510.
- 436 [14] Eck M, Hirsch T. Dynamics and control of parabolic trough collector  
437 loops with direct steam generation. Solar Energy 2007; 81: 268-279.
- 438 [15] Henrion T, Ponweiser K, Band D, Telgen T. Dynamic simulation of a  
439 solar power plant steam generation system. Simulation Modelling Practice  
440 and Theory 2013; 33: 2-17.
- 441 [16] Quoilin S, Aumann R, Grill A, Schuster A, Lemort V, Spliethoff V.  
442 Dynamic modelling and optimal control strategy of waste heat recovery  
443 Organic Rankine Cycles. Applied Energy 2011; 88: 2183-2190.

- 444 [17] Antonelli M, Baccioli A, Francesconi M, Desideri U, Martorano L. Elec-  
445 trical Production of a Small Size Concentrated Solar Power Plant with  
446 Compound Parabolic Collectors. Renewable Energy 2015. Article in press.
- 447 [18] Gudekar AS, Jadhav AS, Panse SV, Joshi JB, Pandit AB. Cost effective  
448 design of compound parabolic collector for steam generation. Sol Energy  
449 2013;90: 4350.
- 450 [19] V. Lemort, S. Quoilin, C. Cuevas, J. Lebrun. Testing and modeling a  
451 scroll expander integrated into an Organic Rankine Cycle. Applied Ther-  
452 mal Engineering 2009; 29: 30943102.
- 453 [20] Farouk Kothdiwala A, Norton B, Eames PC. The effect of variation of  
454 angle of inclination on the performance of low-concentration-ratio com-  
455 pound concentrating solar collector. Solar Energy 1995; 55 (4): 301-9.
- 456 [21] Rabl A. Comparison of solar concentrators. Solar Energy 1975; 18: 93-  
457 111.
- 458 [22] European rule UNI EN ISO 15927-4
- 459 [23] AMESim Thermal Hydraulic Tutorial Guide
- 460 [24] AMESim Two Phase Flow Tutorial Guide.